

Structure Refinements of II-VI Semiconductor Nanoparticles based on PDF Measurements

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Universität Erlangen

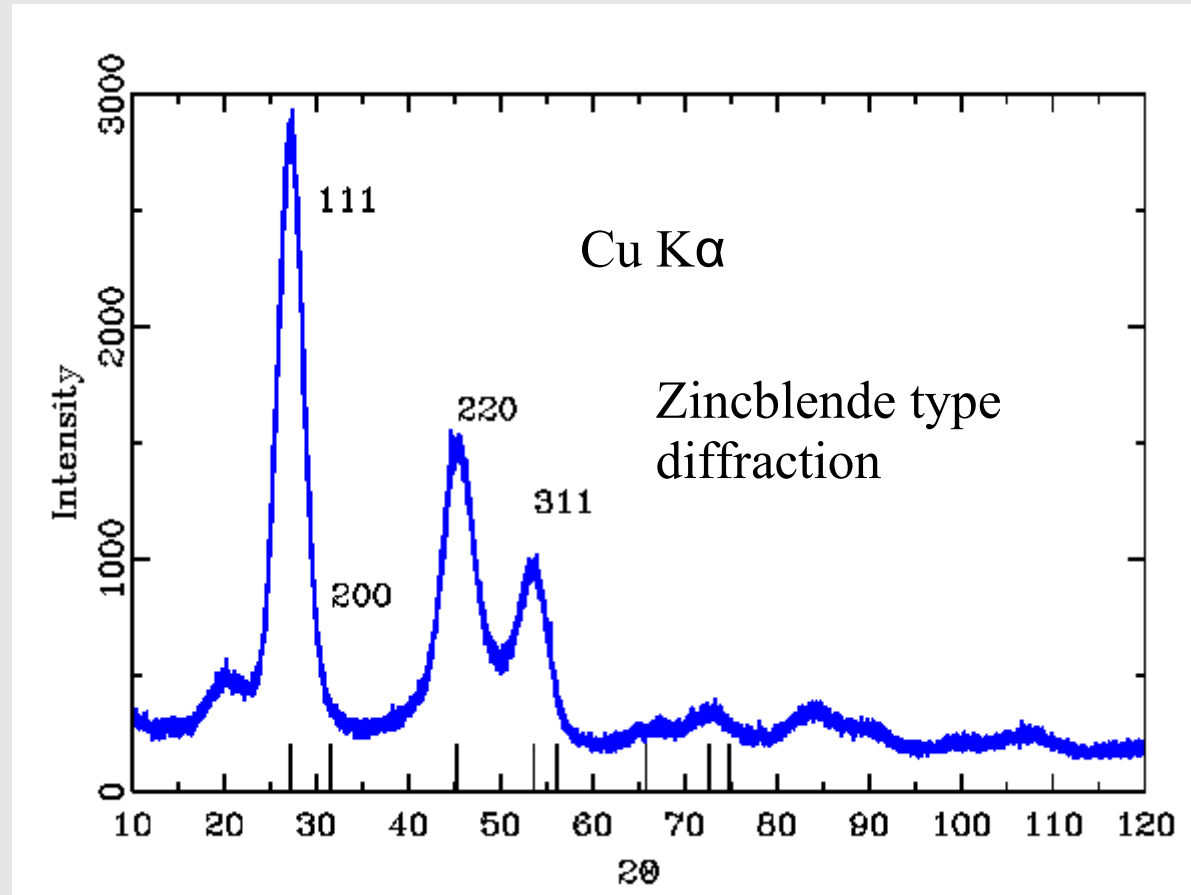
neder@krist.uni-erlangen.de

ZnSe Nanoparticles

Synthesis: Se in Trioctylphosphine + ZnEt₂
into Hexadecylamin at 310 C

FWHM₁₁₁=3.3

Size ~ 26 Å



ZnSe Nanoparticles

Rietveld Refinement: Zincblende Structure

$$a = 4.00 \text{ \AA}$$

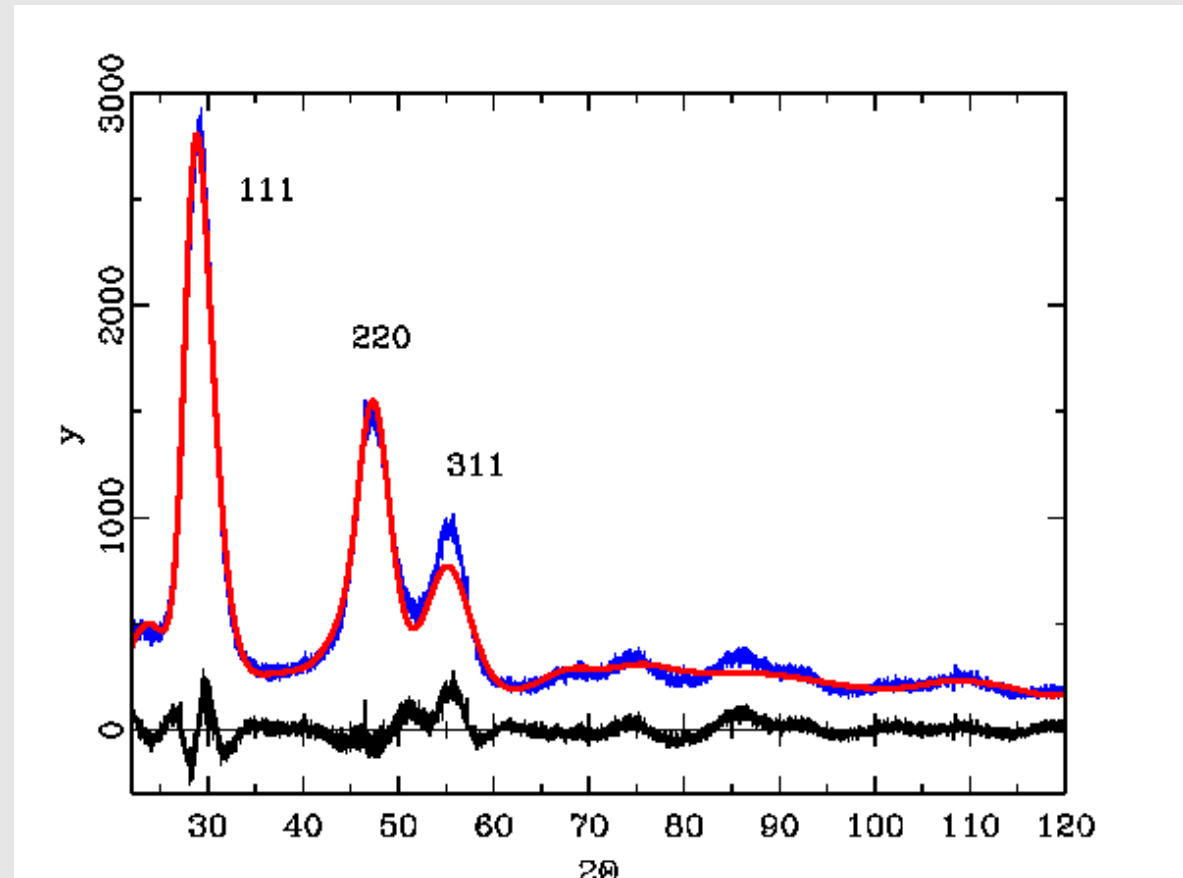
$$\text{Zn-Se} = 2.45 \text{ \AA}$$

$$\text{FWHM}_{111} = 3.3$$

$$\text{Size} \sim 26 \text{ \AA}$$

$$R_{\text{wp}} = 14\%$$

no fit at 311, high order hkl
disordered material



ZnSe Nanoparticles Fitting by Debye

Debye formula :

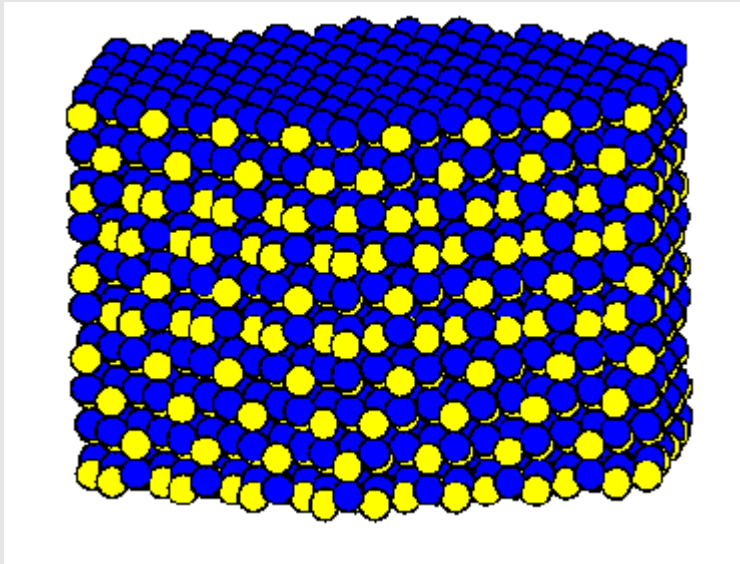
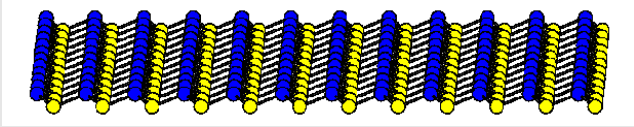
$$\langle |F(\mathbf{h})|^2 \rangle = \sum_j f_j^2 + \sum_i \sum_{j \neq i} f_i f_j \frac{\sin(2\pi \mathbf{h} \cdot \mathbf{r}_{ij})}{(2\pi \mathbf{h} \cdot \mathbf{r}_{ij})}$$

Sum over all atom pairs

→ no restrictions on sample structure

open to finite particle with any shape
defects like stacking faults etc.

creating ZnSe Nanoparticles



$\{110\}$ and $\{001\}$

create a large single Wurtzite layer A/B

Stack along c (with faults)

Cut to proper size

Calculate powder pattern

Repeat and average

Repeat with new set of parameter

using a Differential Evolutionary Scheme

ZnSe Nanoparticles

Debye Refinement: Stacking of layers, almost Zincblende structure

$$a = 3.997 \text{ \AA}$$

$$c = 6.501 \text{ \AA}$$

$$\text{Zn-Se} = 2.39 \text{ \AA}$$

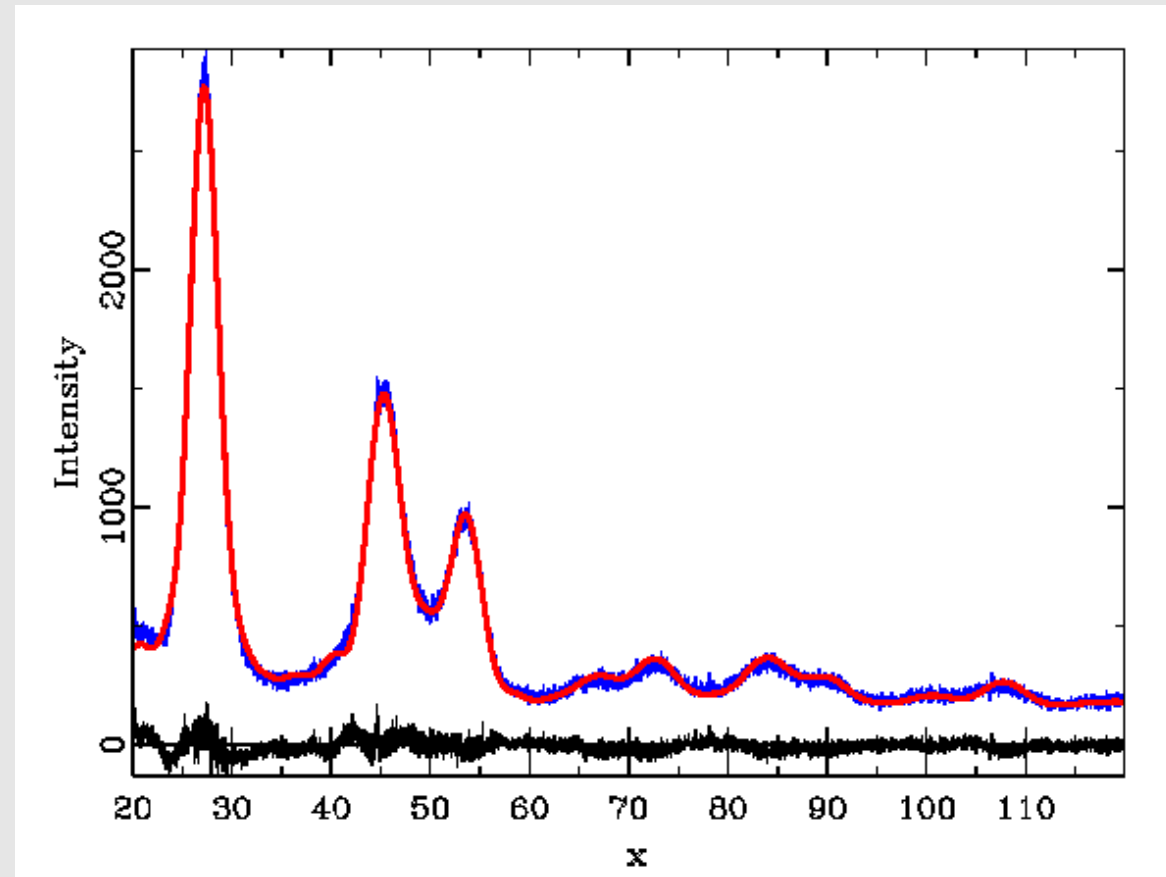
$$\text{Zn-Se} = 2.46 \text{ \AA}$$

$$\text{size a-b} = 26(2) \text{ \AA}$$

$$\text{size c} = 32(2) \text{ \AA}$$

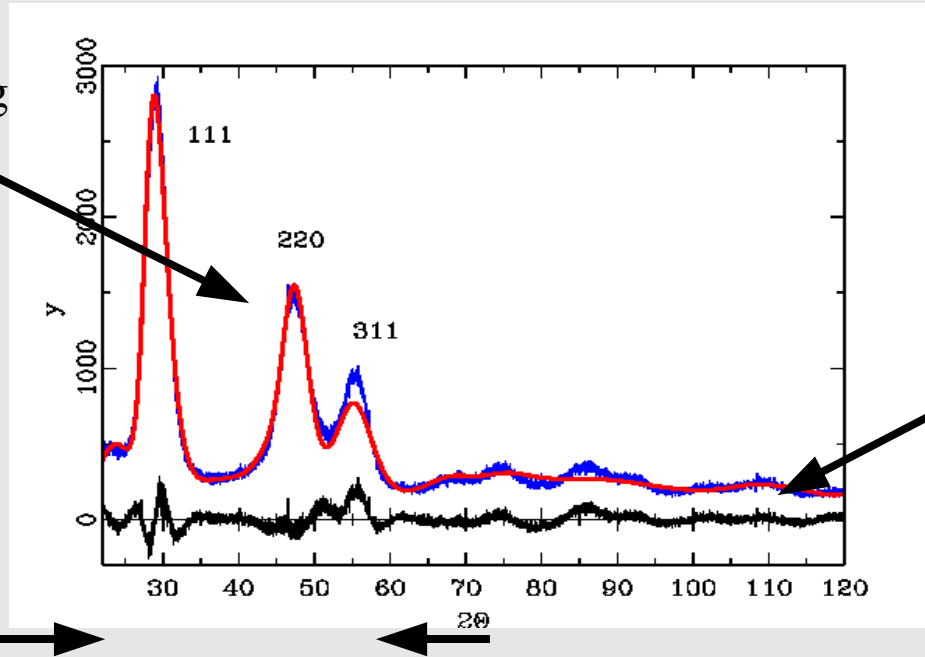
30% stacking fault probability

$$R_{wp} = 5\%$$



Powder Diffraction

Powder diffraction pattern of a nanoparticle ZnSe



broad overlapping
Bragg reflections

small particle
size

Bragg
reflections
widened
artificially

Rietveld Refinement

large background compared to
Bragg reflections at higher 2θ

defects,
organic ligands
sample environment

Accurate Background
estimation very difficult

very limited 2θ range with
significant reflections

small particle size
defects

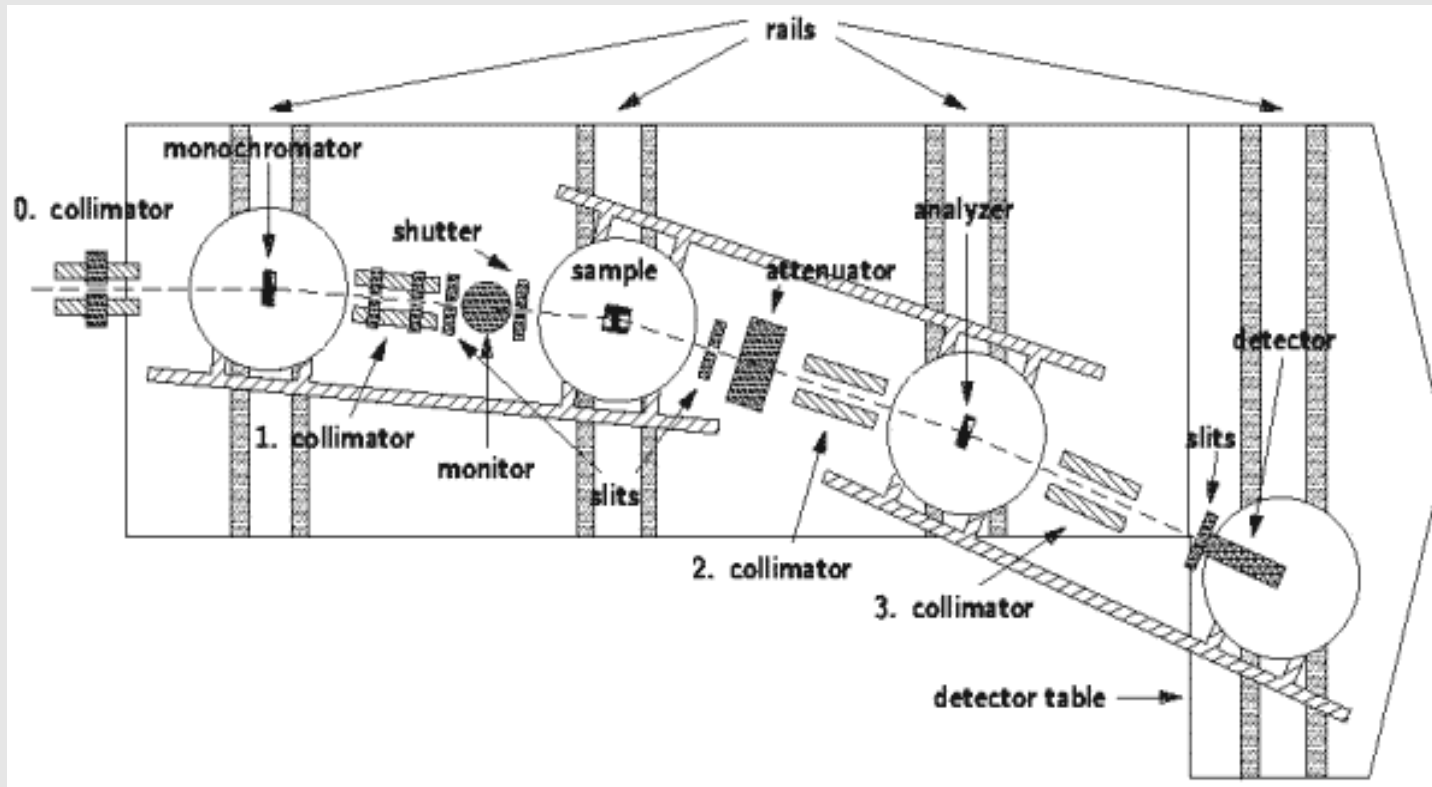
high uncertainties of
structural parameters

limited information content,
high correlation between parameters
defects and size not well treated

PDF Data Collection

collect powder pattern to high 2Θ with high energy X-ray radiation

BW5 HASYLAB, DESY, Germany



$$\lambda = 0.088 \text{ \AA}$$
$$E = 140 \text{ keV}$$

$$2\Theta_{\max} = 35^\circ$$

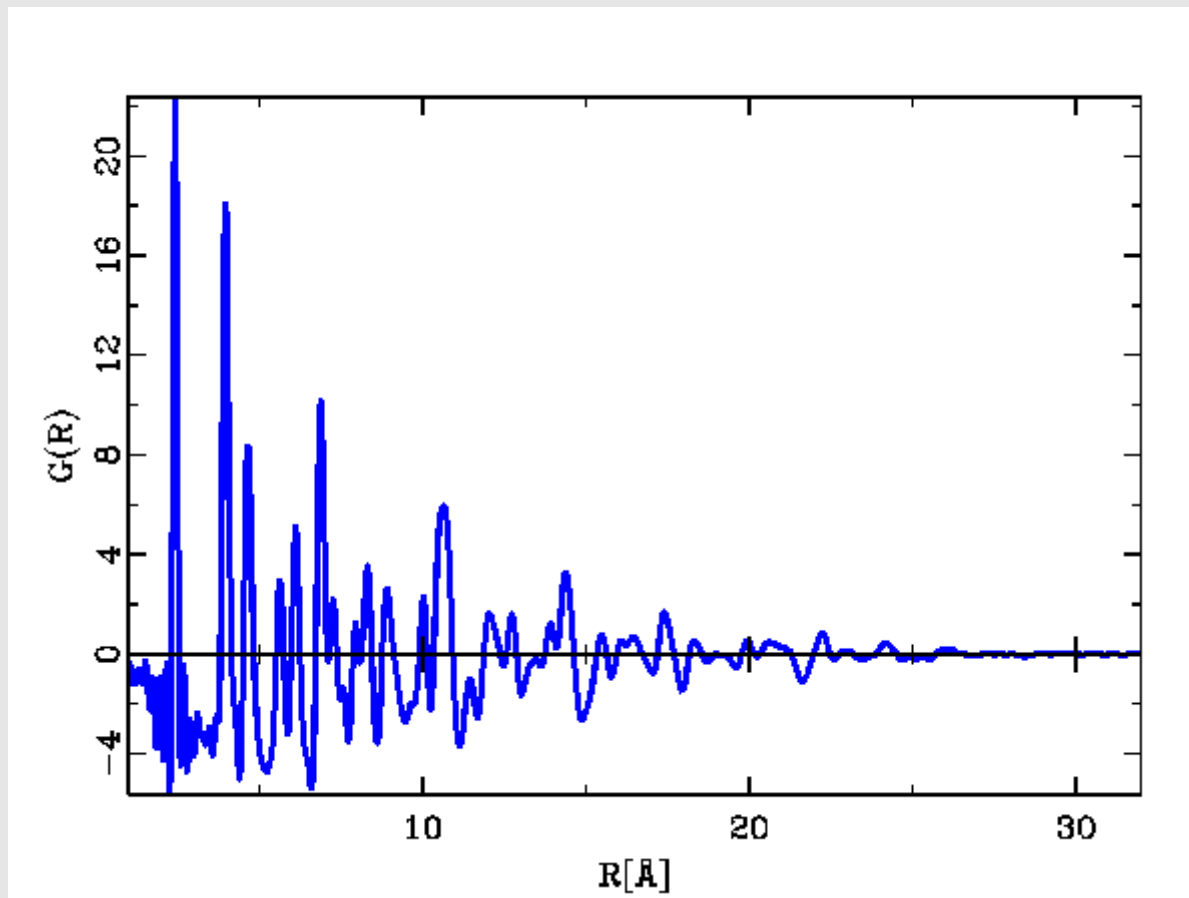
$$T = 15 \text{ K}$$

$$h_{\max} = \left(\frac{\gamma \sin(\Theta)}{\lambda} \right)_{\max} = \gamma \cdot \circ \text{ \AA}^{-1}$$

$$Q_{\max} = \gamma \pi \left(\frac{\gamma \sin(\Theta)}{\lambda} \right)_{\max}$$
$$= \xi \gamma \text{ \AA}^{-1}$$

alternatively
neutron diffraction

ZnSe experimental PDF



Data collection at BW5,
HASYLAB, Germany

$$\lambda = 0.1036 \text{ \AA}$$

$$E = 120 \text{ keV}$$

$$T = 15 \text{ K}$$

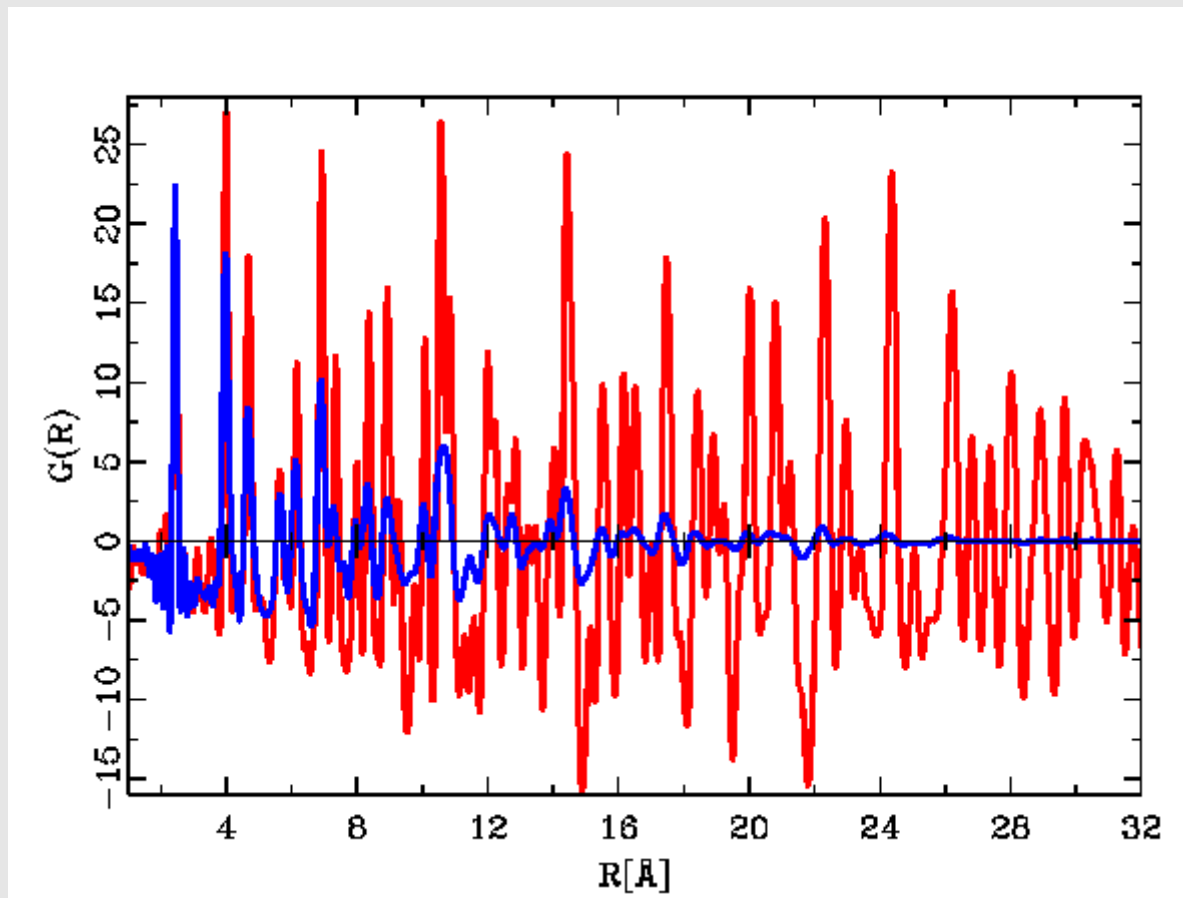
capillary, 2.5 mm diameter

$$2\Theta_{\max} = 32^\circ$$

$$Q_{\max} = \gamma \pi \left(\frac{\gamma \sin(\Theta)}{\lambda} \right)_{\max}$$
$$= \gamma \cdot \lambda \circ \text{ \AA}^{-1}$$

Data treatment as in Korsounski et al., J. Appl. Cryst. **36**, 1389 (2003)

