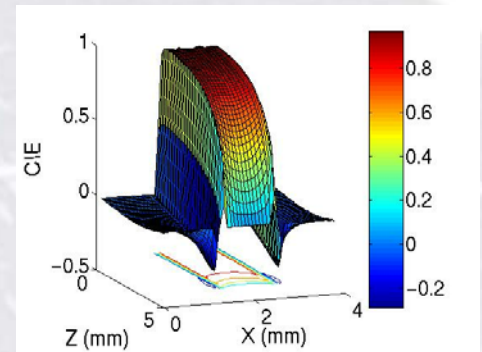
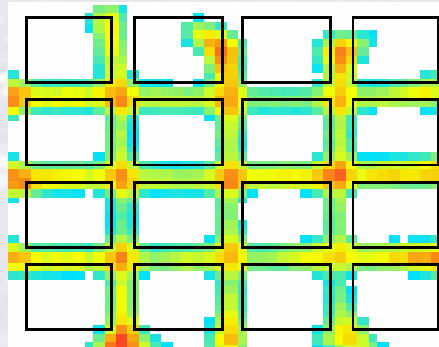
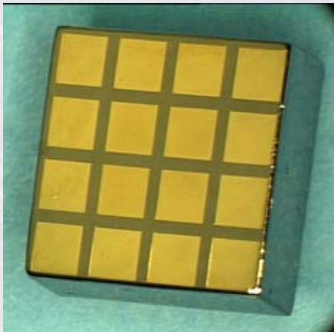


Charge Sharing on Monolithic CdZnTe Gamma Ray Detectors: A Simulation Study



E. Gros d'Aillon, L. Verger, J. Tabary, A. Glière

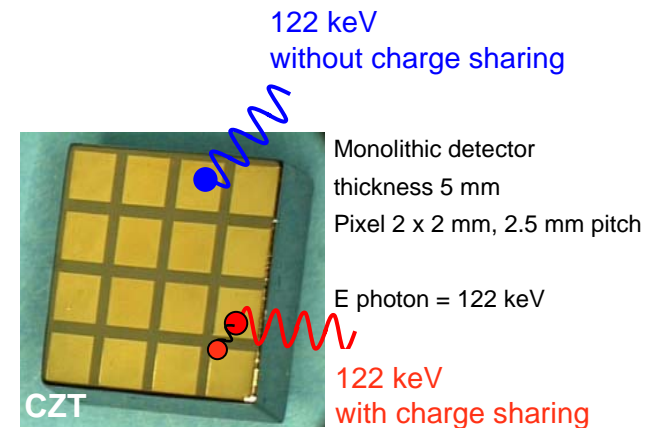
Context and outline

Factor degrading performances of monolithic CdZnTe detectors (tailing)

- Interaction depth dependence of induced signal
Affecting energy resolution
- **Charge sharing** between adjacent pixels
Affecting energy resolution or efficiency

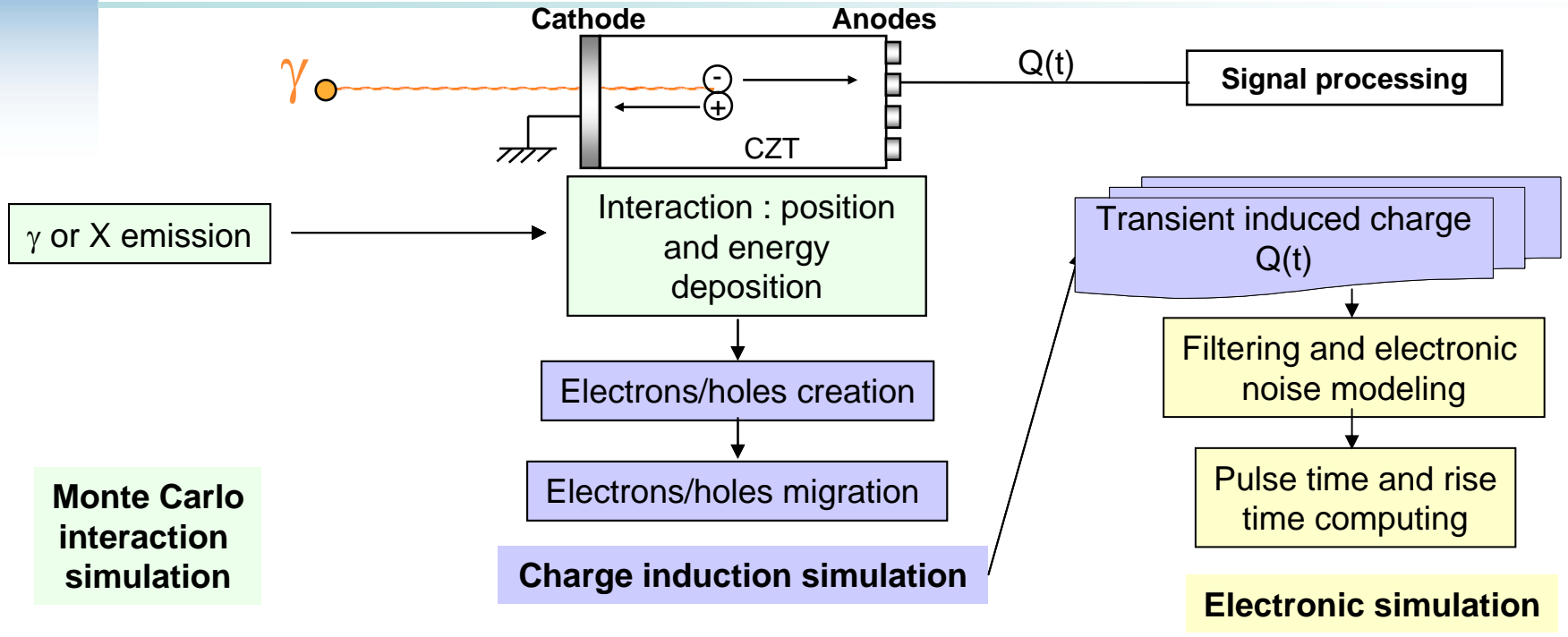
CdTe / CdZnTe Gamma Ray pixelated detectors