ZnSe: Comparison to crystalline ZnSe

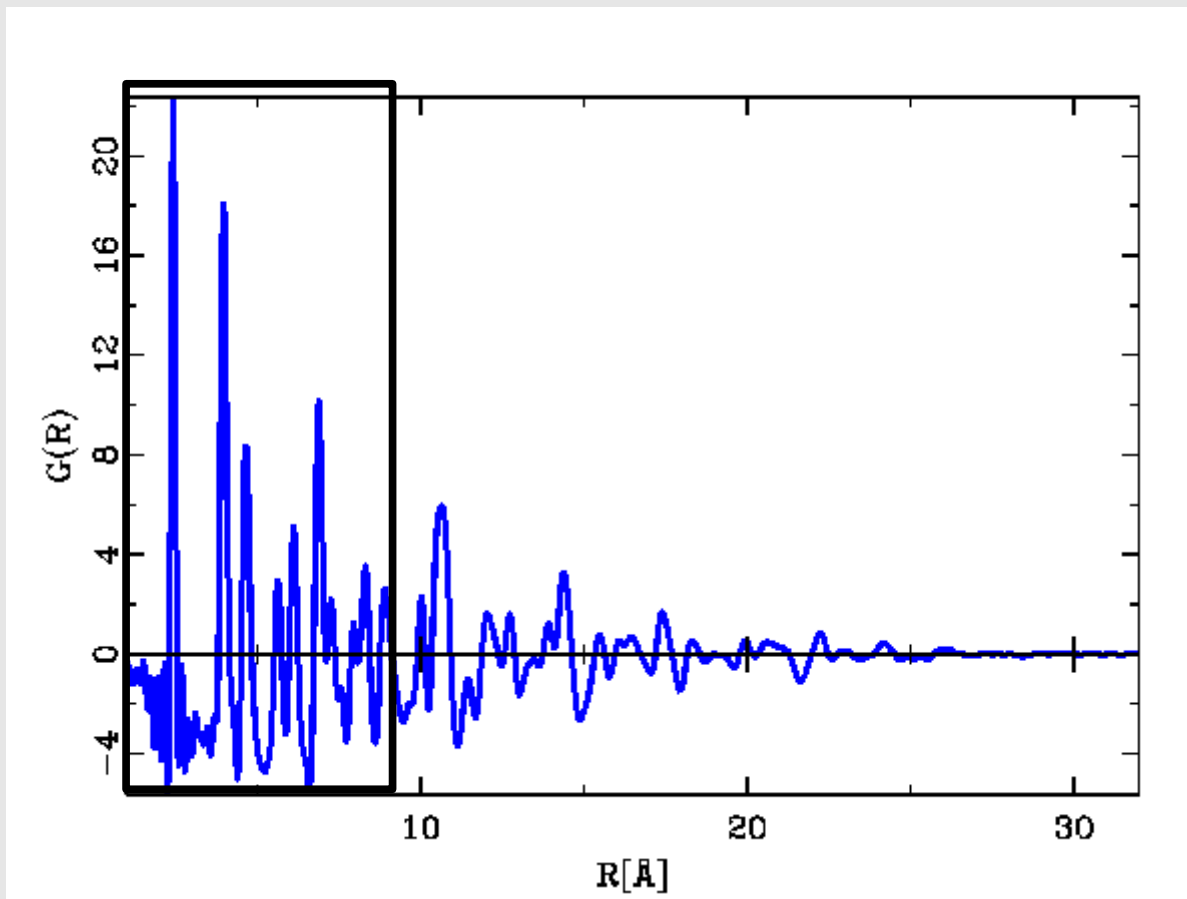


crystalline ZnSe

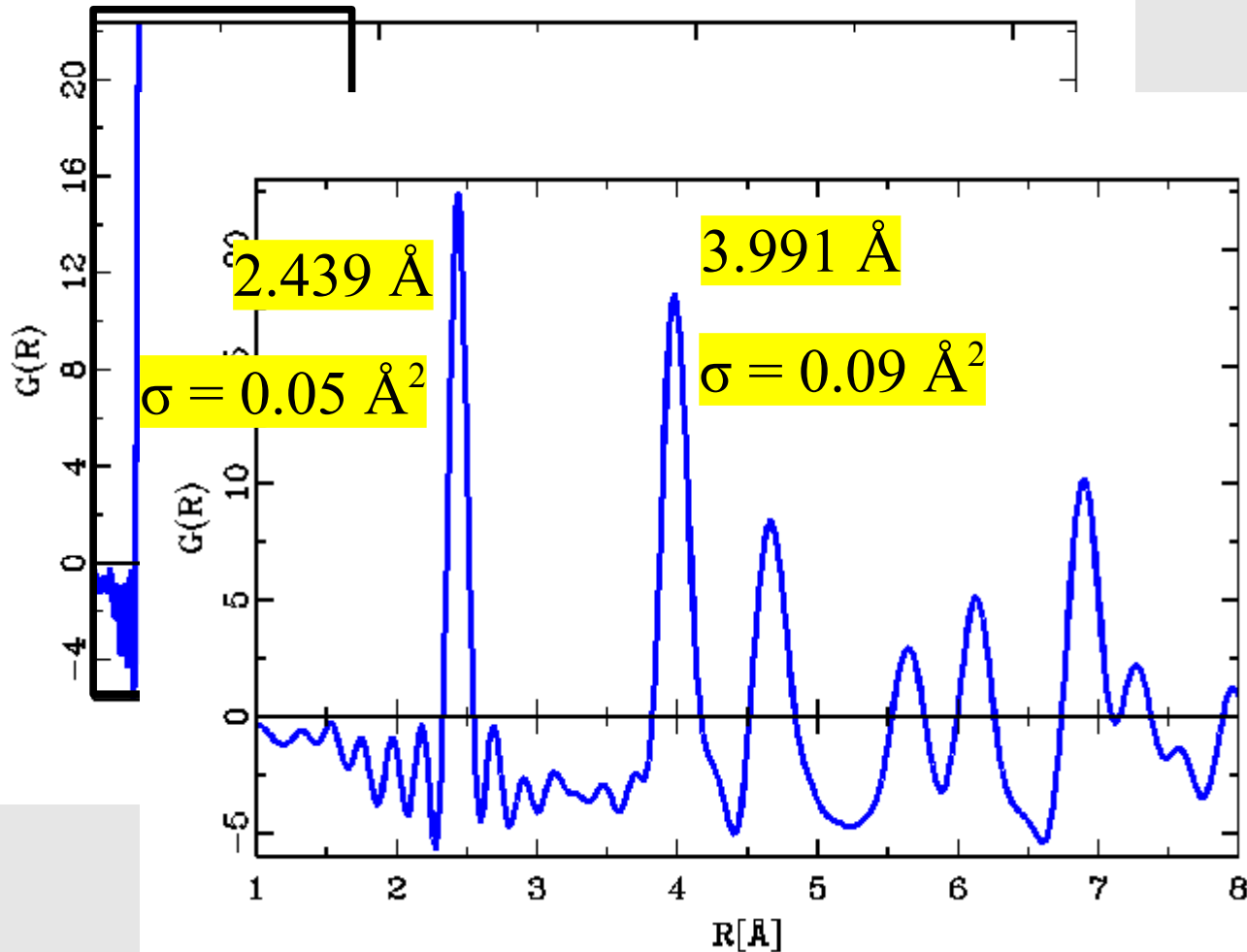
nanocrystalline ZnSe

identical experimental conditions for both samples

ZnSe experimental PDF

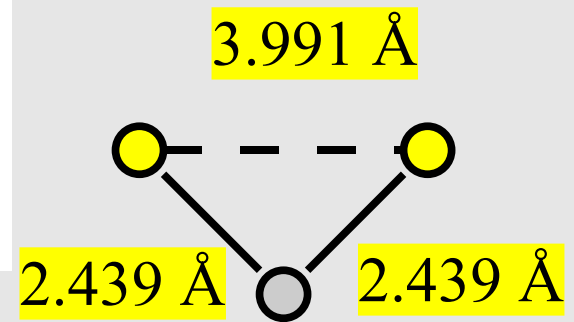


ZnSe experimental PDF

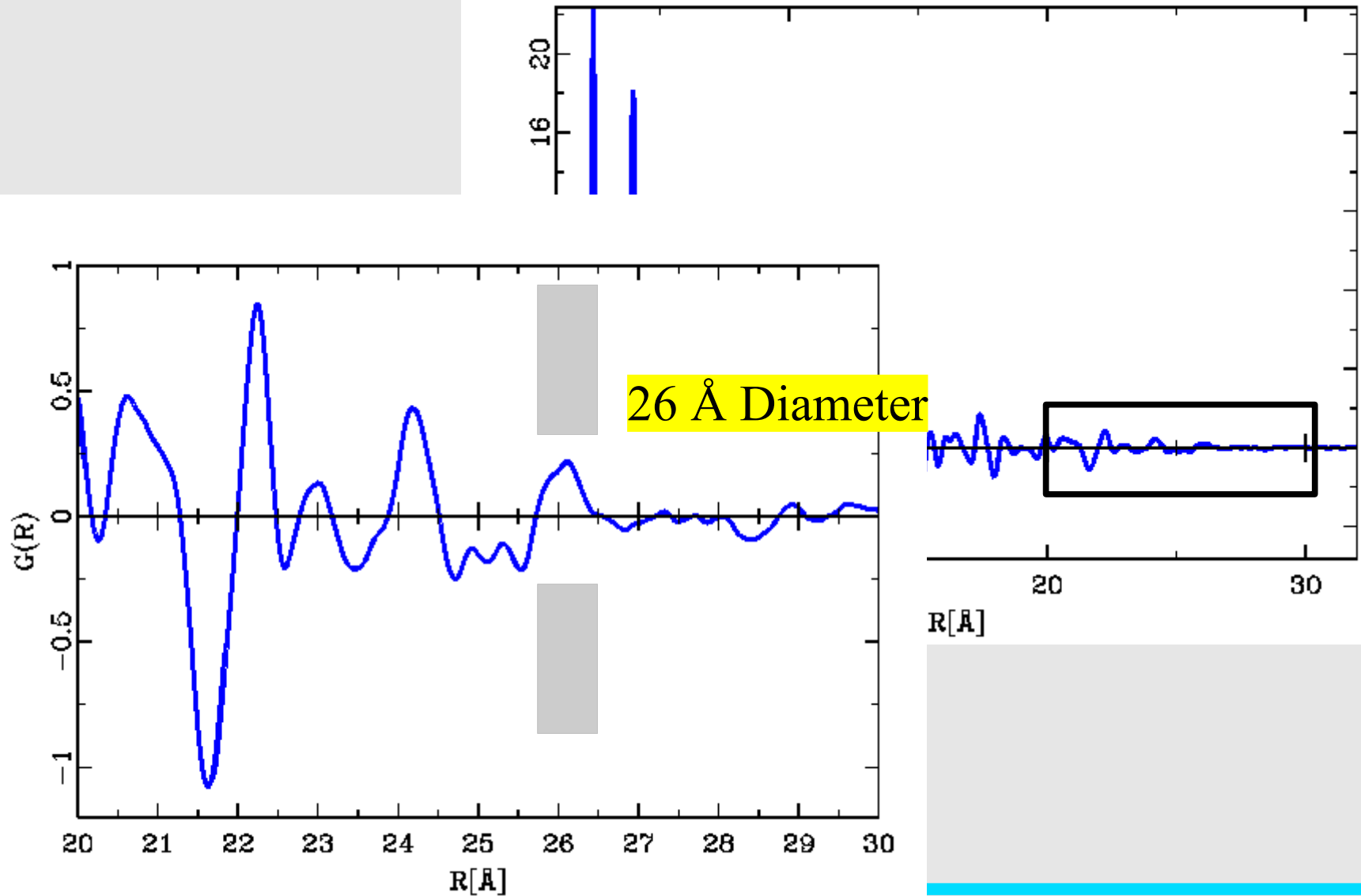


tetrahedral structure

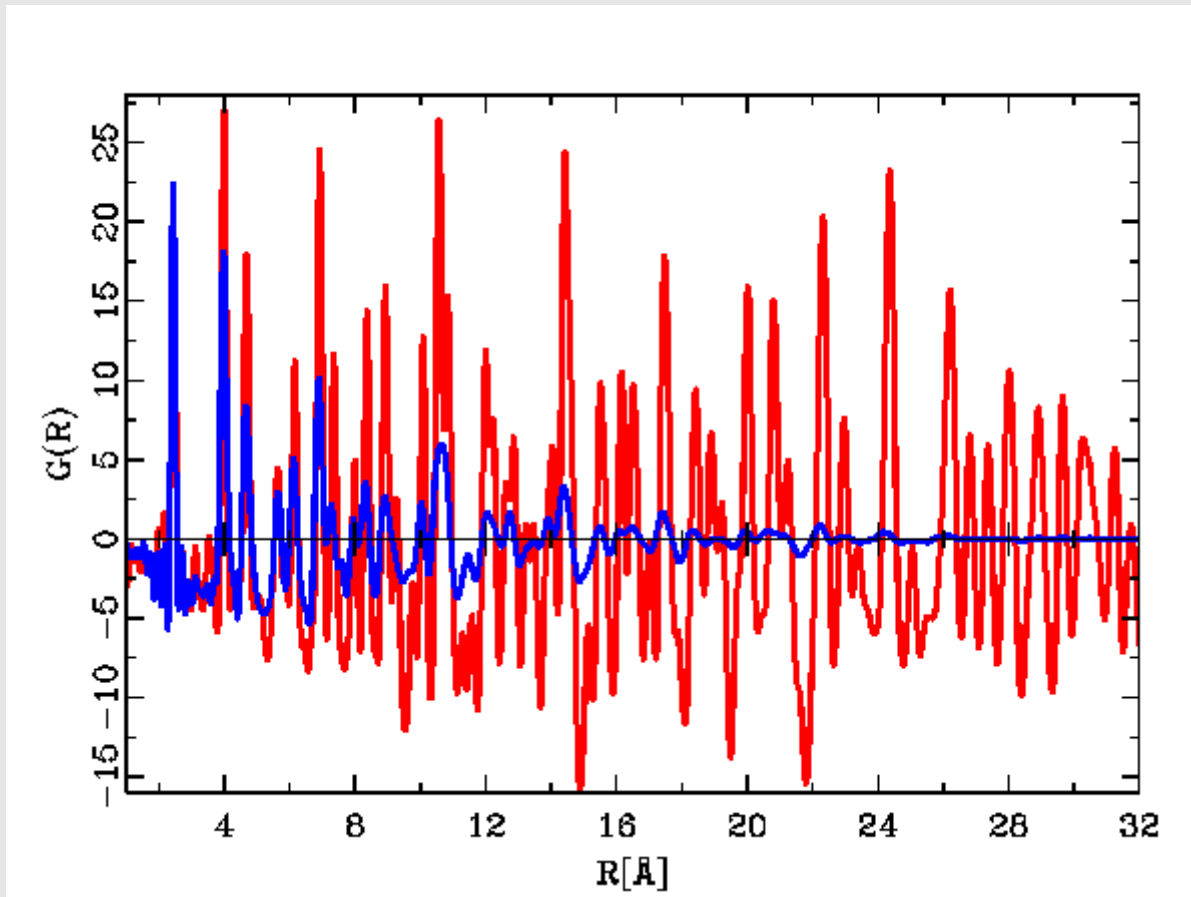
bond angle 109.8°



ZnSe Nanoparticles



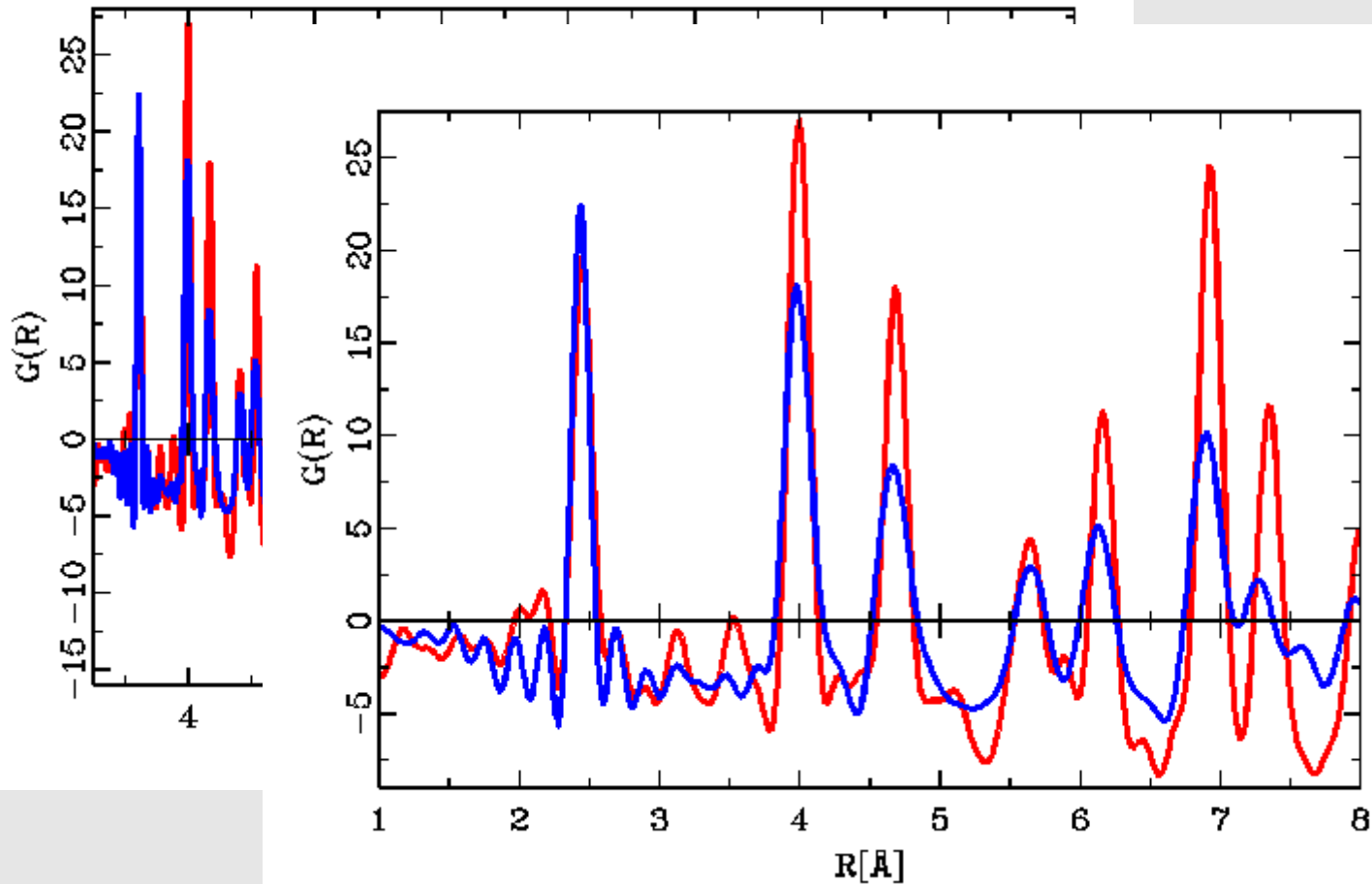
ZnSe: Comparison to crystalline ZnSe



crystalline ZnSe

nanocrystalline ZnSe

ZnSe: Comparison to crystalline ZnSe



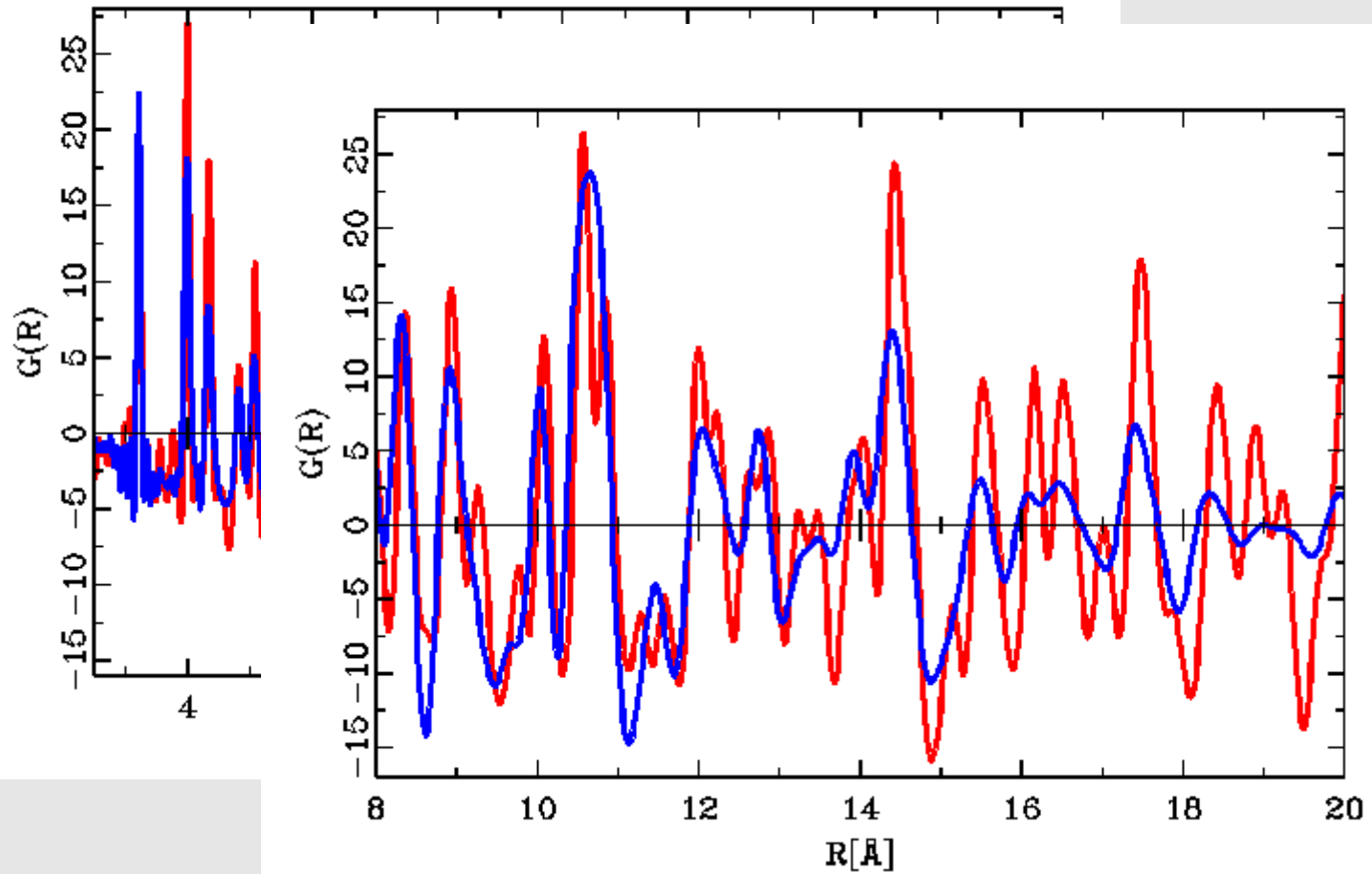
2.439 \AA $\sigma = 0.05 \text{\AA}^2$

3.991 \AA $\sigma = 0.09 \text{\AA}^2$

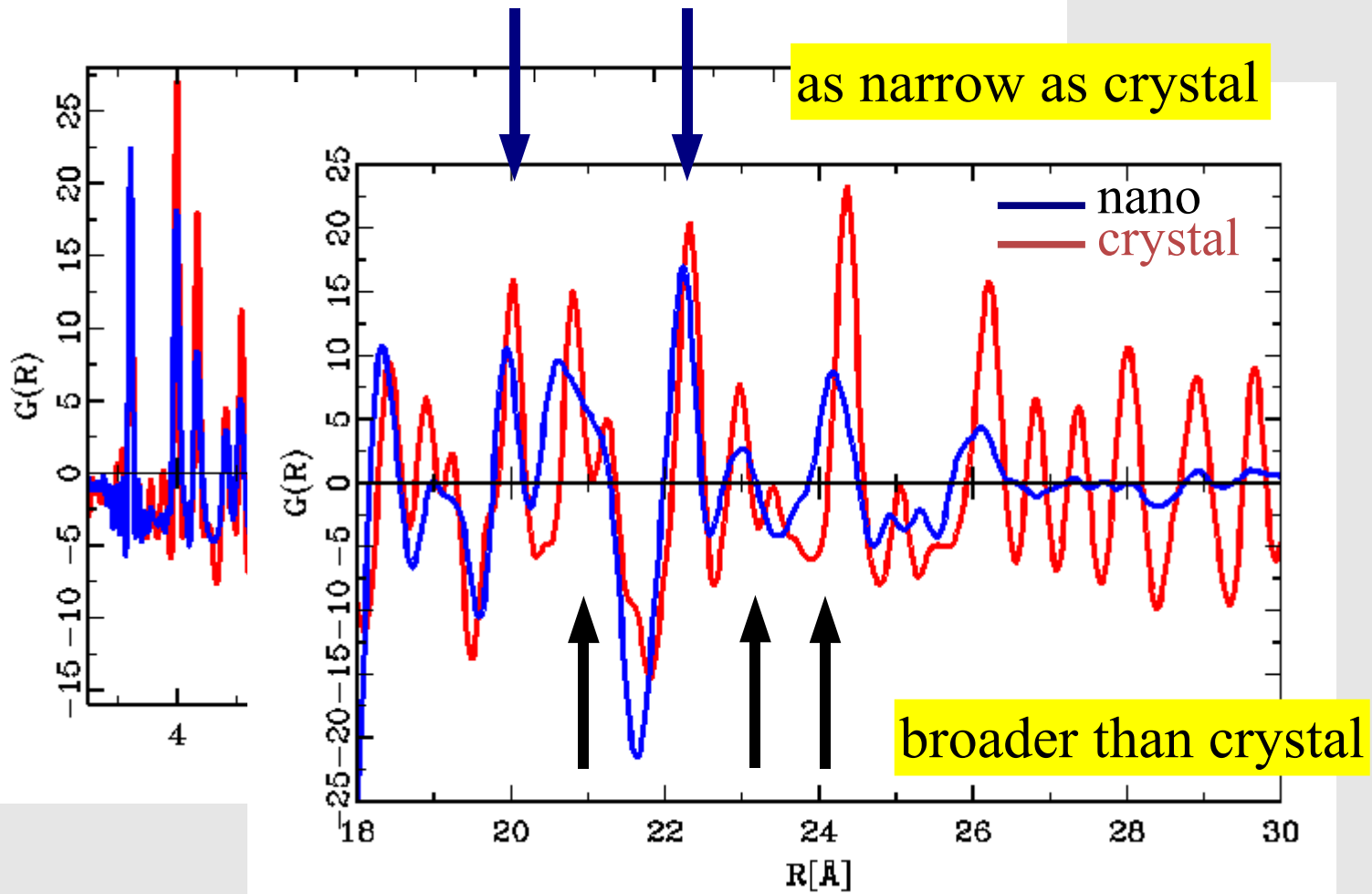
2.450 \AA $\sigma = 0.05 \text{\AA}^2$

3.999 \AA $\sigma = 0.06 \text{\AA}^2$

ZnSe Nanoparticles

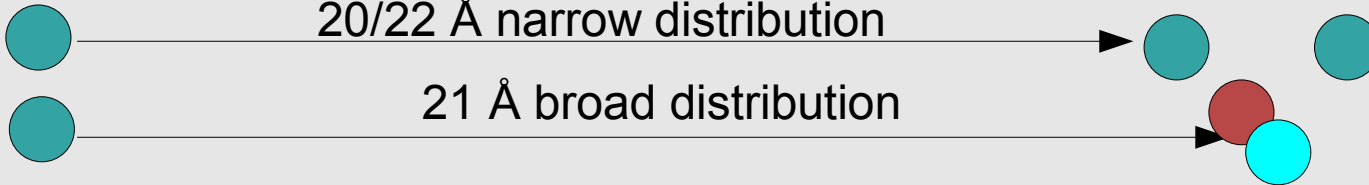


ZnSe Nanoparticles



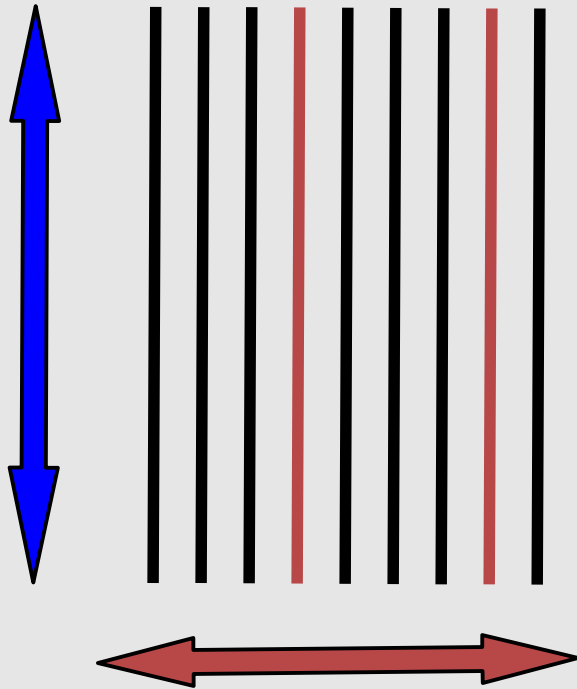
20/22 \AA narrow distribution

21 \AA broad distribution

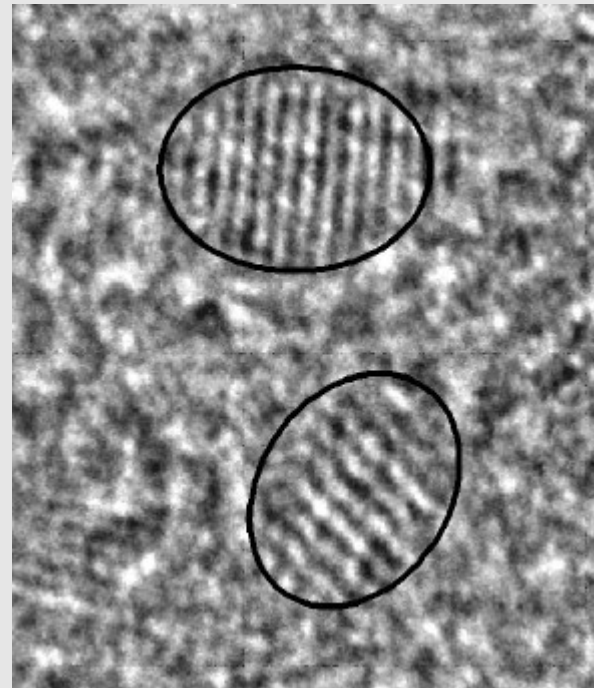


ZnSe Nanoparticles

structural coherence



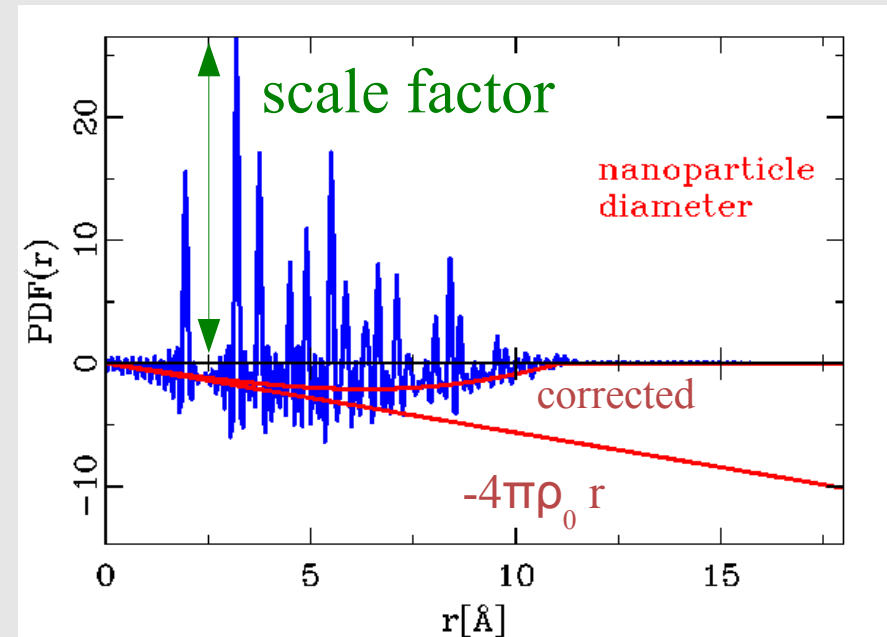
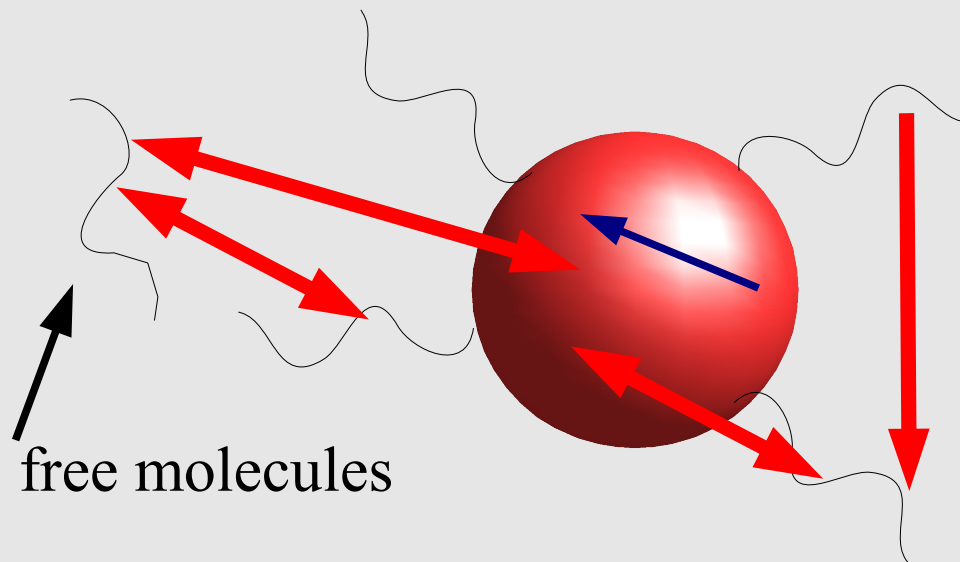
~8 to 10 monolayers
= 4 to 5 unit cells along c
= 24 to 30 Å



loss of coherence due
to stacking faults

Calculation of the PDF for nanoparticles

Nanoparticle with core and stabilizing molecules



Vectors within core defined by model structure

ill defined vectors, not part of the structural model

volume ratio, inaccurate chemical analysis, not part of model

Algorithms for PDF Simulation of Nanoparticles

Simulate a crystal of $N \times M \times O$ cells

calculated PDF with periodic boundary conditions
multiply PDF by suitable shape function

Howell et al., Phys. Rev. B **73**, 094107 (2006)

Kodama et al., Acta. Cryst. A **62**, 444 (2006)

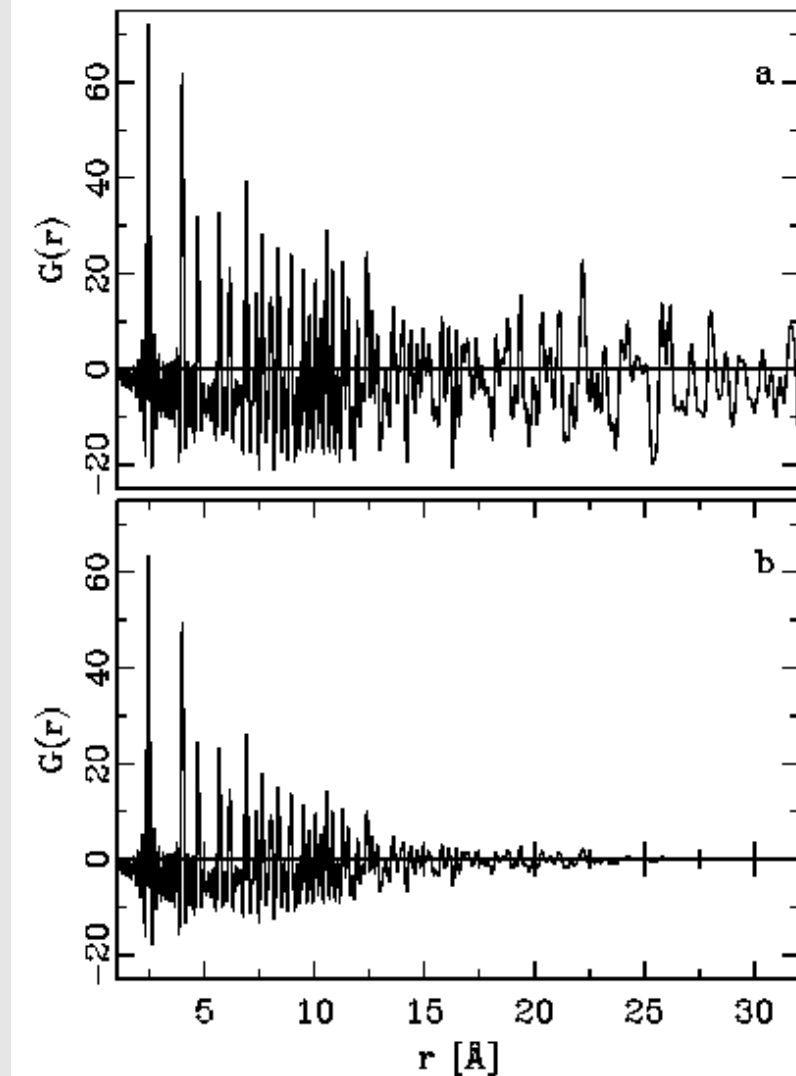
Simulate a finite nanoparticle

calculate PDF from finite model
correct shape of $-4 \pi \rho_0 r$ line

Neder et al. J. Phys.: Condens. Matter **17**, S125 (2005)

Neder et al. phys. stat sol. (c), **4**, 3221 (2007)

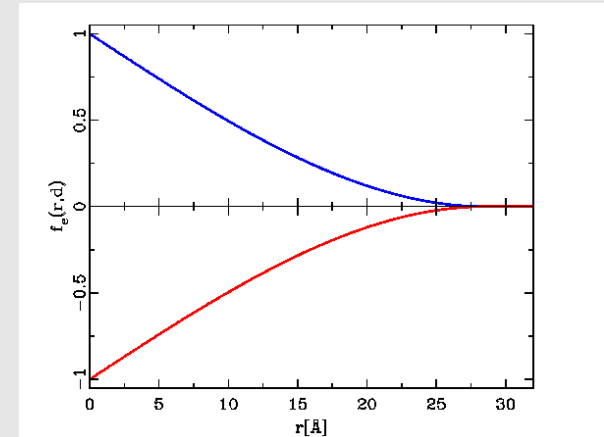
PDF Simulation of Nanoparticles; envelope function



PDF of periodic ZnSe

q_{\max} , q_{α} , etc. taken from fit to crystalline sample

as above, PDF multiplied by envelope function for a sphere



$$\text{PDF}_{\text{nano}} = \text{PDF}_{\text{crystal}} * f_e(r,d)$$

$$f_e(r,d) = 1 - \frac{3}{2} \frac{r}{d} + \frac{1}{2} \left(\frac{r}{d}\right)^3$$

defects can be treated

limited to basic shapes

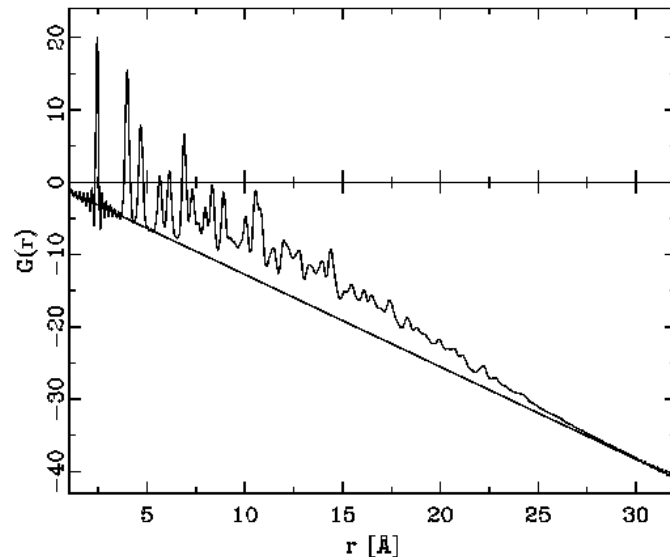
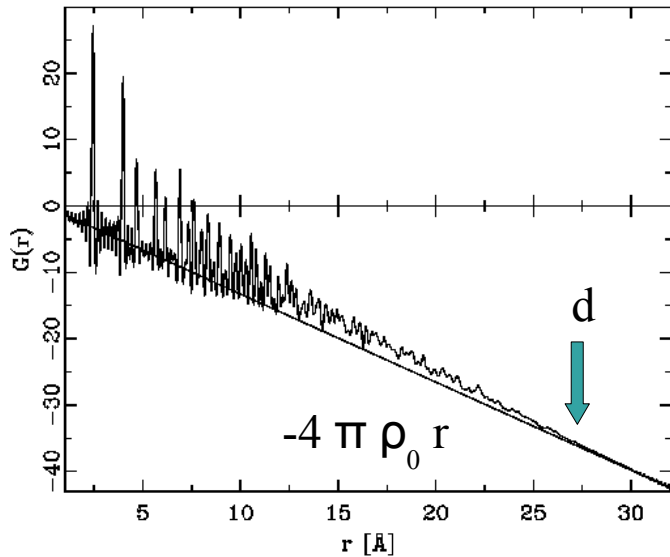
treats two different effects!

finite particle size

change of average number density

PDF Simulation of Nanoparticles; finite particle

Simulation of a single finite sized ZnSe particle



PDF calculated without periodic boundary conditions

q_{\max} , q_{α} , etc. taken from fit to crystalline sample

open to any shape
here elliptical shape!

defects can be treated

defects in a single simulation are **NOT** a true representation for whole sample

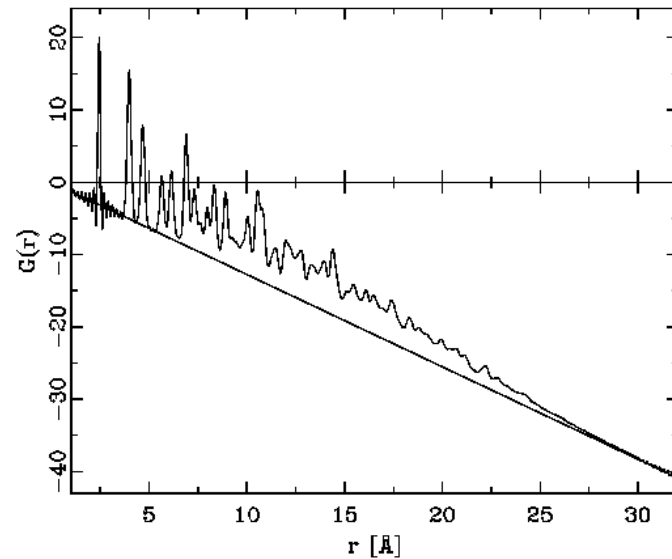
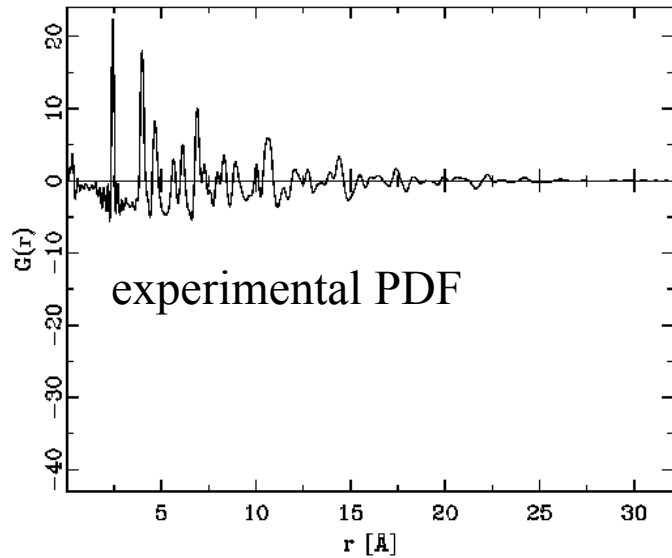
requires assembly average

assembly average may include:
defect distribution
size/shape distribution

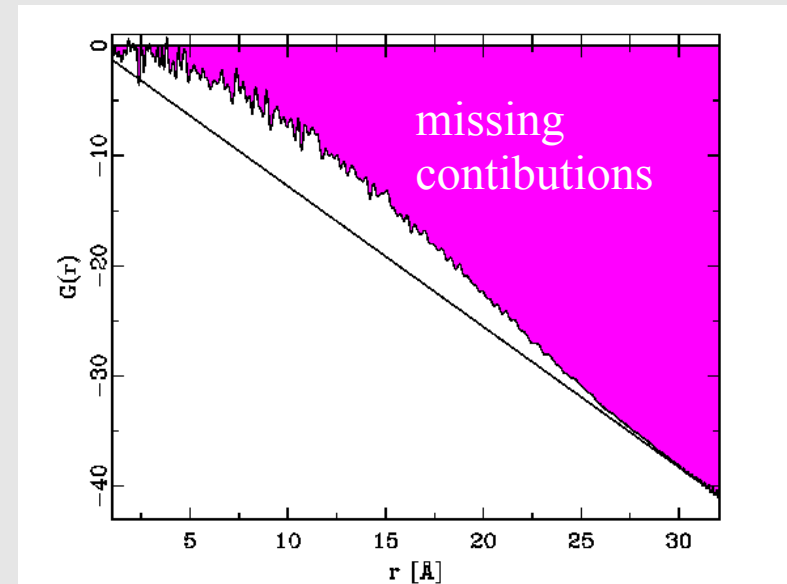
average PDF of 20 individual particles
with stacking fault

PDF Simulation of Nanoparticles; finite particle

Simulation of a single finite sized ZnSe particle



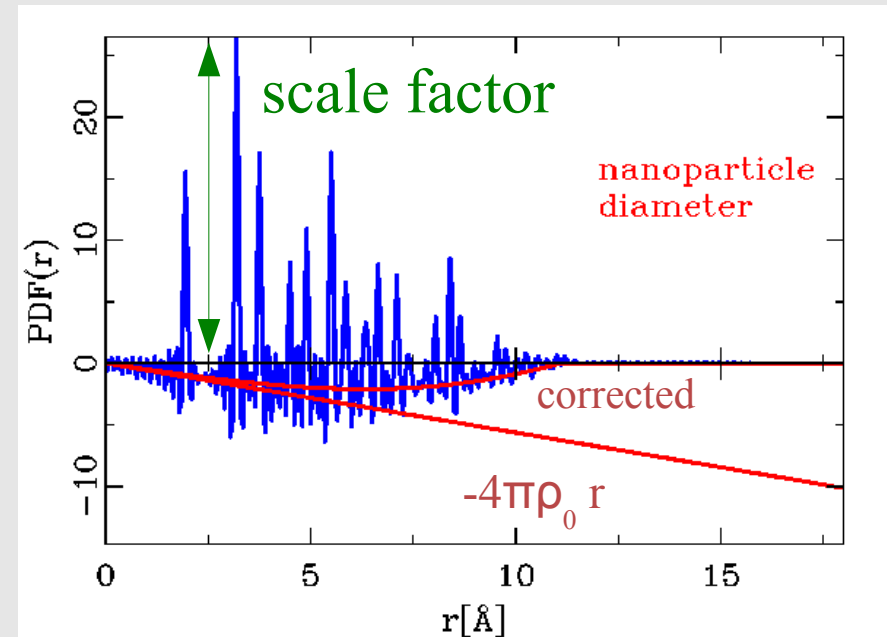
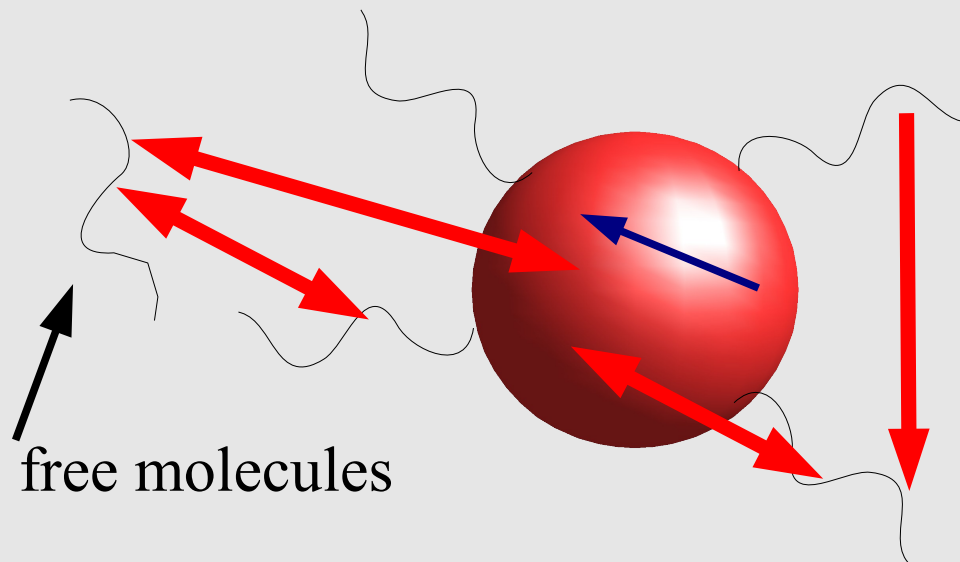
Difference calc - exp:



average PDF of 20 individual particles
with stacking fault

Calculation of the PDF for nanoparticles

Nanoparticle with core and stabilizing molecules



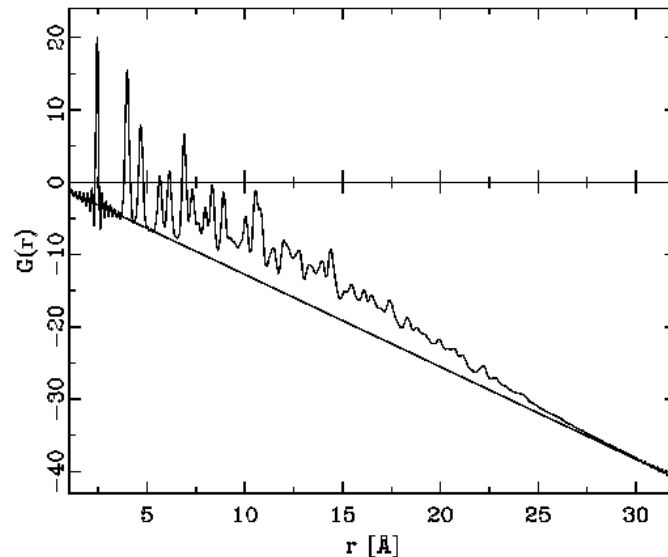
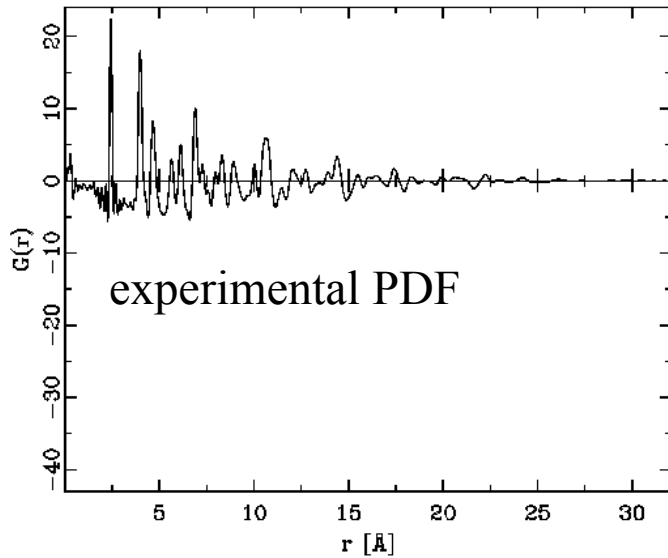
Vectors within core defined by model structure

ill defined vectors, not part of the structural model

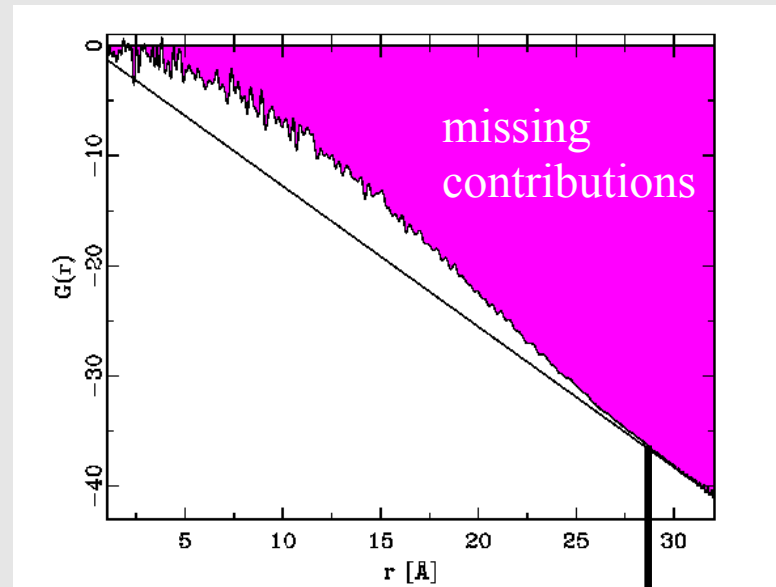
volume ratio, inaccurate chemical analysis, not part of model

PDF Simulation of Nanoparticles; finite particle

Simulation of a single finite sized ZnSe particle



Difference calc - exp:



$r < d$:
vectors within model

$r > d$:
no vectors in model
 $G(r) = 0$ instead of
 $-4 \pi \rho_0 r$

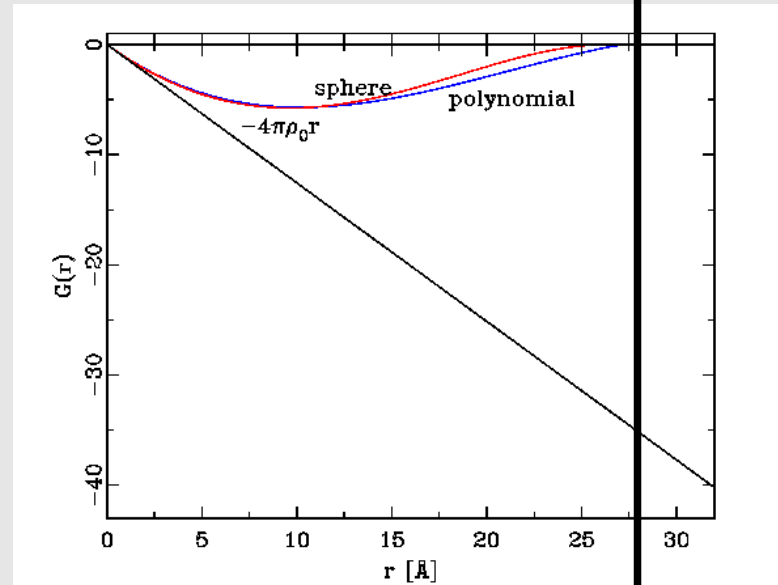
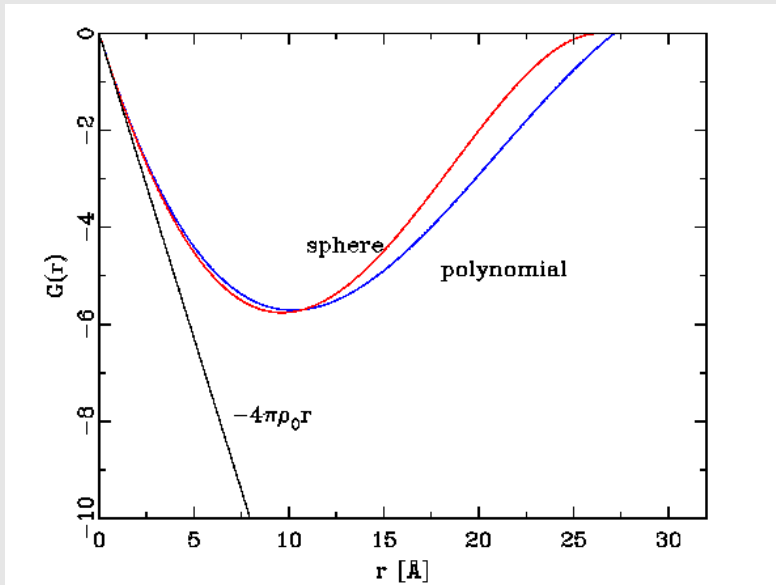
$G(r)_{\text{total}}$ is:

$$-4 \pi \rho_0 r + p_0 + p_1 r + p_2 r^2 + p_3 r^3 + G(r)_{\text{model}}$$

average PDF of 20 individual particles
with stacking fault

PDF Simulation of Nanoparticles; finite particle

Simulation of a single finite sized ZnSe particle



$r < d$:

vectors in model:

$G(r) = G(r)_{model} + \text{background contribution}$

$$-4 \pi \rho_0 r + p_0 + p_1 r + p_2 r^2 + p_3 r^3$$

sphere:

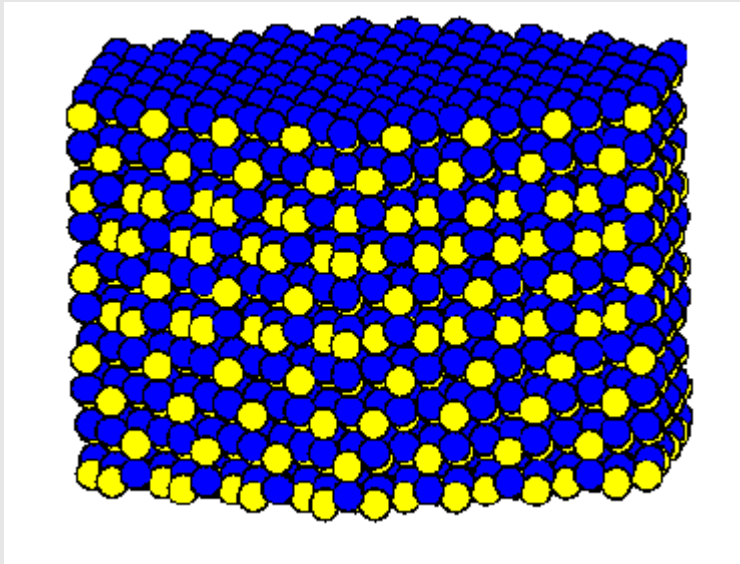
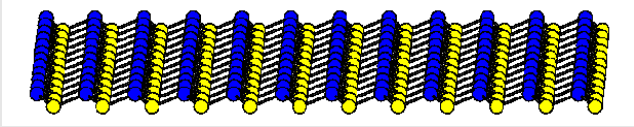
$$-4 \pi \rho_0 r * f_e(r,d) = -4 \pi \rho_0 r * [1 - 3/2 r/d + 1/2 (r/d)^3]$$

$r > d$:

no vectors in model:

$$G(r) = 0$$

creating ZnSe Nanoparticles



$\{110\}$ and $\{001\}$

create a large single Wurtzite layer A/B

Stack along c (with faults)

Cut to proper size

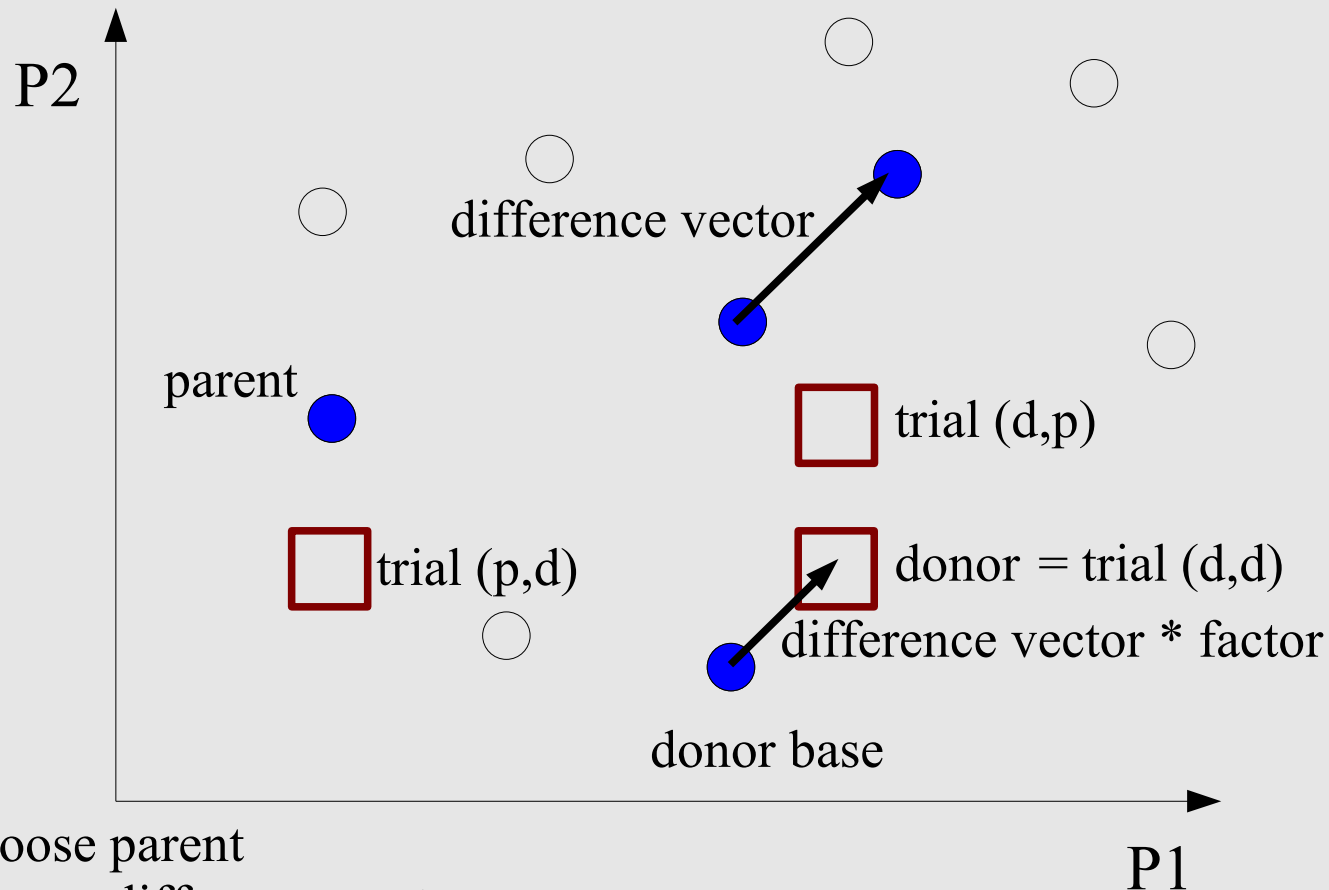
Calculate PDF / powder pattern

Repeat and average

Repeat with new set of parameter

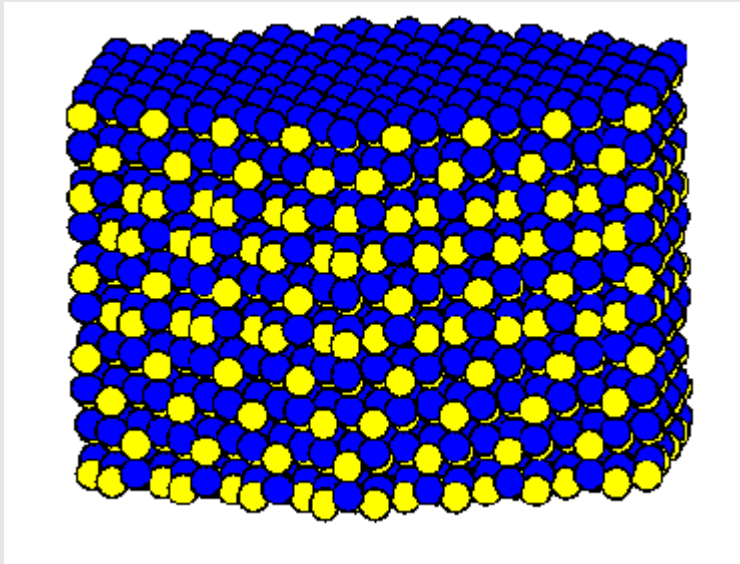
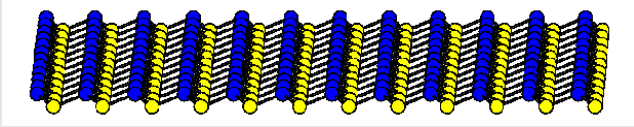
using a Differential Evolutionary Scheme

Differential Evolution



- choose parent
- choose difference vector
- add to donor base to get donor
- cross-over between parent and donor
- compute cost function, keep better of parent/trial

creating ZnO Nanoparticles



$\{110\}$ and $\{001\}$

create a large single Wurtzite layer A/B

Stack along c (**with faults**)

Cut to proper size

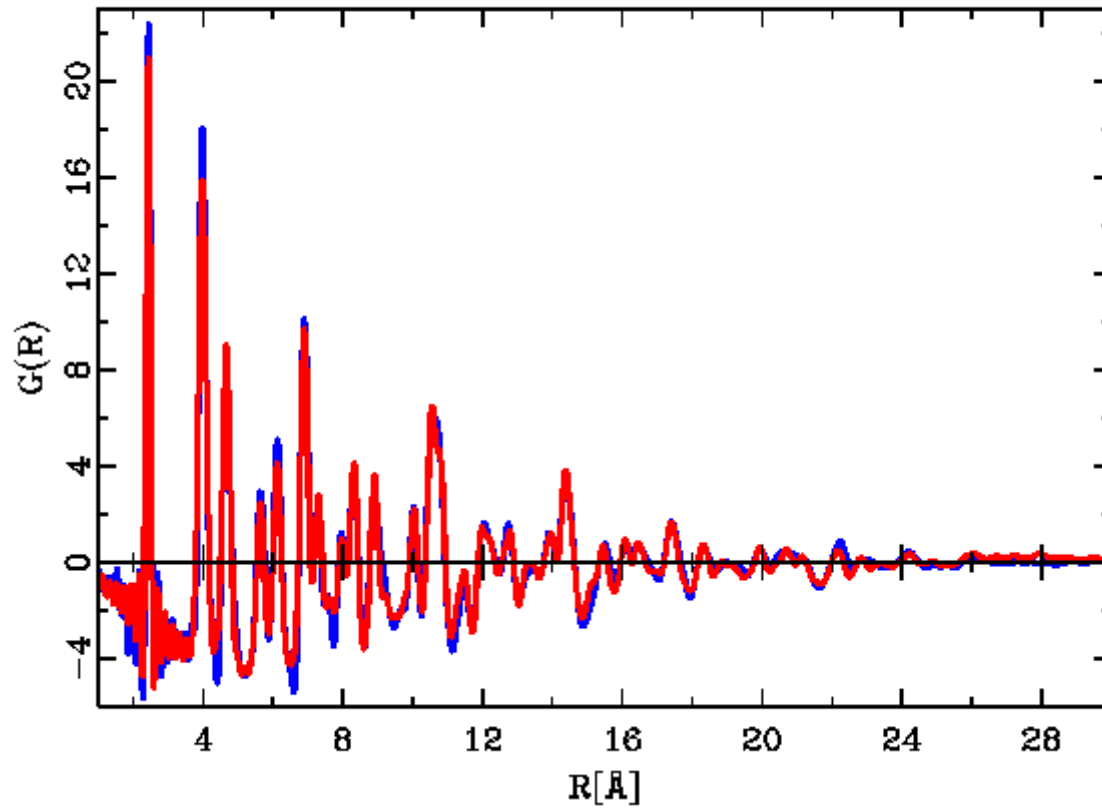
Calculate PDF / powder pattern

Repeat and average

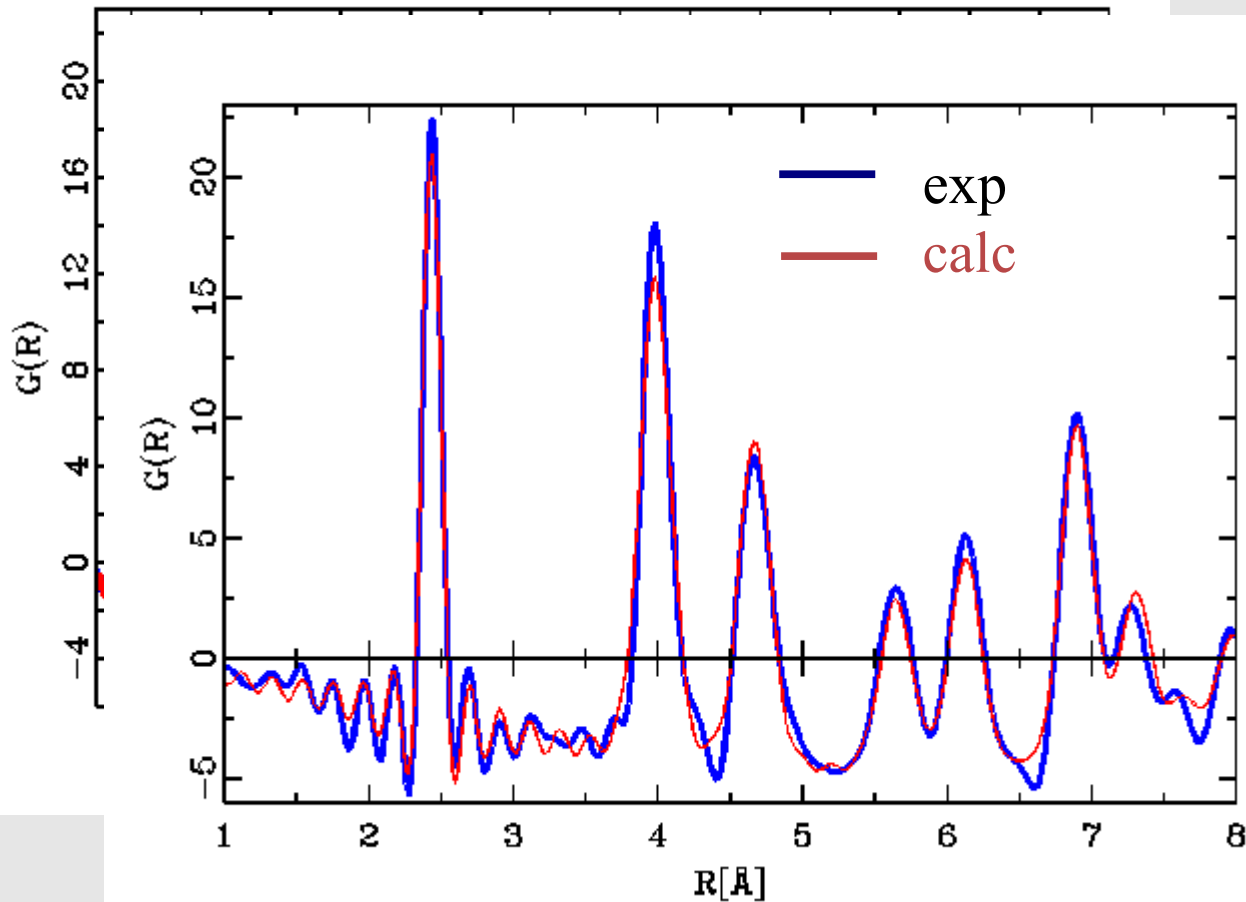
Repeat with new set of parameter

using a Differential Evolutionary Scheme

ZnSe Nanoparticles



ZnSe Nanoparticles



No distinction: prismatic vs spherical crystal

a 3.987 \AA
c 6.493 \AA

ideal tetrahedron
Zn-Se = 2.45(1) \AA

size a-b = 24(2) \AA
size c = 31(2) \AA

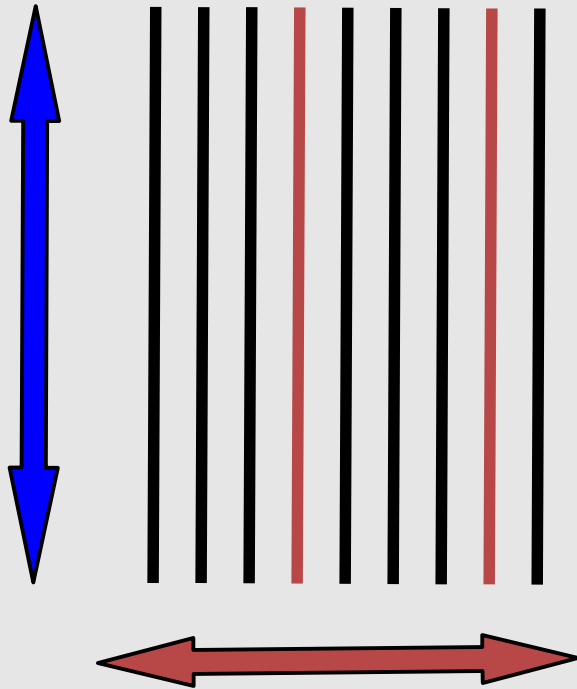
ratio $d_c/d_{ab} = 1.2$
elliptical shape

Stacking fault:
0.7

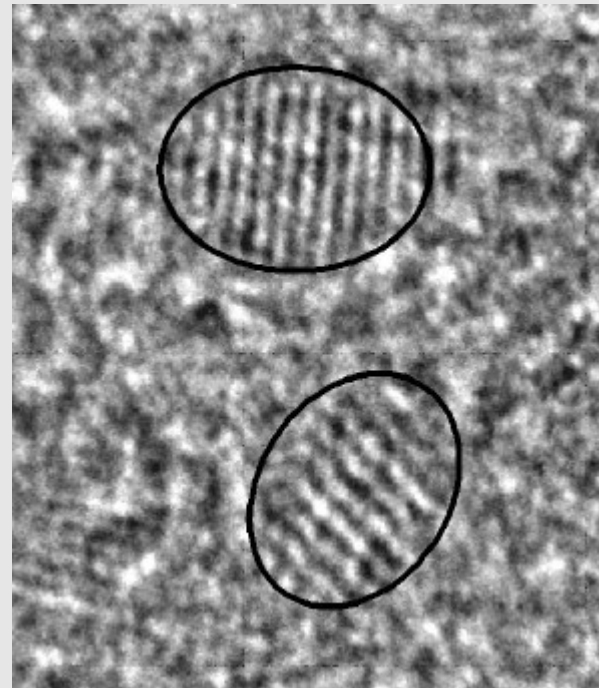
ZnSe Nanoparticles

~8 to 10 monolayers
= 4 to 5 unit cells along c
= 24 to 30 Å

structural coherence

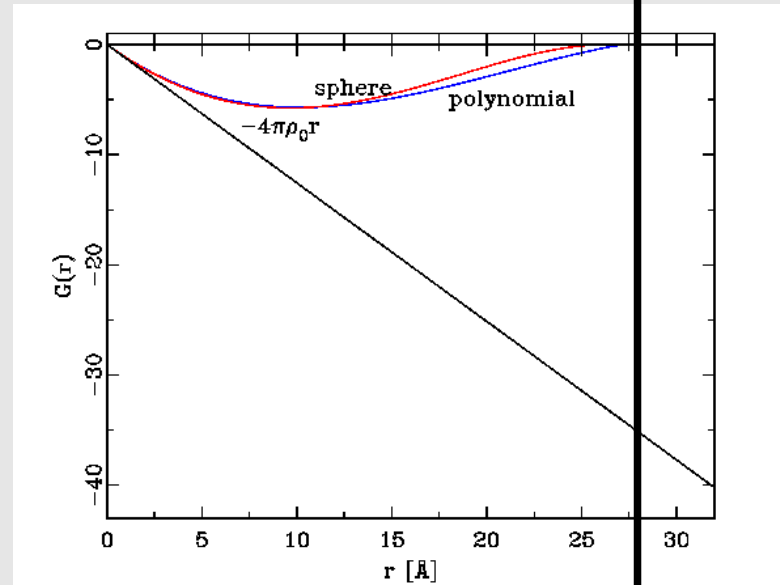
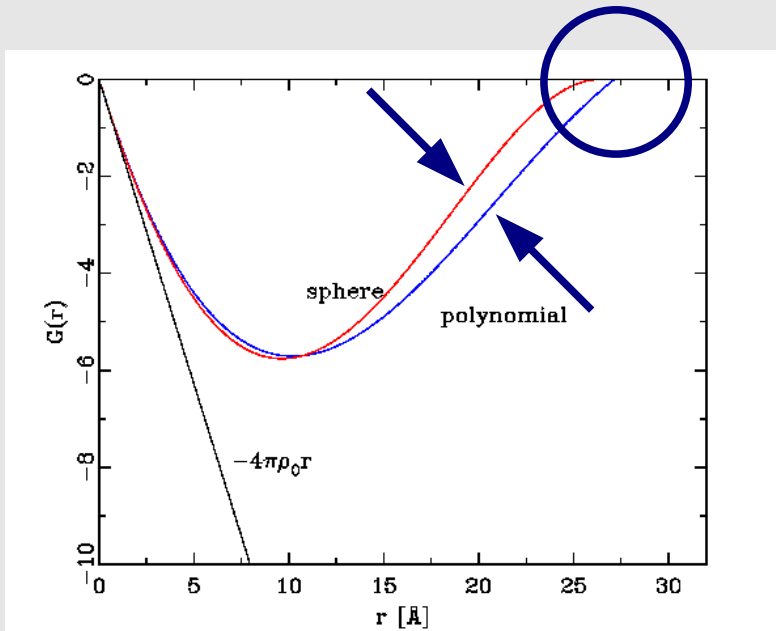


loss of coherence due
to stacking faults



PDF Simulation of Nanoparticles; finite particle

Simulation of a single finite sized ZnSe particle



$r < d$:

vectors in model:

$$G(r) = G(r)_{model} + \text{background contribution}$$

$$-4 \pi \rho_0 r + p_0 + p_1 r + p_2 r^2 + p_3 r^3$$

$r > d$:

no vectors in model:

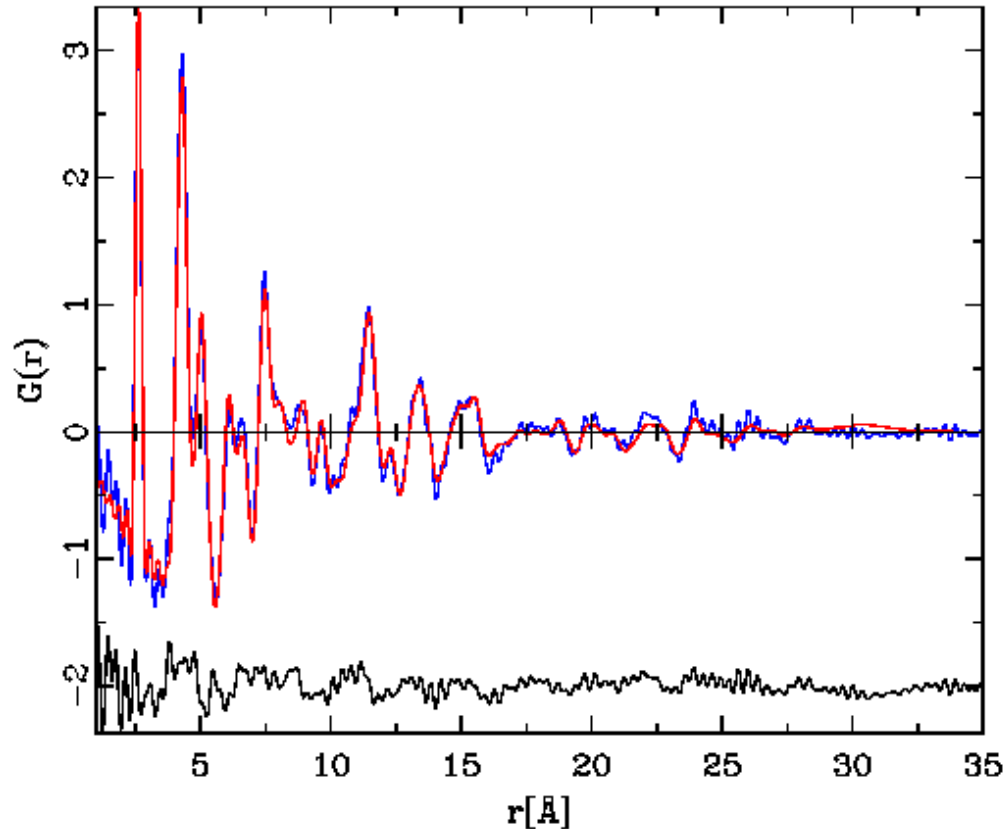
$$G(r) = 0$$

sphere:

$$-4 \pi \rho_0 r * f_e(r, \mathbf{d}) = -4 \pi \rho_0 r * [1 - 3/2 r/\mathbf{d} + 1/2 (r/\mathbf{d})^3]$$

$$\mathbf{d} = 1/3 (2*24 + 31) \text{ \AA}$$

CdSe Nanoparticles (Billinge)



$$\delta = 0.00028$$

$$\gamma = 0.08$$

$$Q_{\max} = 19 \text{ \AA}^{-1}$$

$$a = 4.303 \text{ \AA}$$

$$c = 6.997 \text{ \AA}$$

non ideal tetrahedron

$$z(\text{Zn}) = 0.382 \text{ \AA}$$

B iso = 2.3!

$$\text{size } a-b = 35(2) \text{ \AA}$$

$$\text{size } c = 32(2) \text{ \AA}$$

$$\text{ratio } d_c/d_{ab} = 0.9$$

almost spherical shape

Stacking fault:

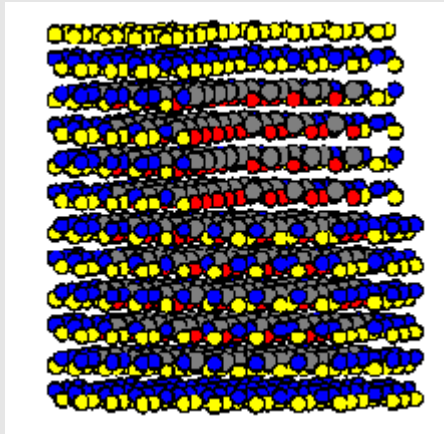
$$0.28$$

$$\text{density} = 0.024$$

$$\text{first peak width} = 0.56$$

$$\text{scale} = 0.85$$

CdSe/ZnS Core/Shell particles

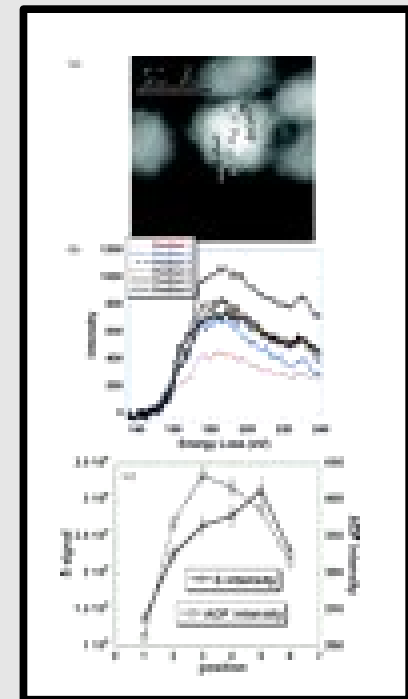
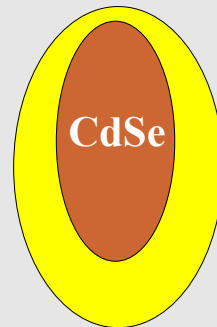


Core: CdSe ~ 3.2 nm \emptyset
Shell: ZnS ~ 1 layer
Stabilizer: TOPO

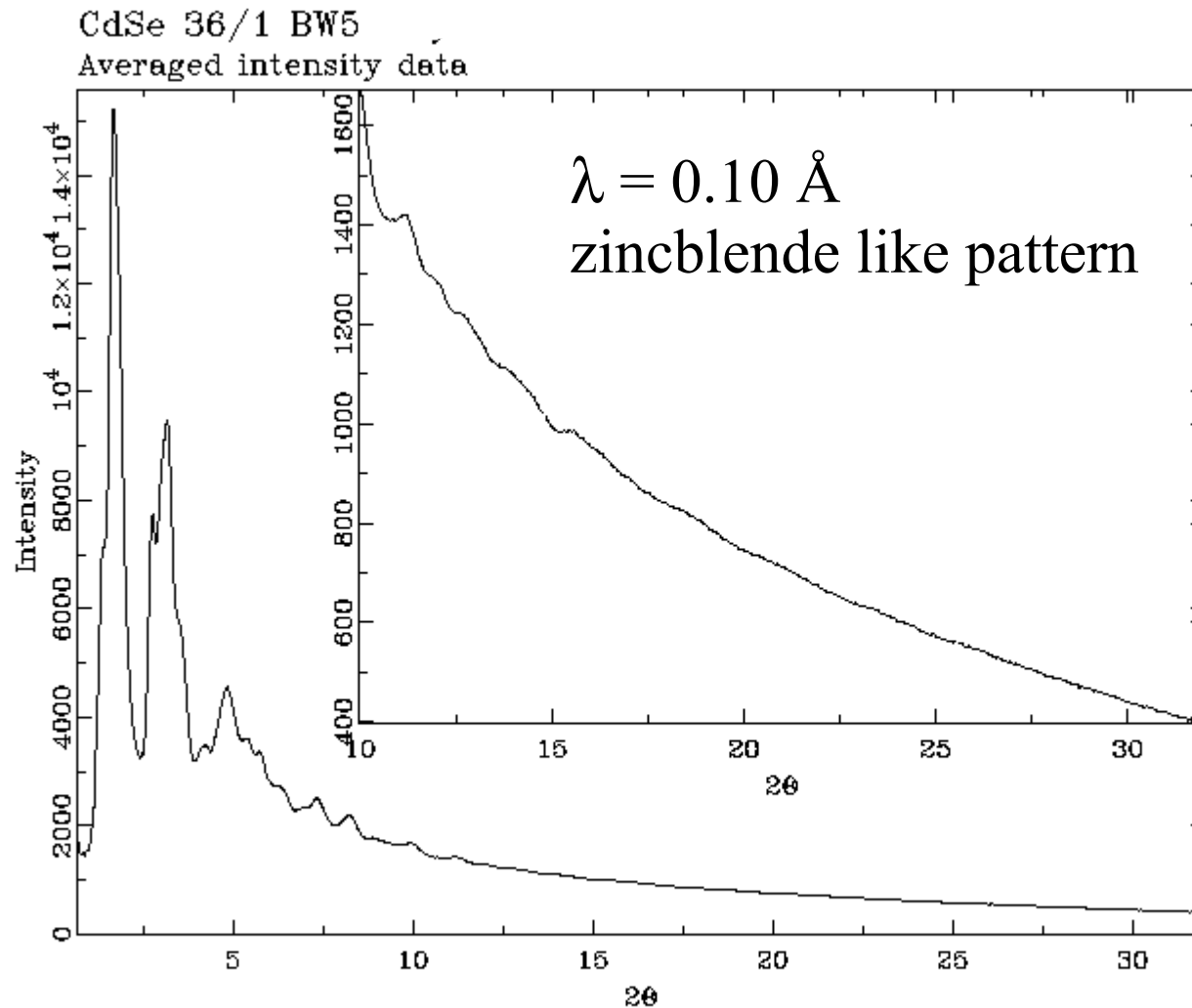
Band gap ZnS $>$ CdSe
efficient luminosity
quantum confinement

Structure of Core / Shell ?

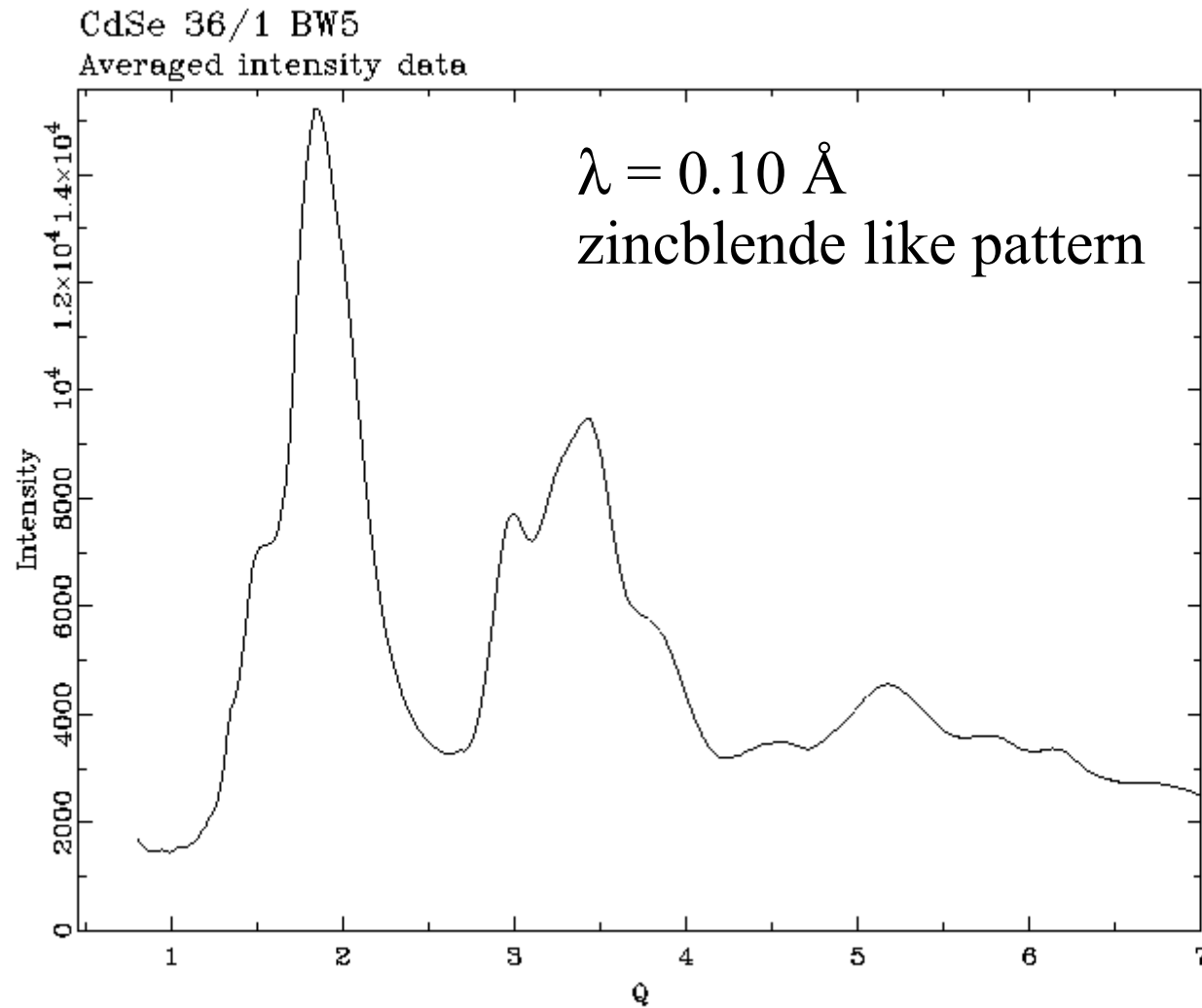
Epitaxial growth ? 11% lattice mismatch!



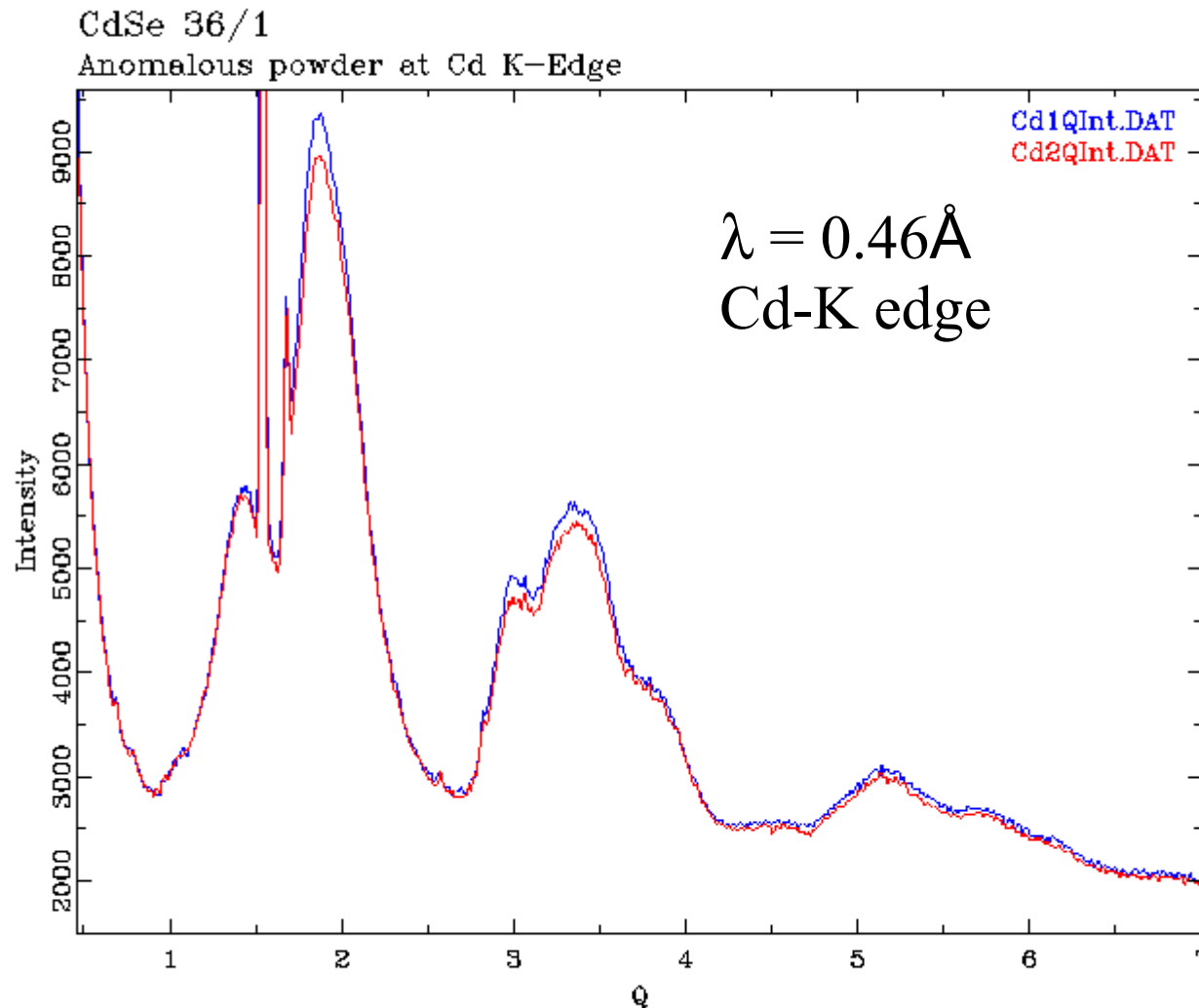
CdSe/ZnS Core/Shell particles



CdSe/ZnS Core/Shell particles

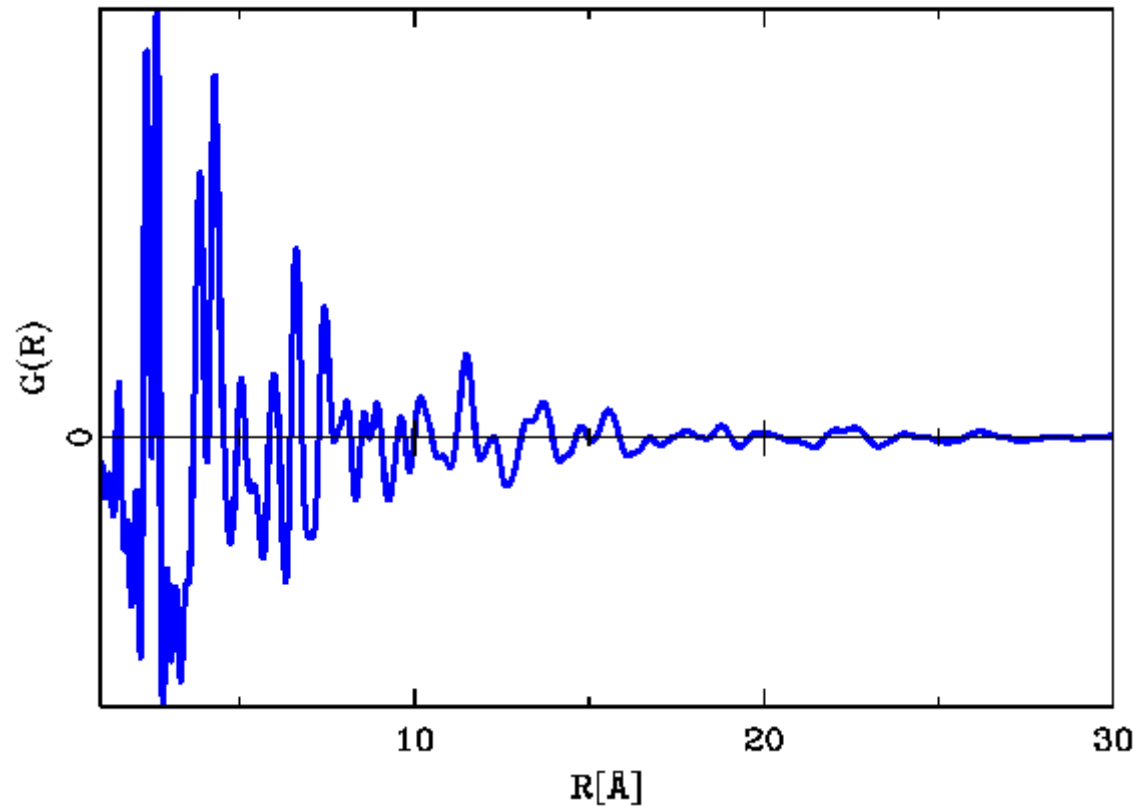


CdSe/ZnS Core/Shell particles

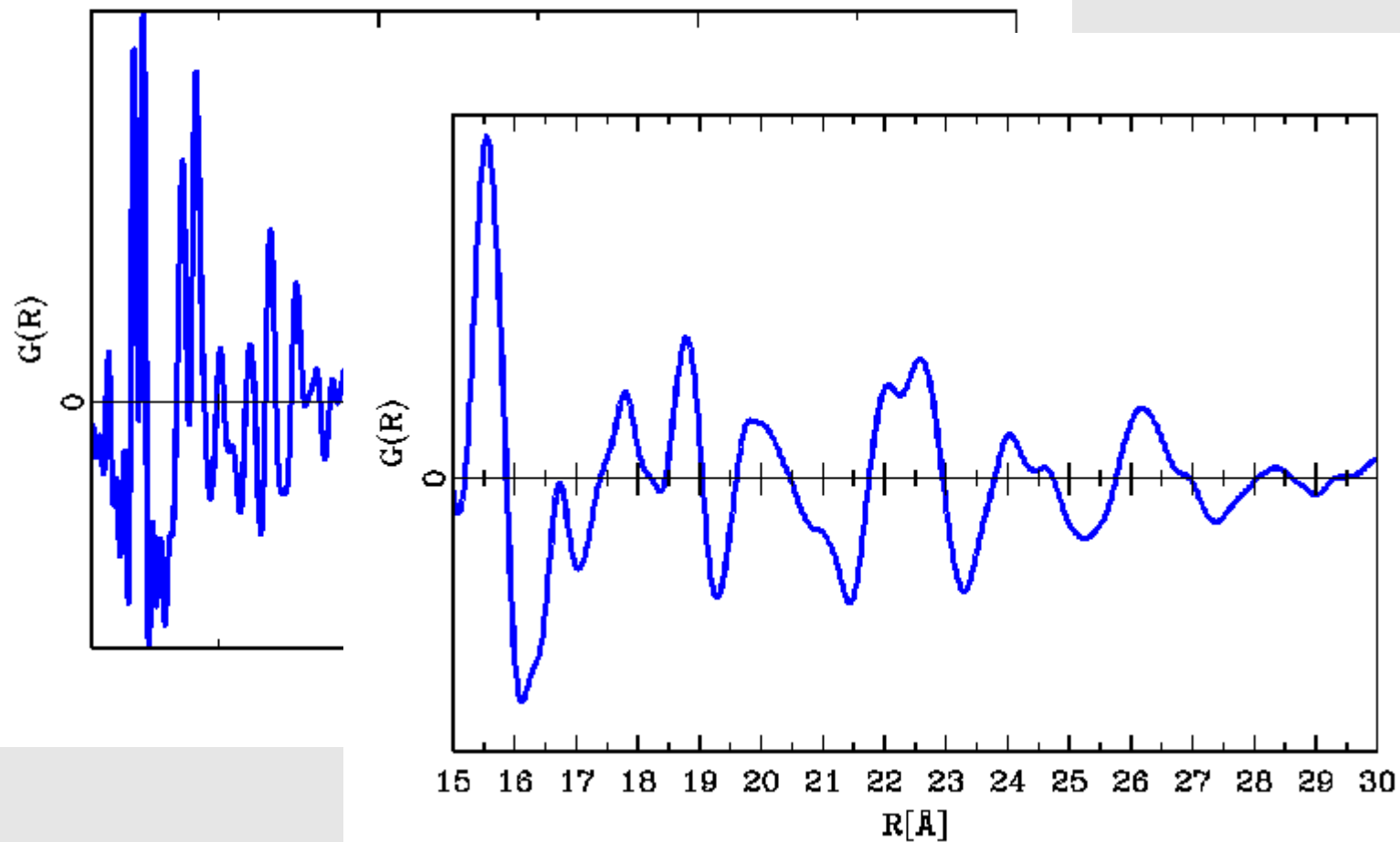


anomalous powder diffraction ==> chemically selective structure info

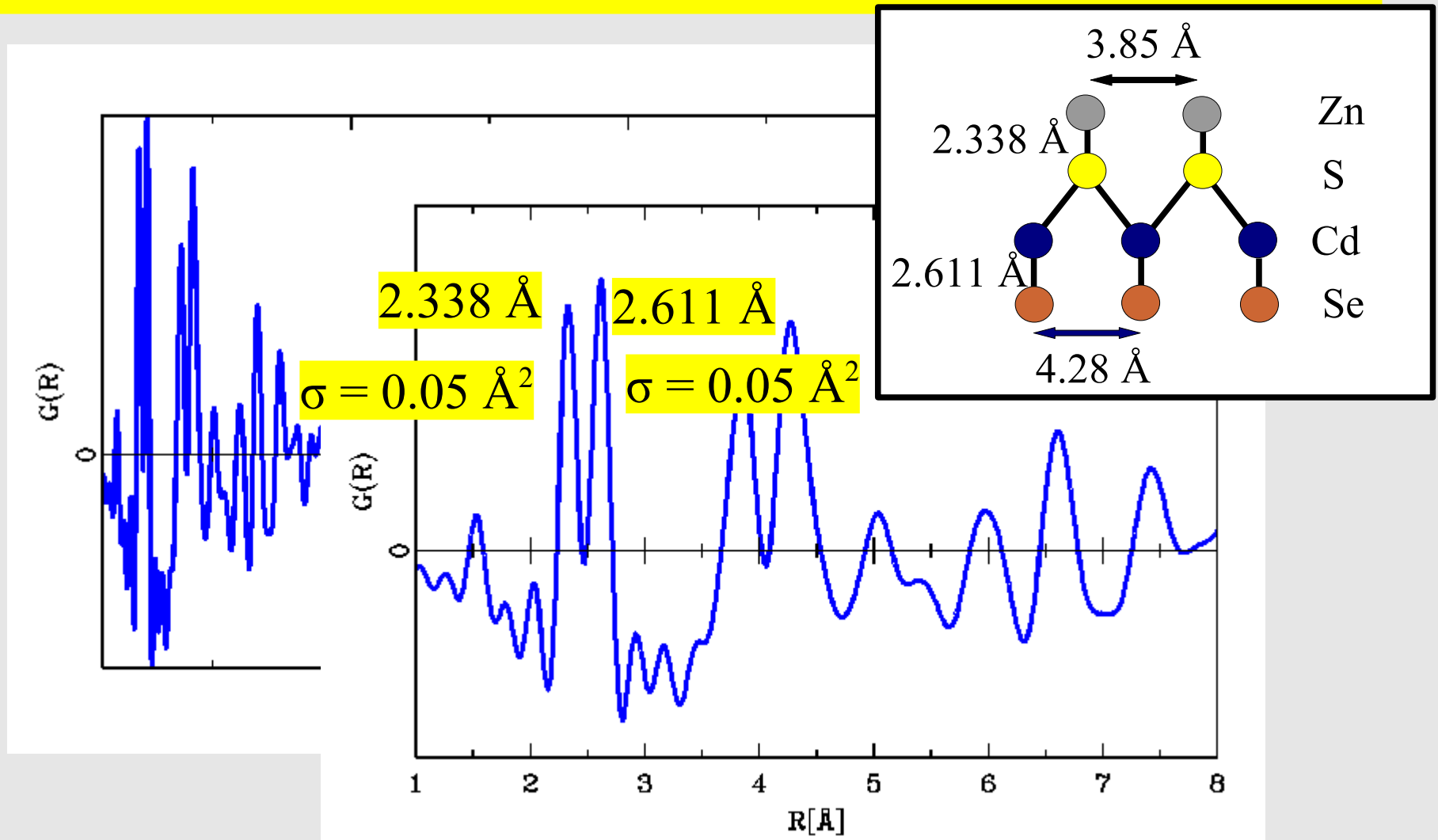
CdSe/ZnS experimental PDF



CdSe/ZnS experimental PDF



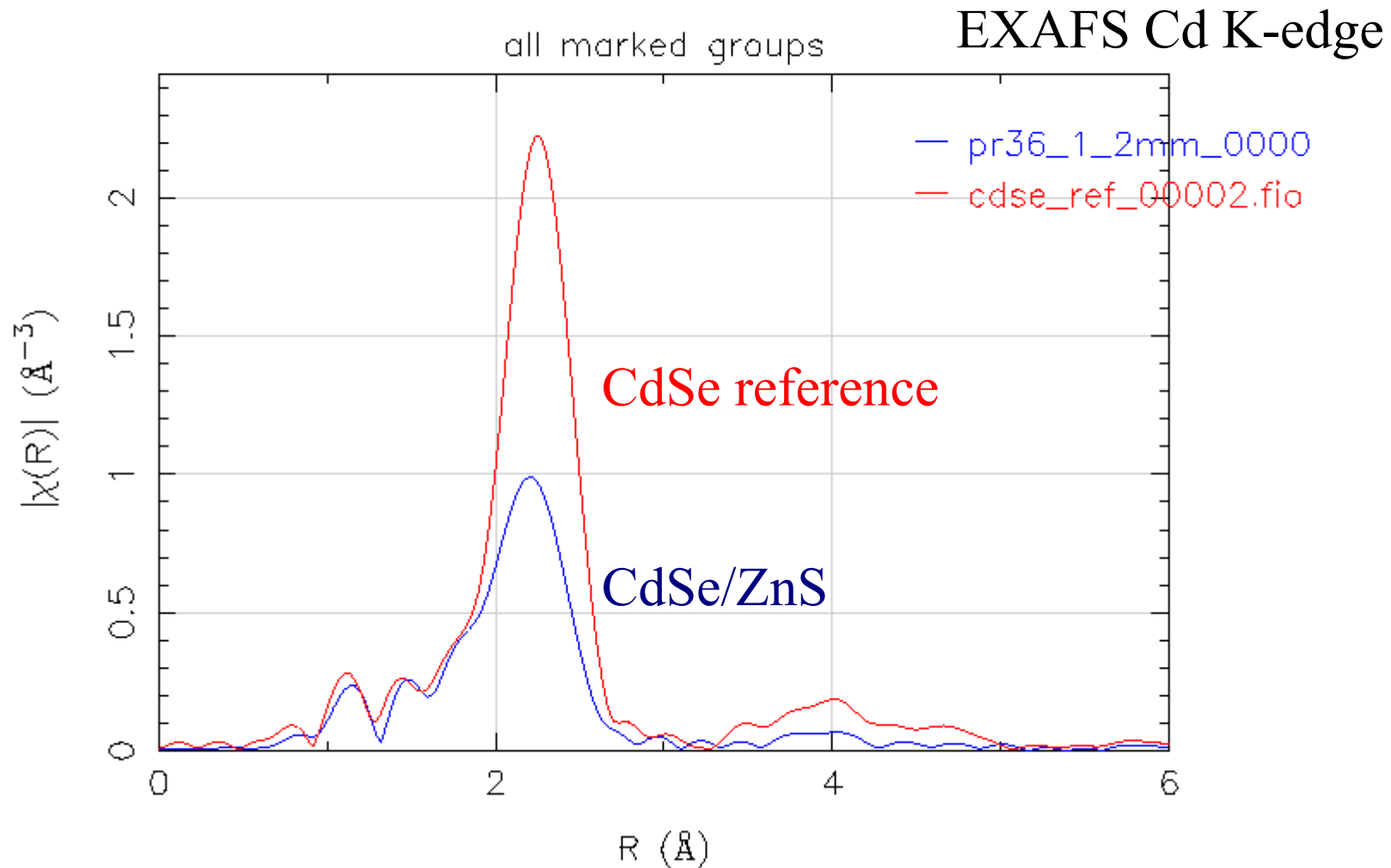
CdSe/ZnS experimental PDF



narrow symmetrical first peaks

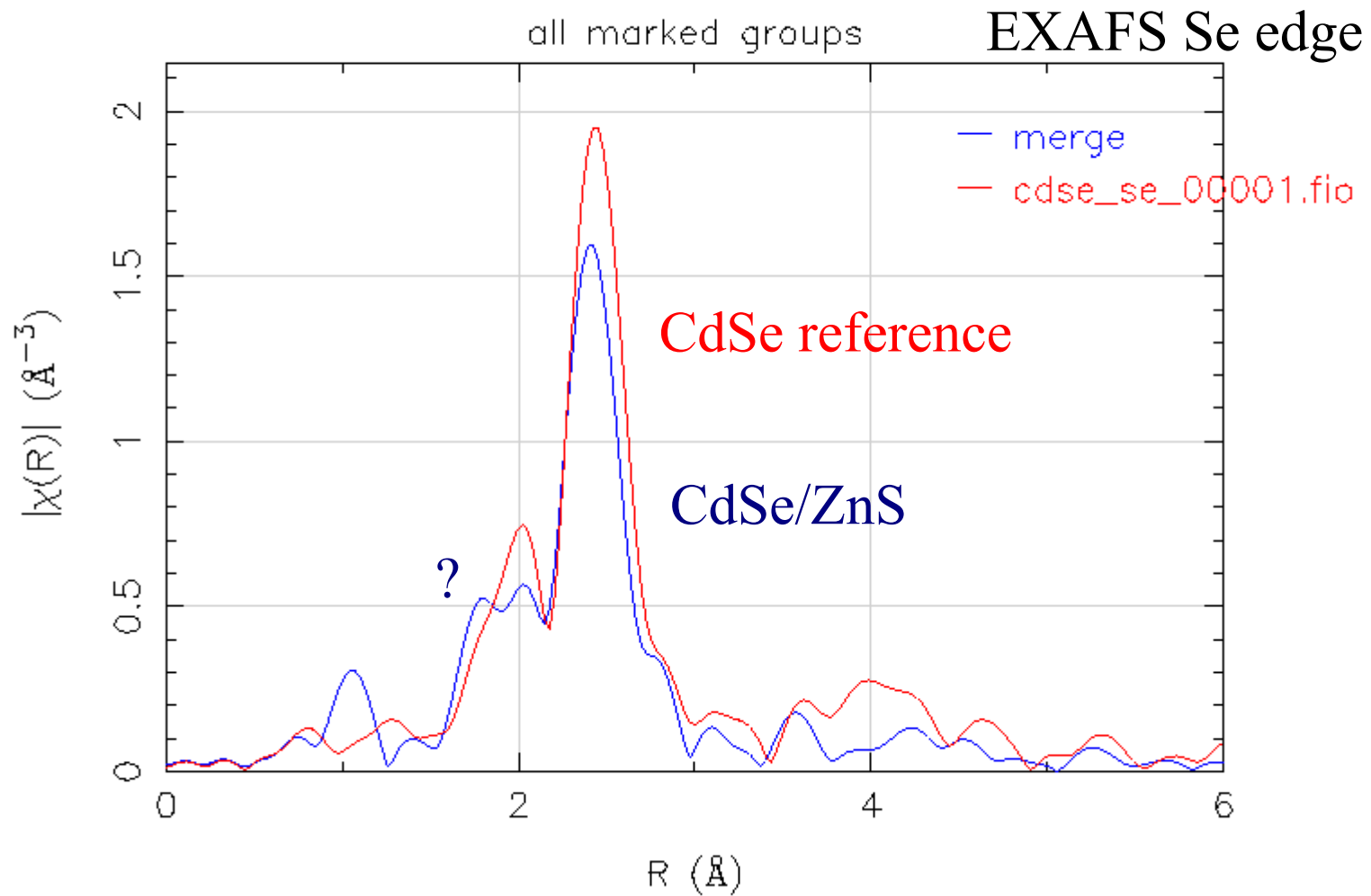
no indication of interaction

CdSe/ZnS Core/Shell particles

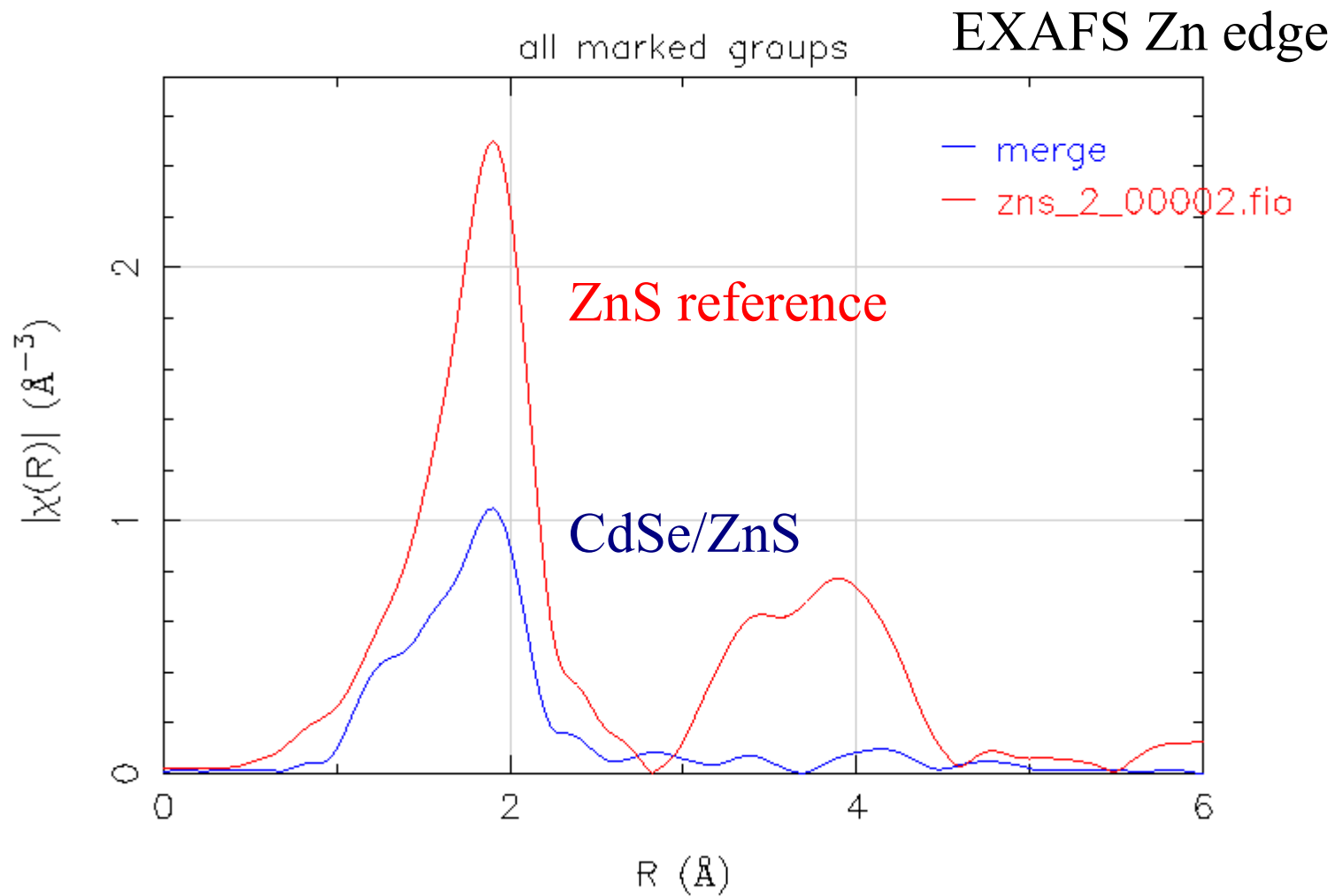


no significant differences CdSe core like crystalline structure

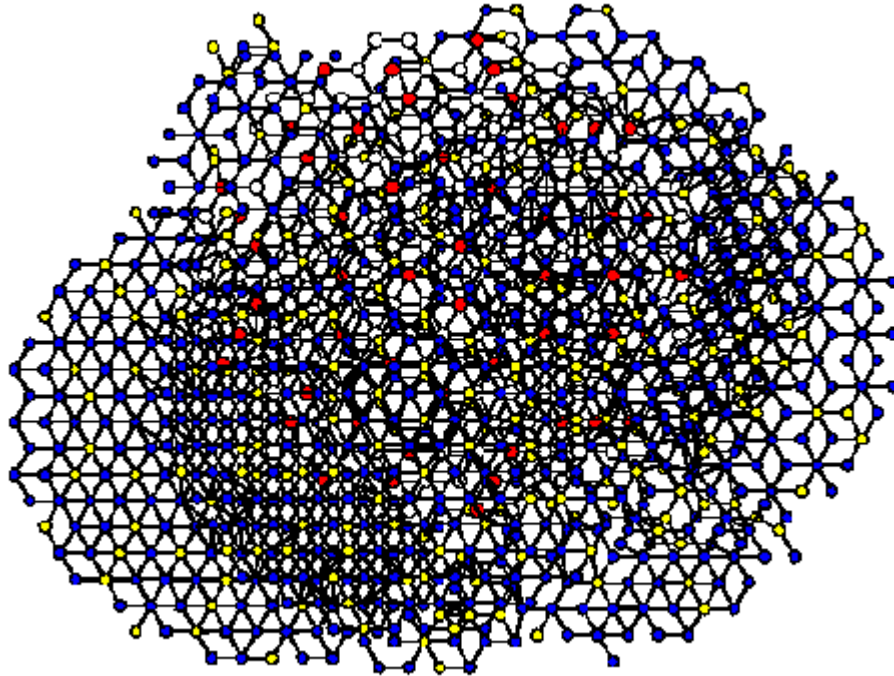
CdSe/ZnS Core/Shell particles



CdSe/ZnS Core/Shell particles



CdSe/ZnS Core/Shell particles



Elliptical CdSe core with stacking faults

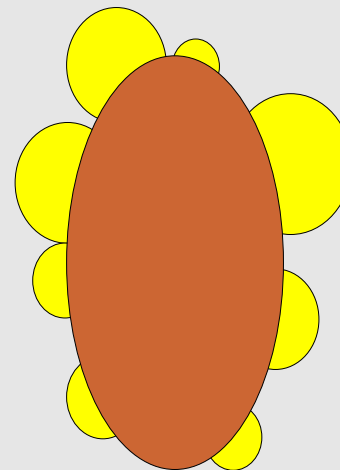
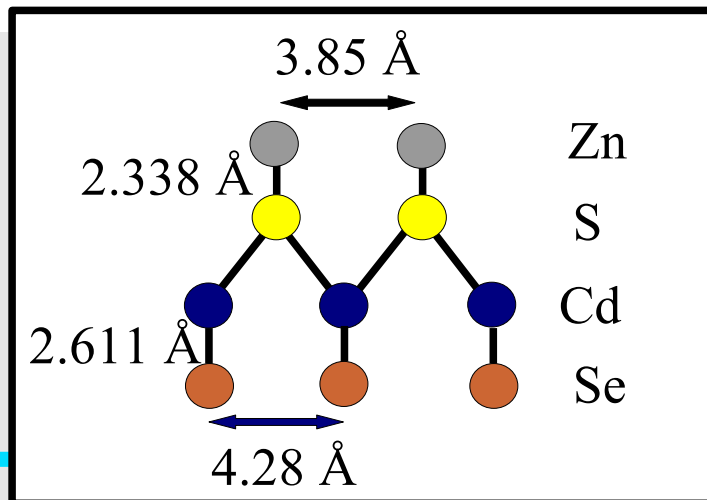
a, c, z, B
Ra, Rc, ρ

ZnS shell consisting of semi spherical subunits with stacking faults size distribution

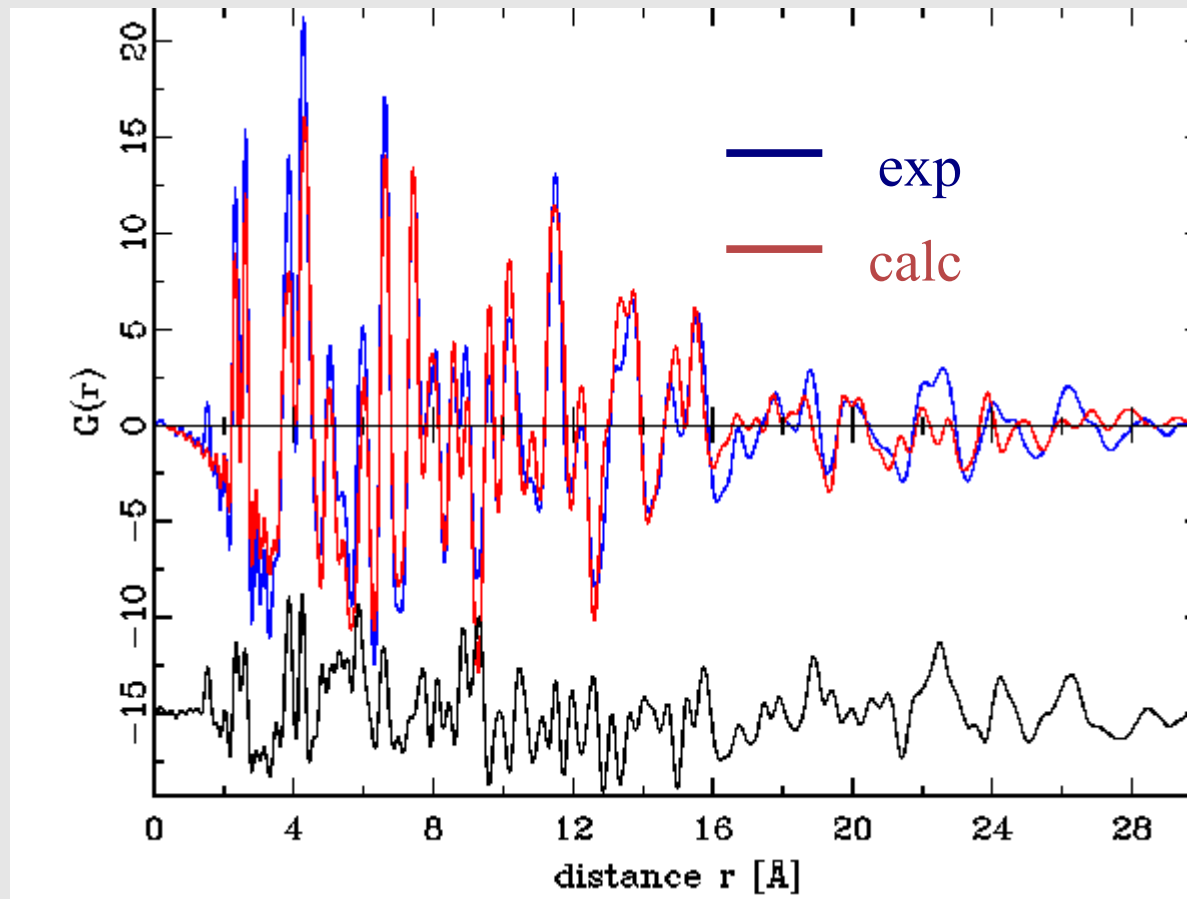
a, c, z, B
Ra, σR, ρ

Shell particles placed randomly at core surface, locally epitaxial

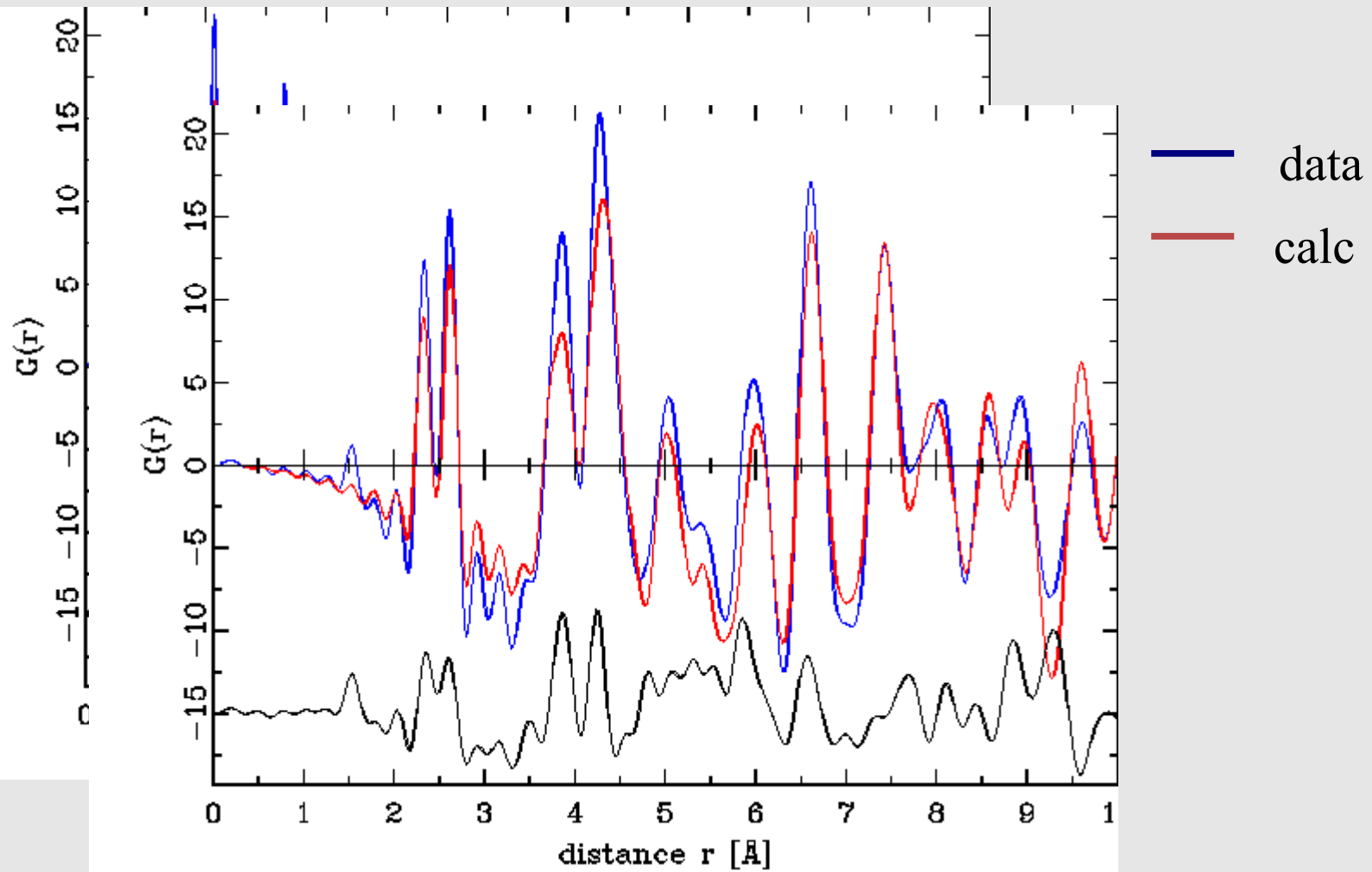
N



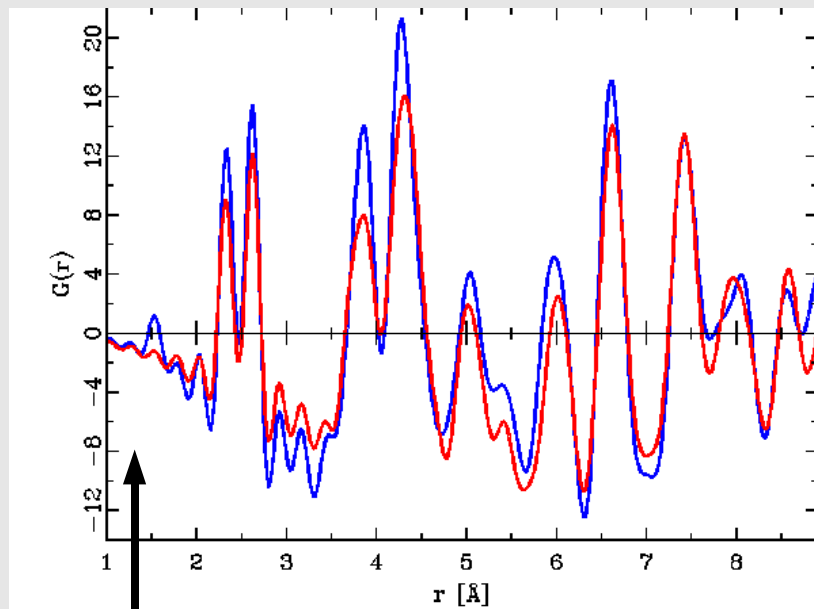
CdSe/ZnS Core/Shell particles



CdSe/ZnS Core/Shell particles



CdSe/ZnS Core/Shell particles



— data
— calc

Carbon – Carbon distances

lattice constants as in bulk
core and shell

high stacking fault probability

core more wurtzite like 35%

shell highly disorderd 50%

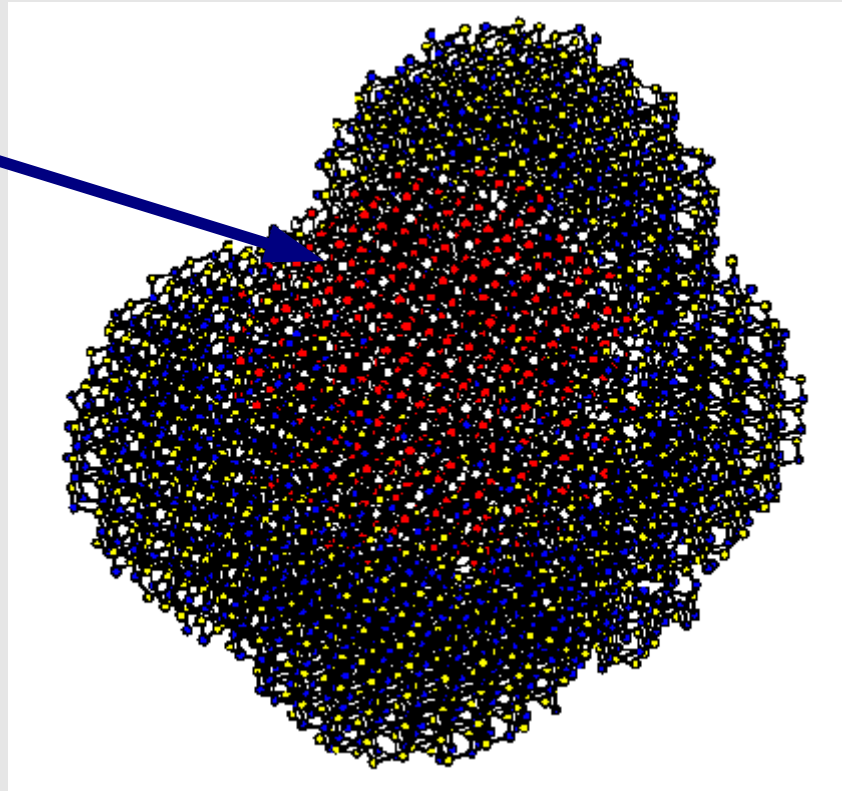
37 Å * 39 Å radius core

10 Å thickness shell

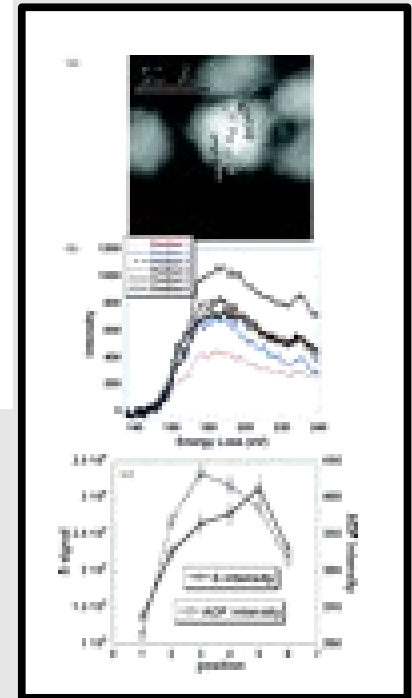
no noticeable interaction between
core and shell

CdSe/ZnS Core/Shell particles

parts of core surface
not covered



irregularly placed
shell particles
cover the core



stacking faults in II-VI nanoparticles

ZnO Wurtzite 18%

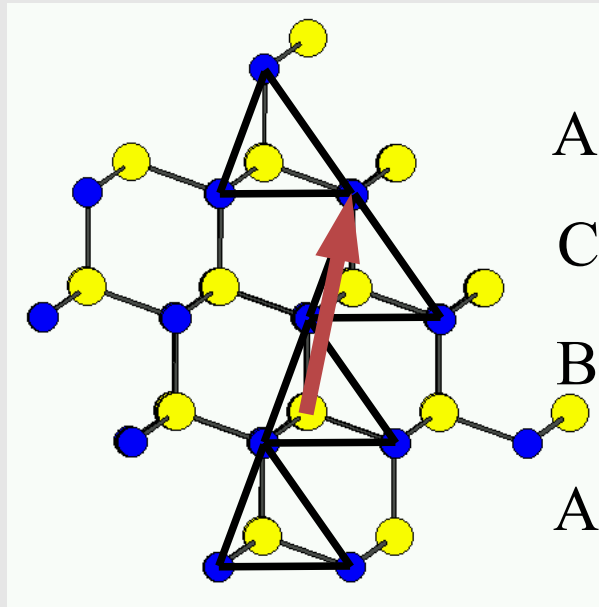
ZnSe Zinblende 30%

CdSe/ZnS core shell

core Wurtzite 35%

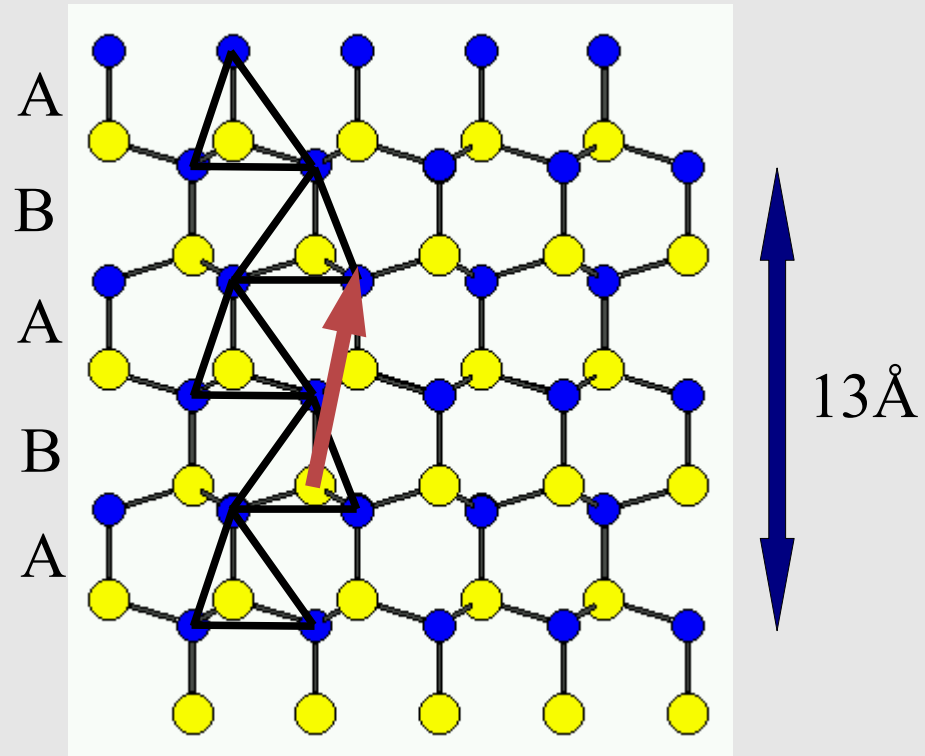
shell Zinblende 50%

Stacking Zincblende / Wurtzite



cubic closed packed
stacking of tetrahedra

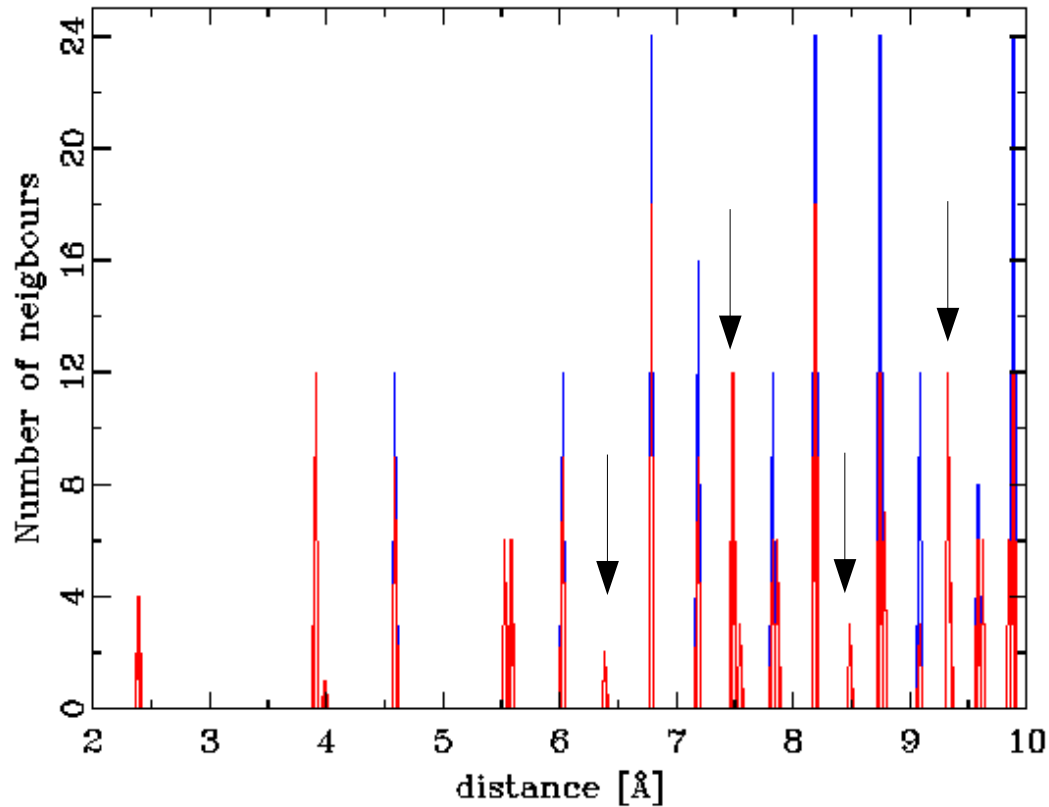
Zincblende



hexagonal close packed
stacking of tetrahedra

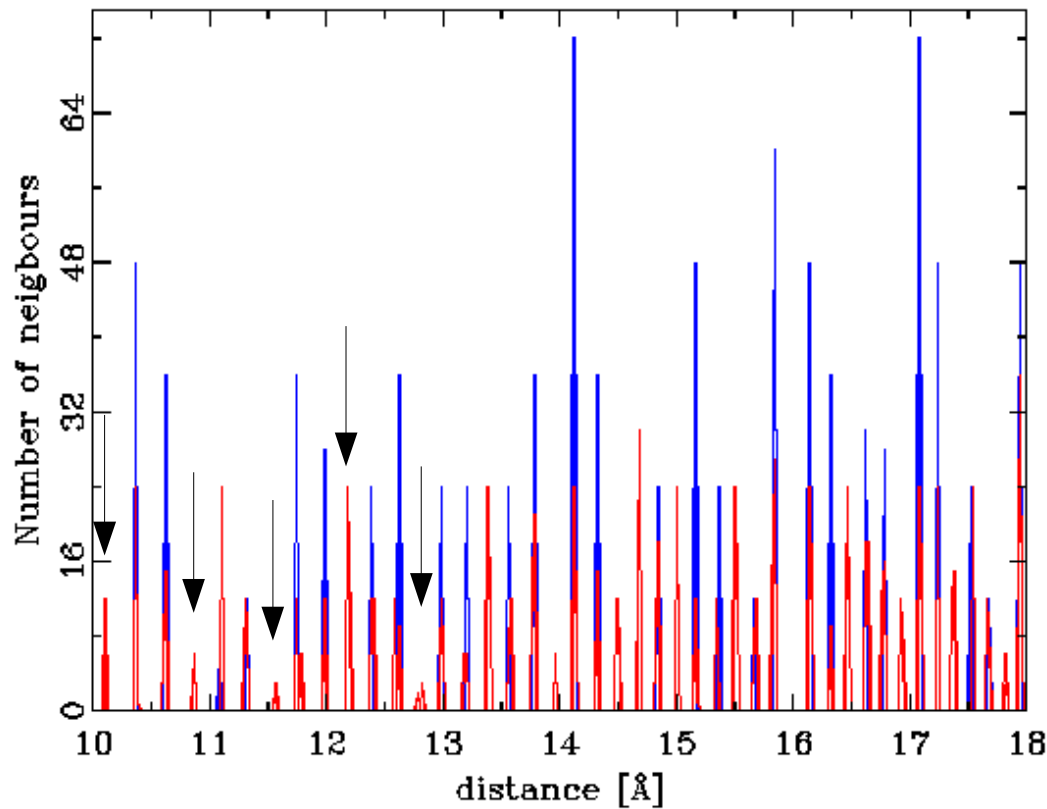
Wurtzite

Stacking Zincblende / Wurtzite



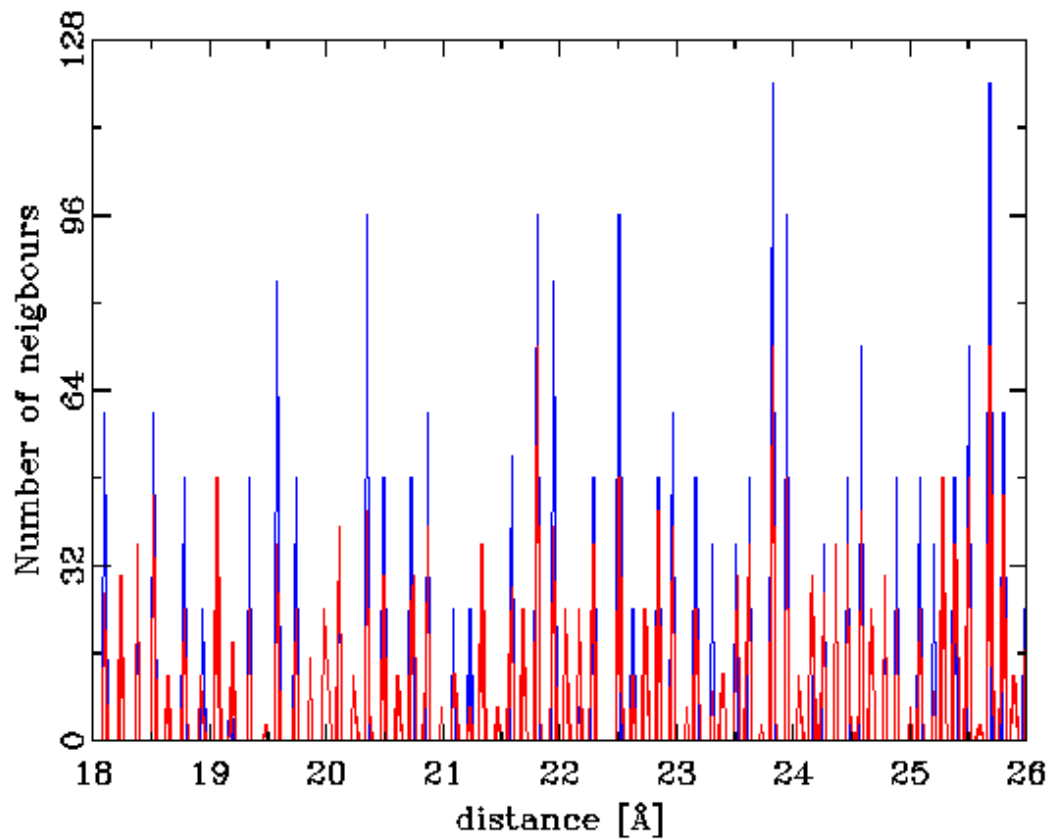
only minor differences in bond lengths

Stacking Zincblende / Wurtzite



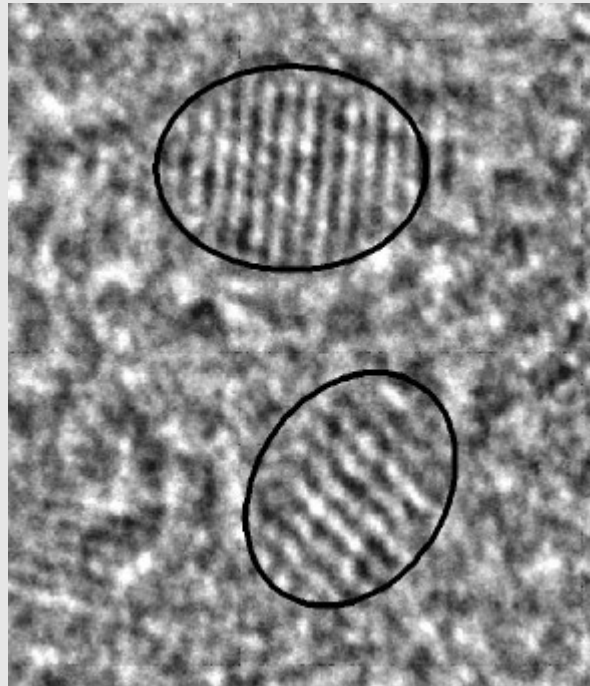
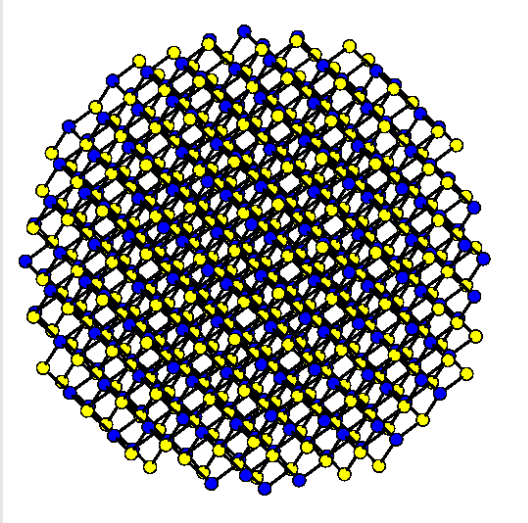
only minor differences in bond lengths
additional different distances in Wurtzite
all Zincblende distances also in Wurtzite!

Stacking Zincblende / Wurtzite



only minor differences in bond lengths
additional different distances in Wurtzite
all Zincblende distances also in Wurtzite!

Stacking Zincblende / Wurtzite



~8 to 10 monolayers
= 4 to 5 unit cells along c
= 24 to 30 Å

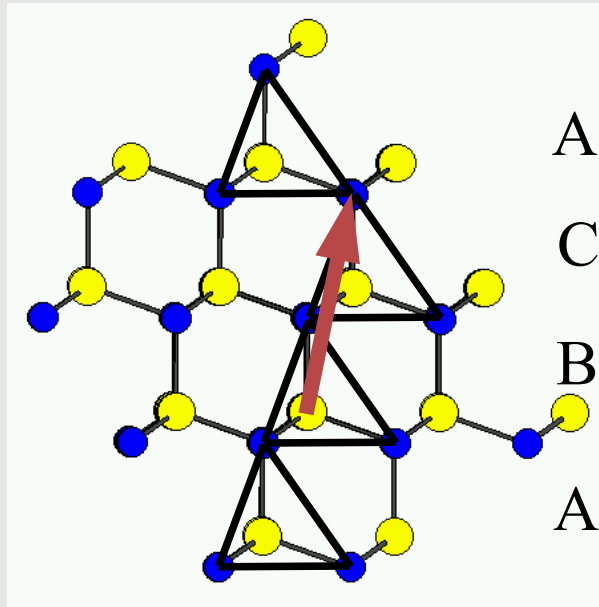
spherical II-VI nanoparticle

30 Å diameter \Rightarrow 660 atoms

25 Å diameter \Rightarrow 380 atoms

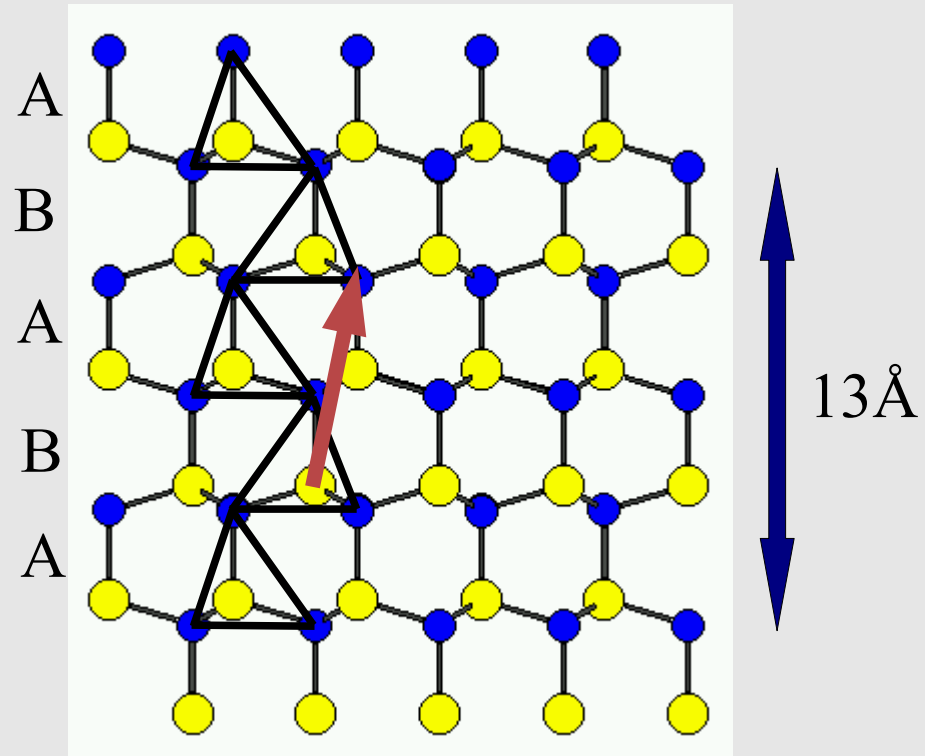
layered structure layers identical in Wurtzite and Zincblende

Stacking Zincblende / Wurtzite



cubic closed packed
stacking of tetrahedra

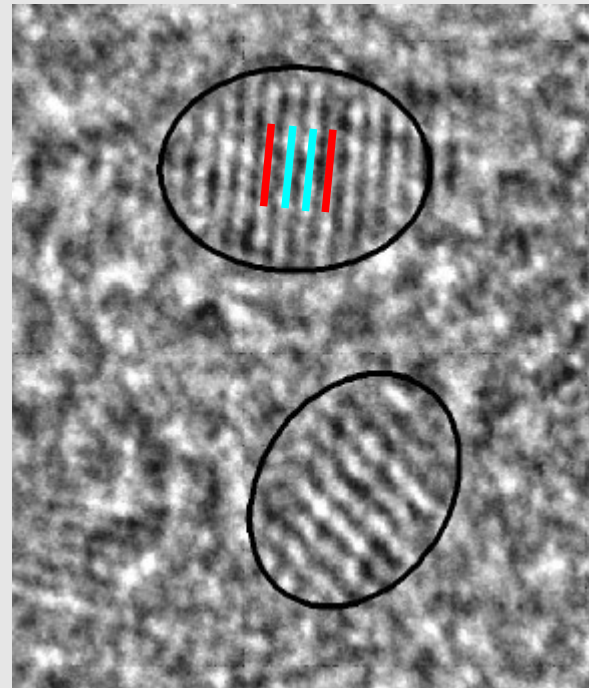
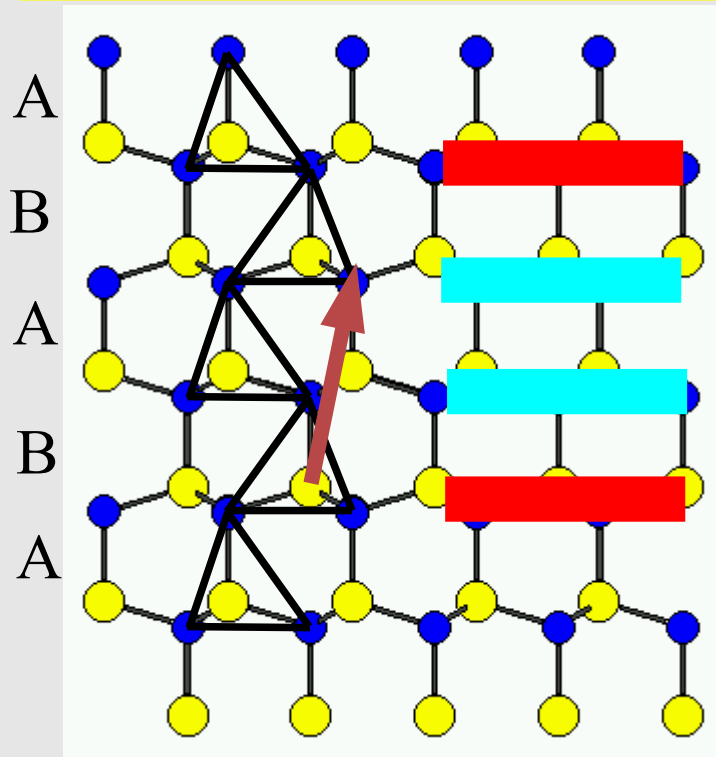
Zincblende



hexagonal close packed
stacking of tetrahedra

Wurtzite

Common building principles



~ 40 atoms

~ 100 atoms

Common structural characteristics:

layered structure layers identical in Wurtzite and Zincblende

⇒ high stacking fault probability

30% probability \cong 3 to 4 faults

No relaxation of first neighbour distances

Relaxation of second neighbour distance

Acknowledgements

V.I. Korsunskiy

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A. Hofmann

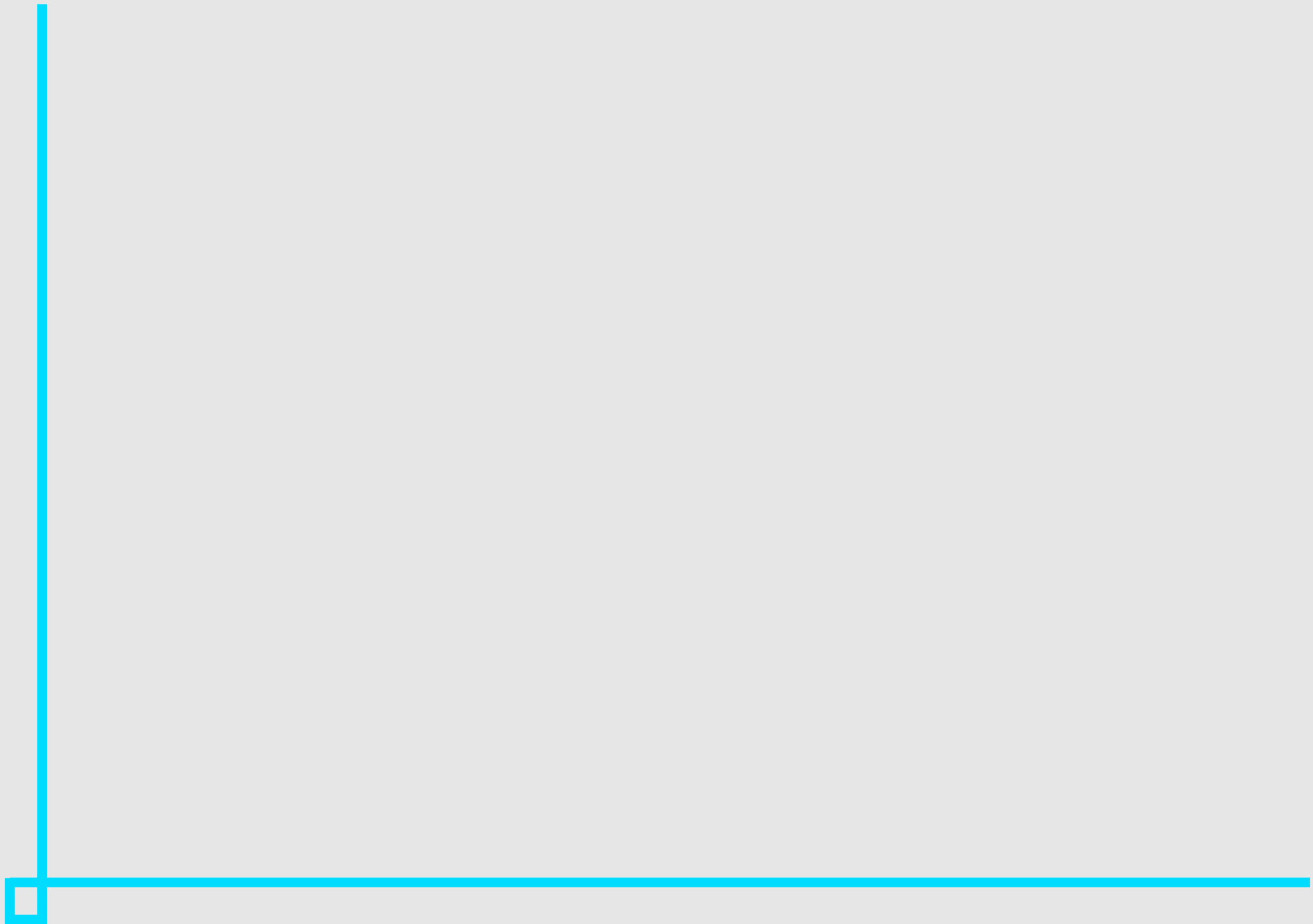
S. Dembski

C. Graf

C. Rühl

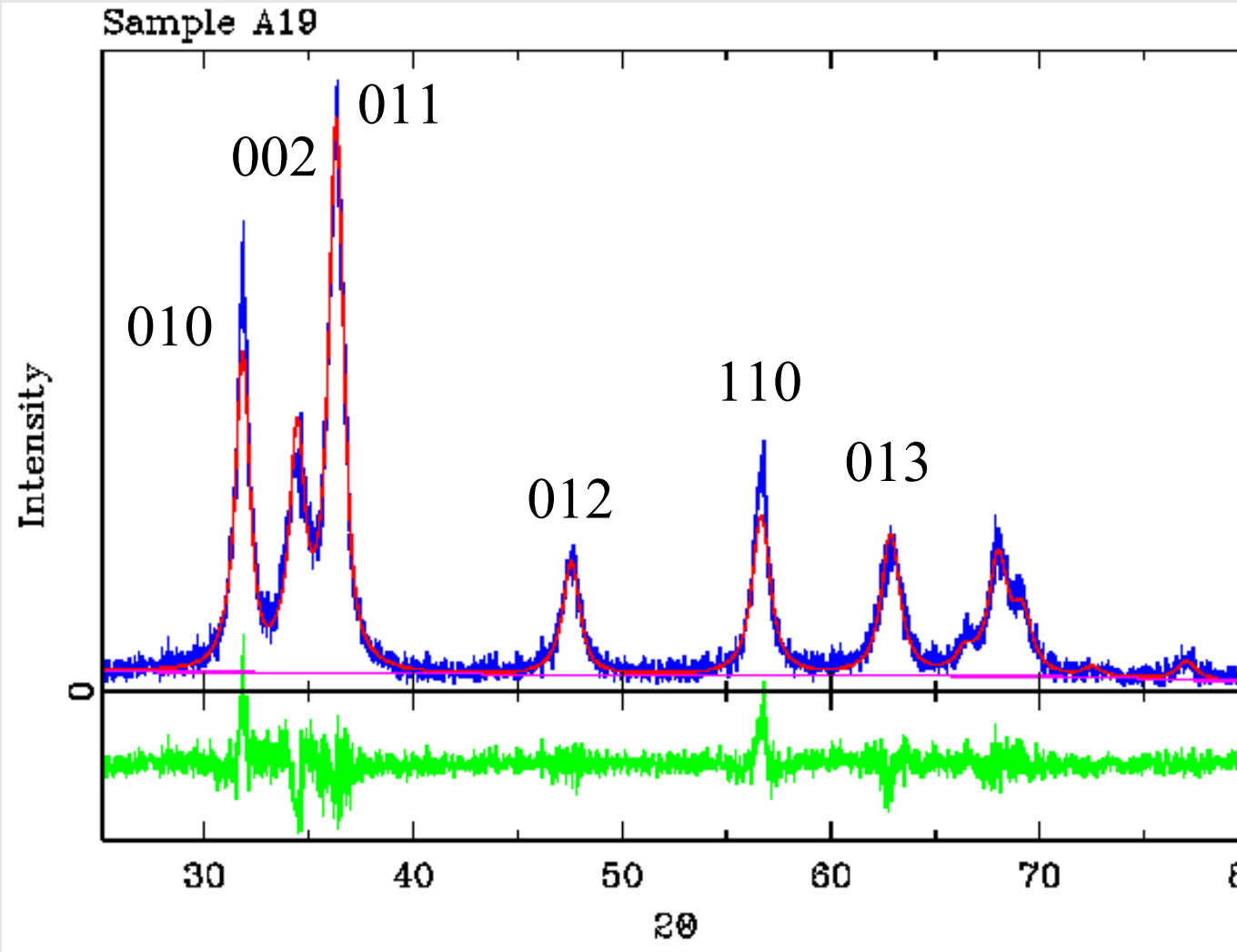
German Science Foundation

SFB410 II-VI Semiconductors



ZnO Nanoparticles

Rietveld refinement



Wurtzite

R_{wp} 18 %

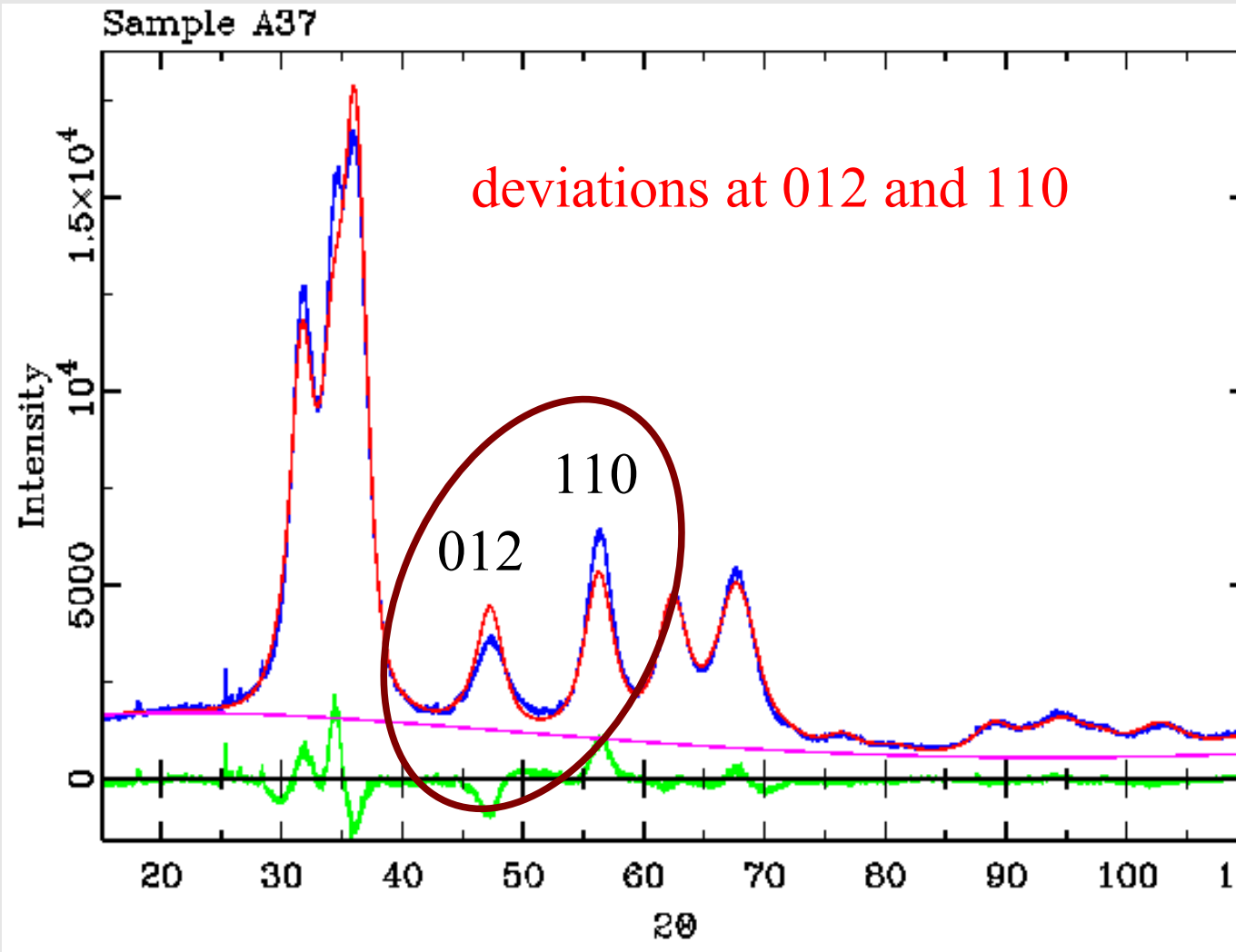
FWHM 60 = 1.0

size 9.5 nm

anisotropic
line widths

ZnO Nanoparticles

Rietveld refinement



Wurtzite

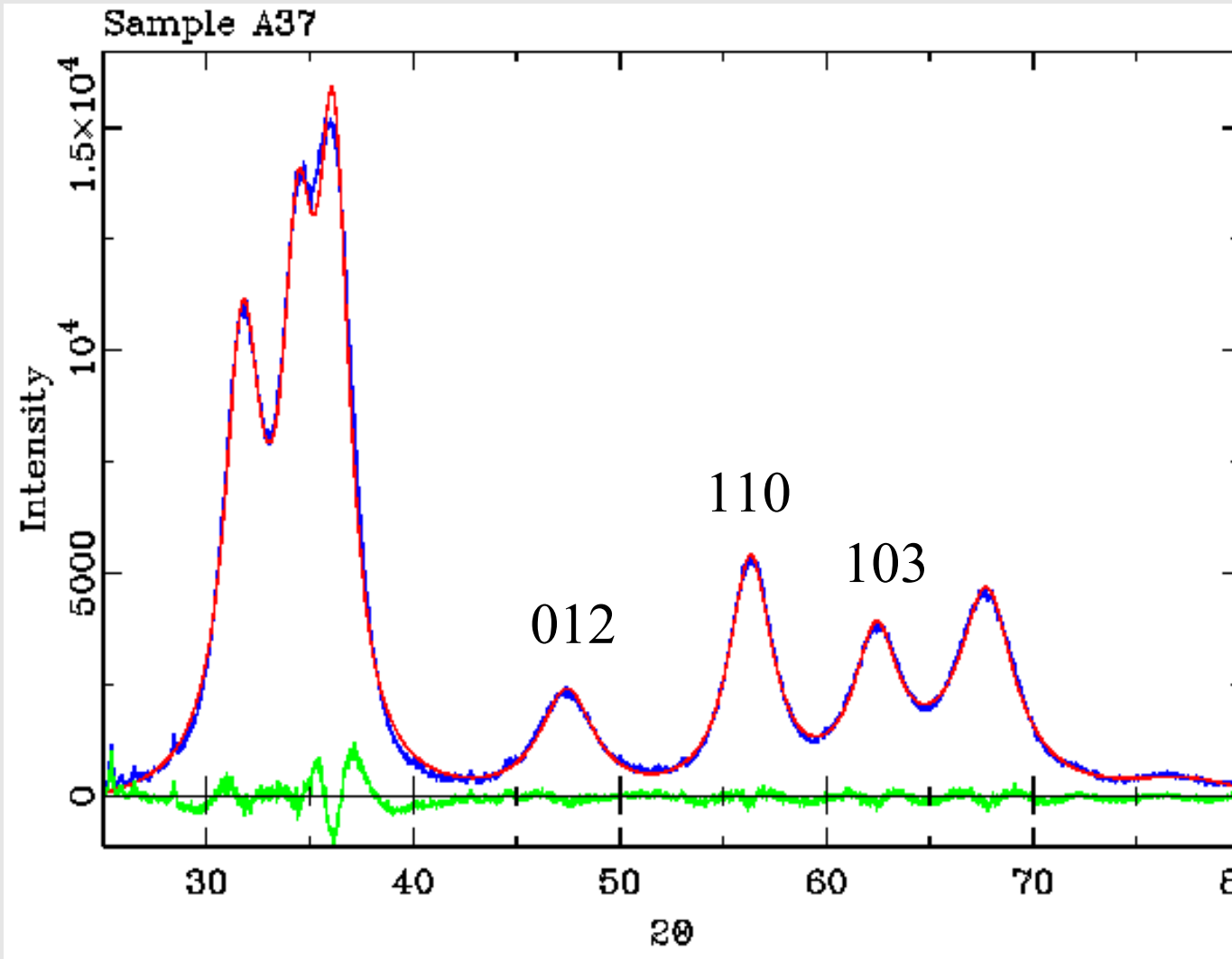
R_{wp} 7 %

FWHM 60 = 3.0

size 3.2 nm

texture
anisotropic shape
stacking faults

ZnO Nanoparticles



Single line fit

hkl FWHM Size

110 2.72 3.45

103 2.68 3.60

012 3.75 2.42

texture

anisotropic shape

stacking faults

ZnO Nanoparticles Fitting by Debye

Debye formula :

$$\langle |F(\mathbf{h})|^2 \rangle = \sum_j f_j^2 + \sum_i \sum_{j,j \neq i} f_i f_j \sin(2\pi \mathbf{h} \cdot \mathbf{r}_{ij}) / (2\pi \mathbf{h} \cdot \mathbf{r}_{ij})$$

Sum over all atom pairs

→ no restrictions on sample structure

open to finite particle with any shape
defects like stacking faults etc.

ZnO Nanoparticles Fitting by Debye

Debye formula

ZnO Wurtzite Structure

a

c

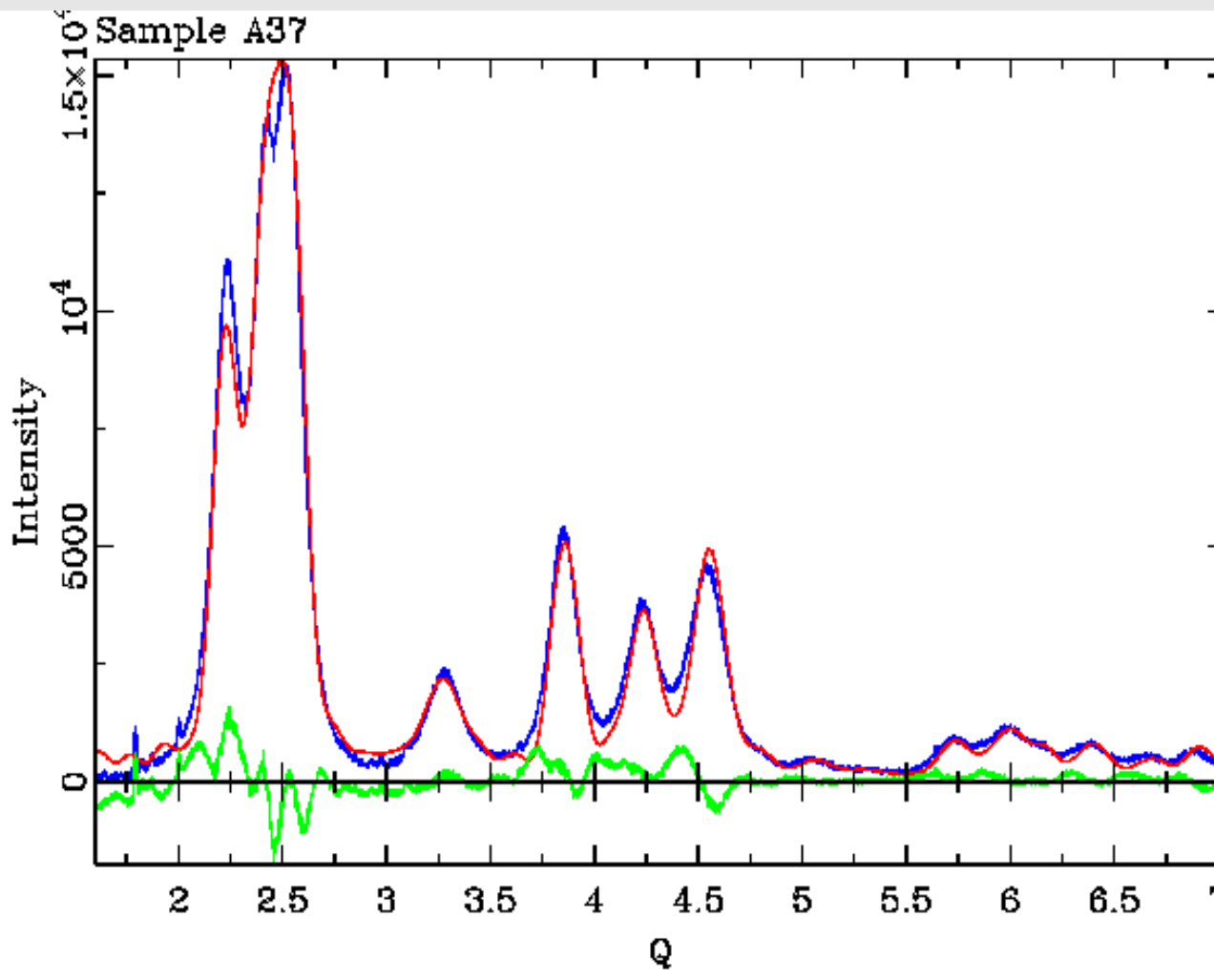
overall U

size in a-b plane

size along c

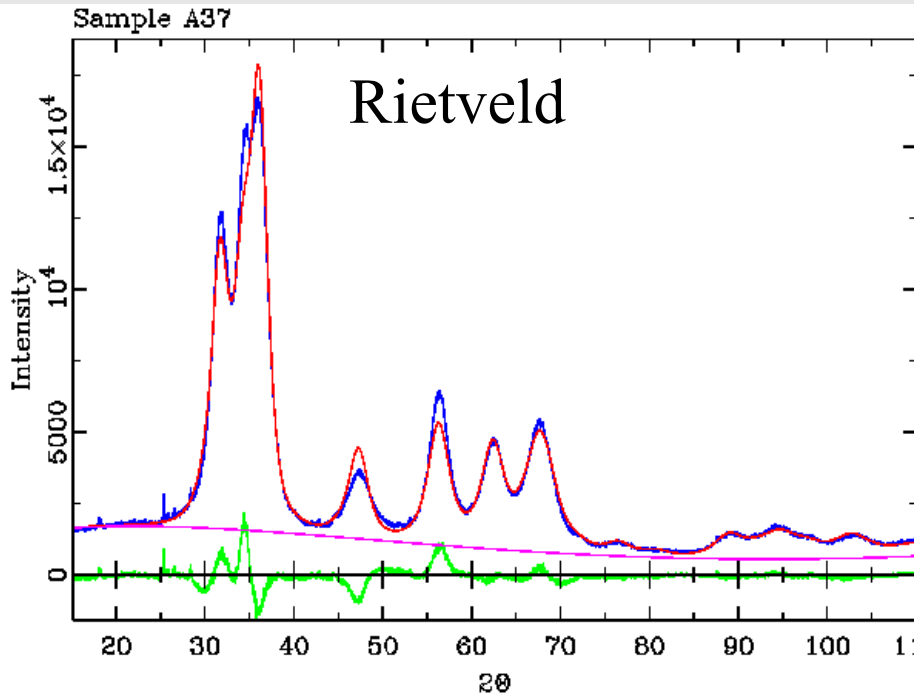
z(oxygen)

Stacking probability



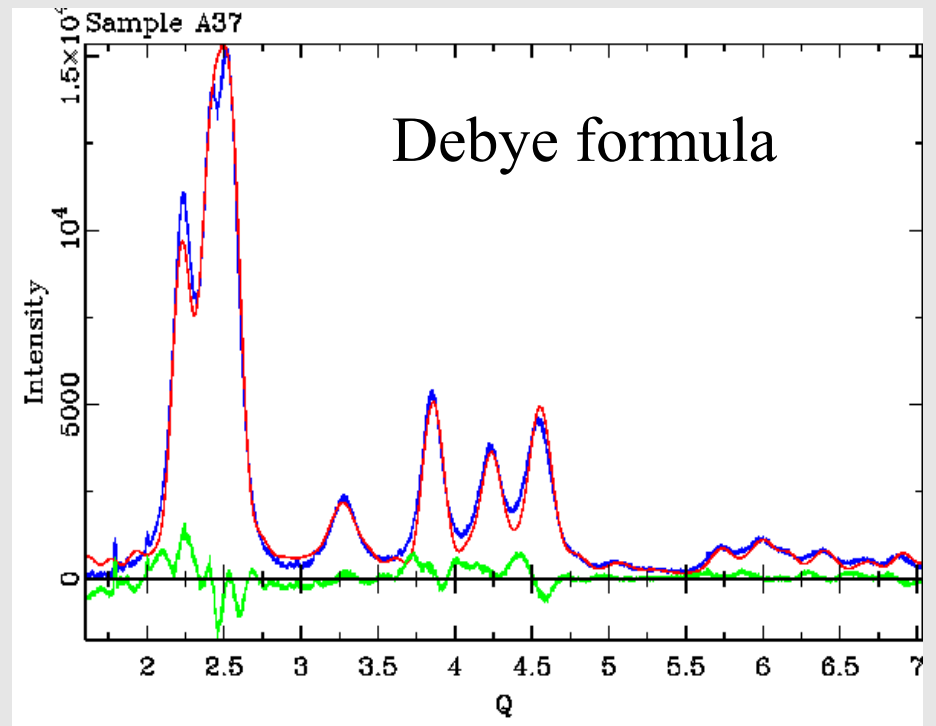
R = 8.8 %

ZnO Nanoparticles

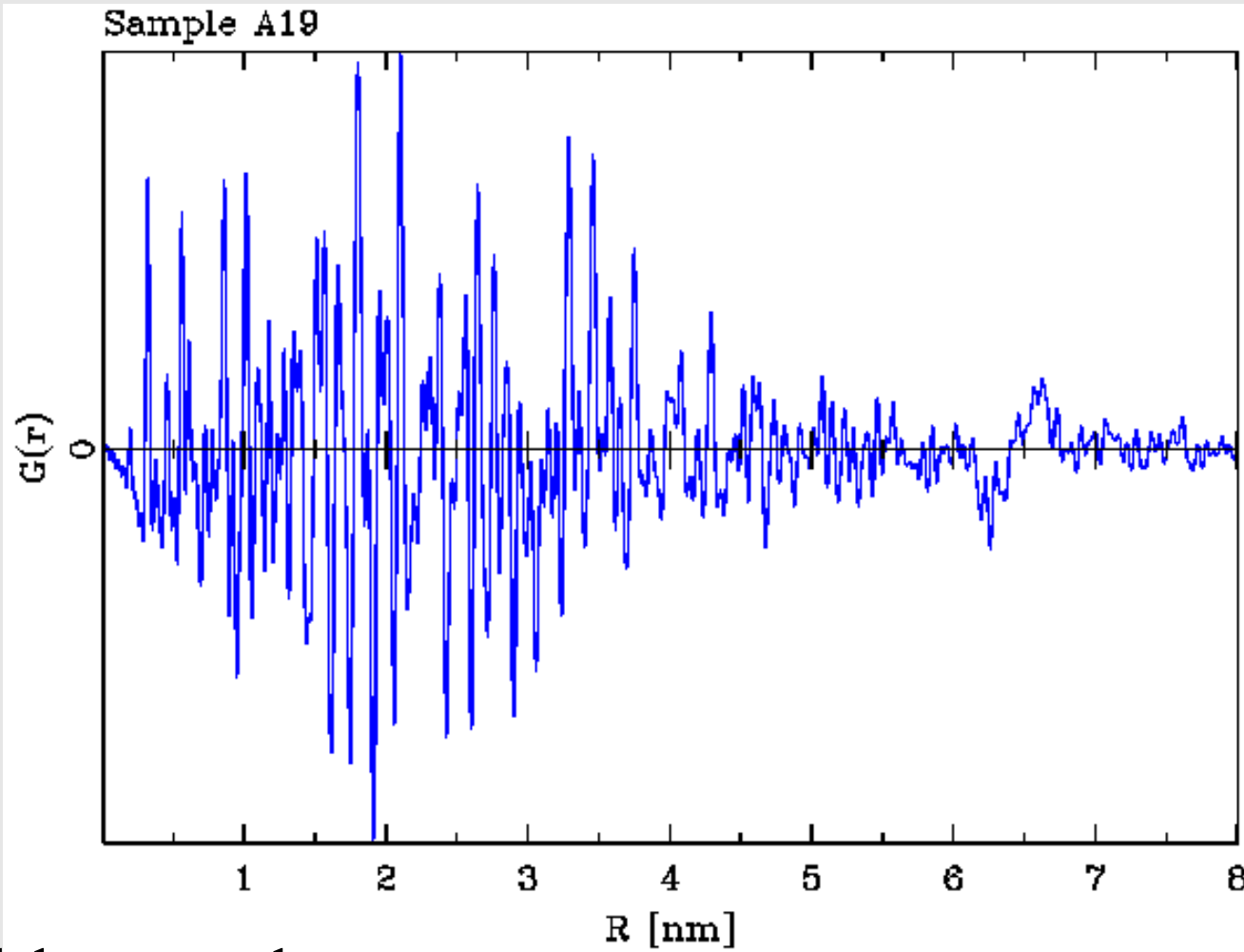


	Rietveld	Debye
a	3.269	3.256
c	5.250	5.224
z(O)	0.3876	0.3861
B	1.1	1.5

	Rietveld	Debye
size	3.2	3.6 / 3.8
prob	---	0.14



ZnO Pair Distribution Function



sharp maxima

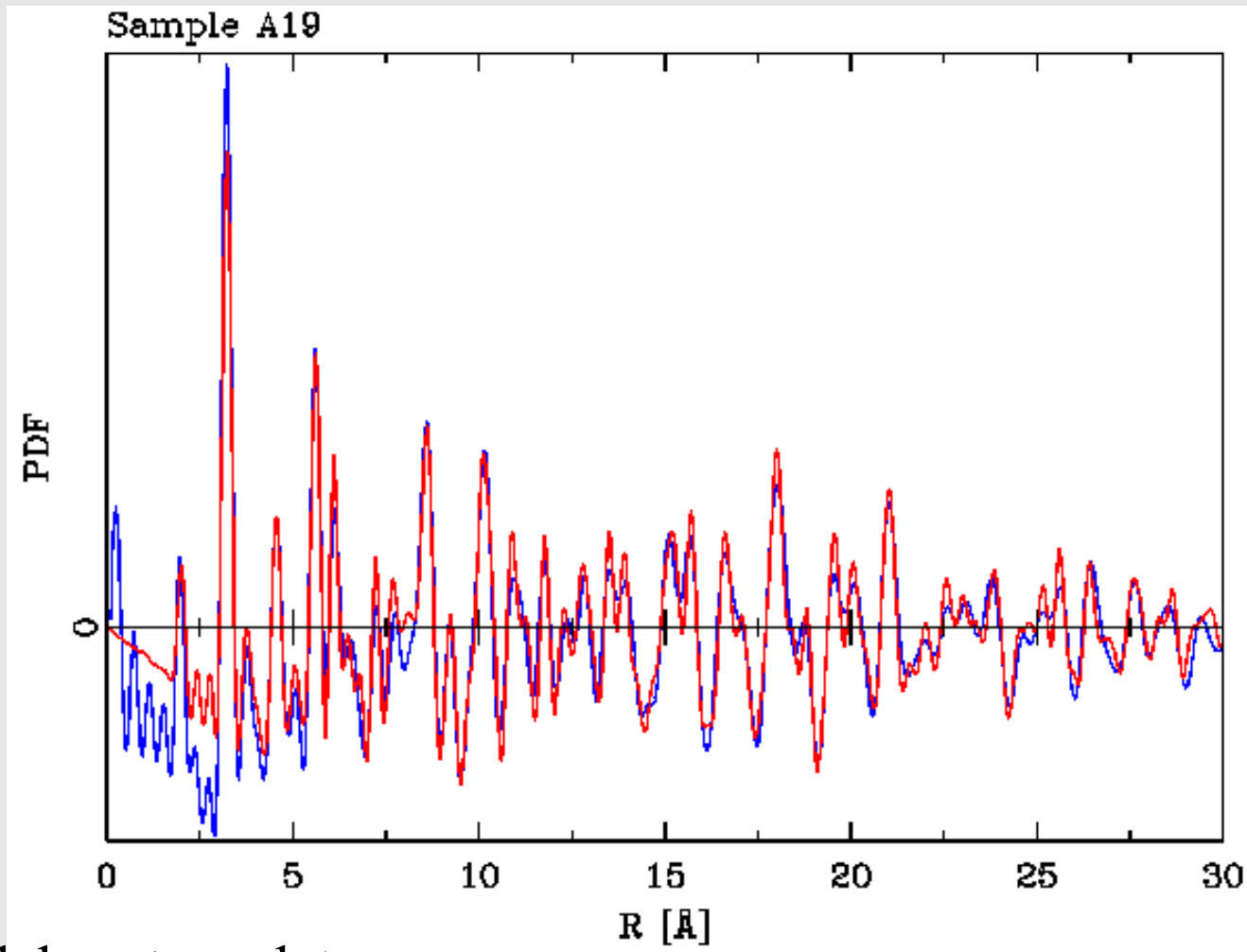
few stacking faults

Size ~ 9.5 nm

laboratory data

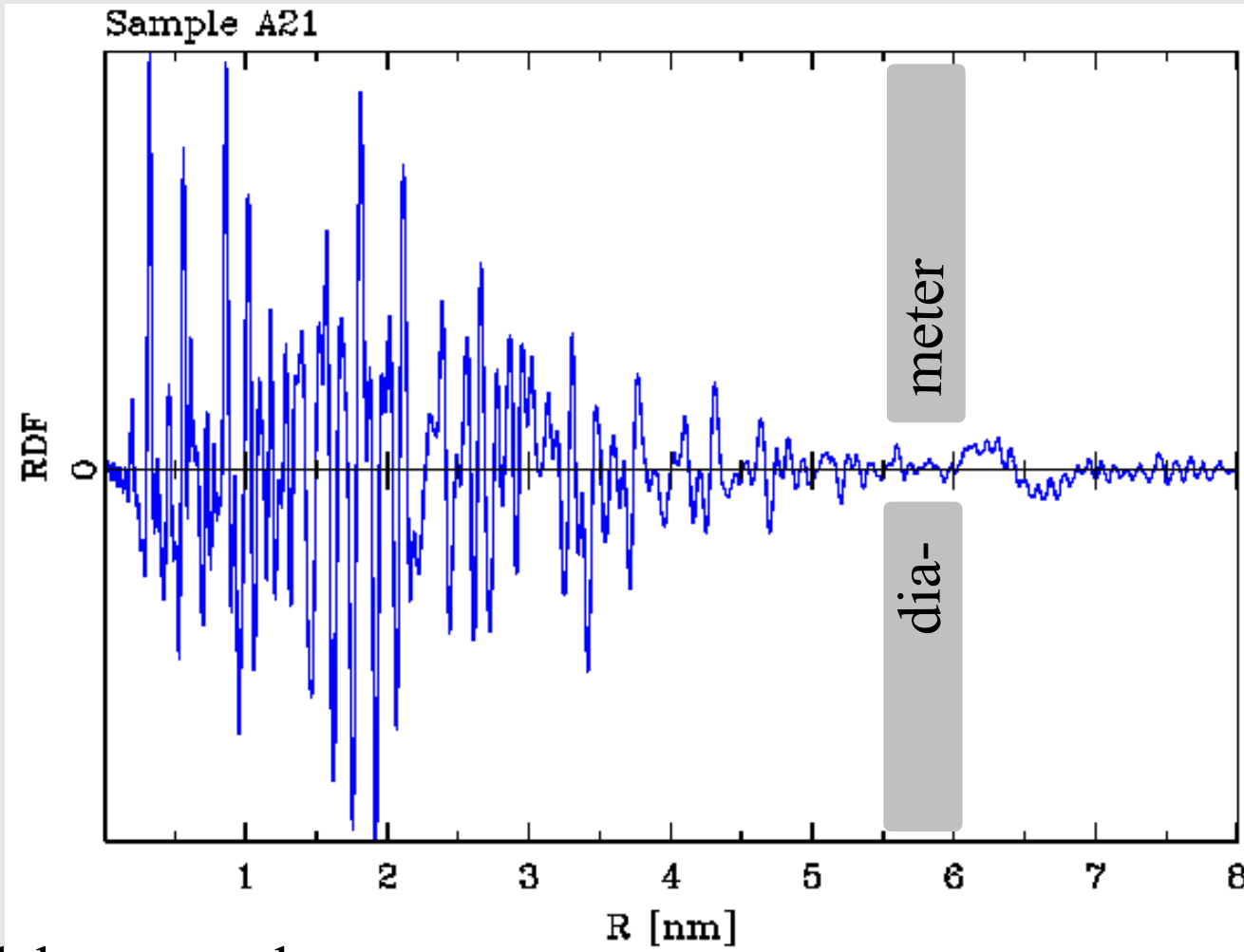
ZnO Pair Distribution Function

simulation based on periodic structure



laboratory data

ZnO Pair Distribution Function



sharp maxima

diameter ~ 5.5 nm

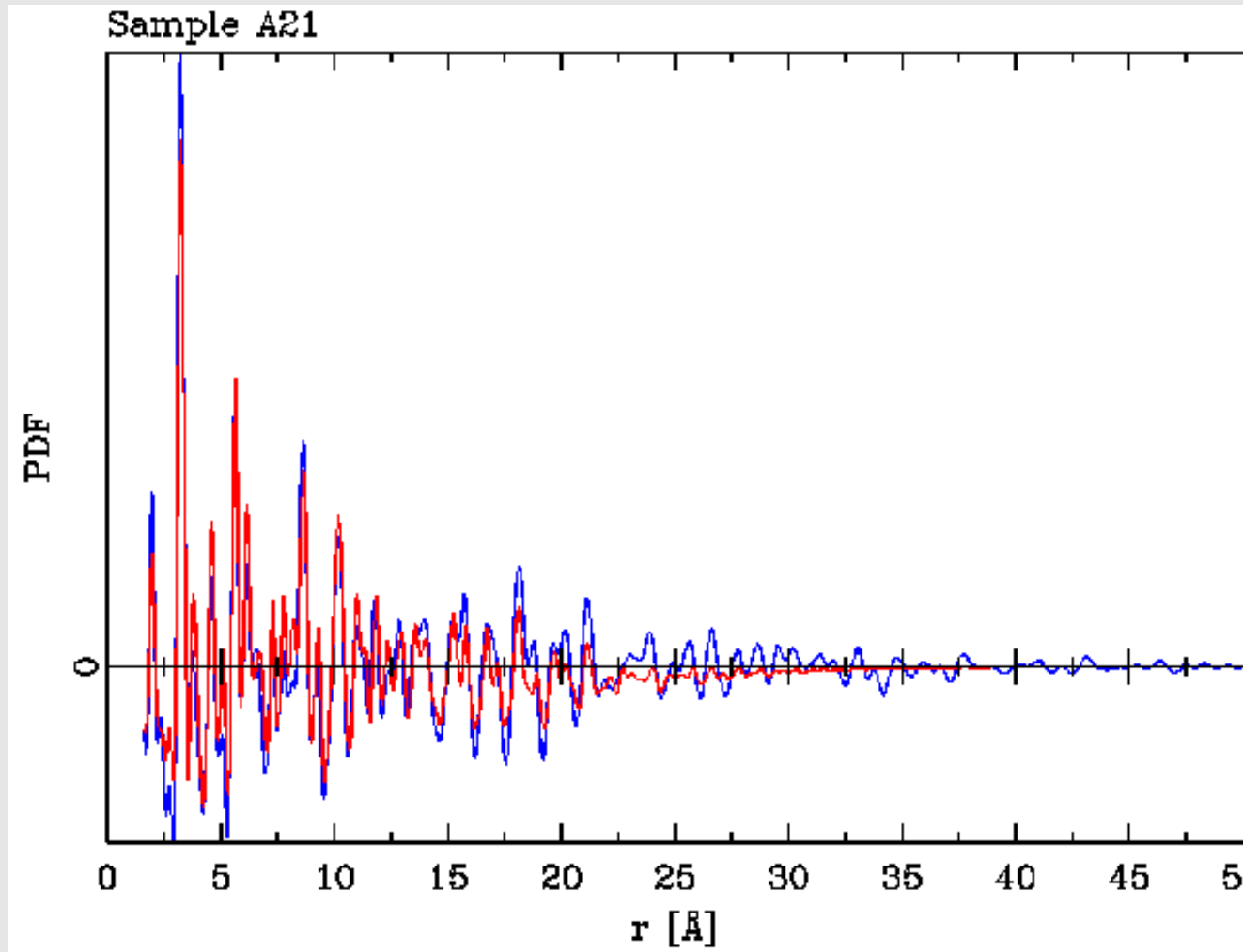
single line fit

5.0 nm

Rietveld 3.7 nm

laboratory data

ZnO Pair Distribution Function



laboratory data

prismatic crystals
no stacking faults

a

c

z(O)

B

size

	Rietveld	PDF
a	3.256	3.264
c	5.238	5.250
z(O)	0.3817	0.3836
size	38	63

ZnO Nanoparticles Fitting by Debye

Debye formula :

$$\begin{aligned} \langle |F(\mathbf{h})|^2 \rangle &= \sum_j f_j^2 + \sum_i \sum_{j \neq i} f_i f_j \sin(2\pi \mathbf{h} \cdot \mathbf{r}_{ij}) / (2\pi \mathbf{h} \cdot \mathbf{r}_{ij}) \\ &= N c_J \sum_J f_J^2 + 2 \sum_I \sum_J f_I f_J \sum_i \sum_{j > i} \sin(2\pi \mathbf{h} \cdot \mathbf{r}_{ij}) / (2\pi \mathbf{h} \cdot \mathbf{r}_{ij}) \end{aligned}$$

ZnO Nanoparticles Fitting by Debye

$$\langle |F(\mathbf{h})|^2 \rangle = N \sum_J c_J f_J^2 + 2 \sum_I \sum_J f_i f_j \sum_i \sum_{j>i} \sin(2\pi \mathbf{h} \cdot \mathbf{r}_{ij}) / (2\pi \mathbf{h} \cdot \mathbf{r}_{ij})$$

for all atom i

for all atoms j > i

compile distance r_{ij} into histogram for type IJ

compile relative fraction of atoms type I

for all atom pairs IJ

for all h

multiply histogram by $\sin(2\pi \mathbf{h} \cdot \mathbf{r}_{ij}) / (2\pi \mathbf{h} \cdot \mathbf{r}_{ij})$ (from lookup table)

multiply by $2 * f_i f_j$

for all atom type I

for all h

add $f_i^2 * \text{relative amount}$