- Typical energy 122 keV (^{57}Co medical energy)
- Typical **pitch** 2.5 mm (between 0.2 to 3 mm)
- Typical thickness 5 mm

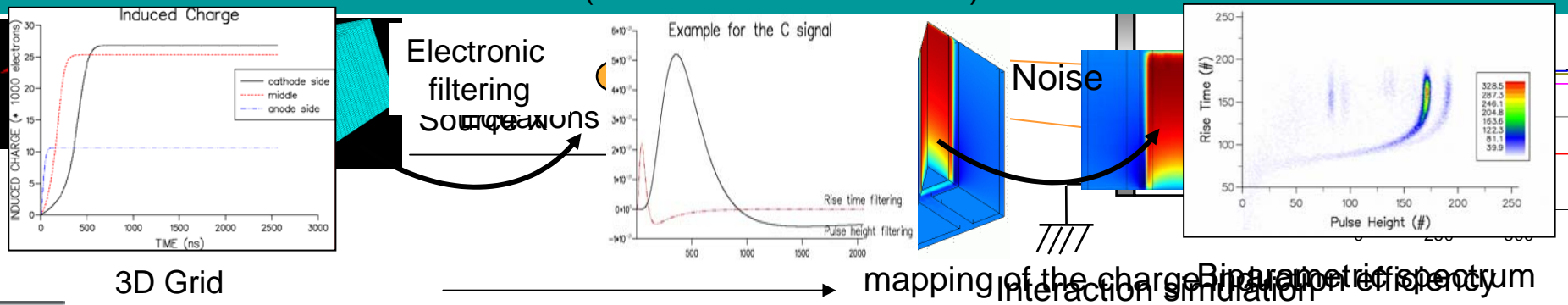


Outline

- Ulysse : 3D simulator of CZT gamma ray spectrometrer
- γ ray matter interaction \rightarrow size of the the **deposited cloud**
- Physic phenomena in **detectors** \rightarrow measured charge sharing
- First **comparison with experimentation**



Signal processing module developed in Fortran and integrated in Ulysse :
(with FemLab[®] software)



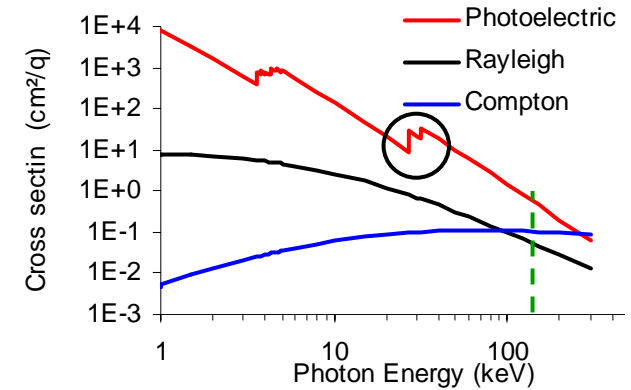
3D Grid → mapping of the charge Biparametric spectrum
Interaction simulation →

F. Mathy, A. Glière, E. Gros d'Aillon, B. Péroche, M. Pissard-Wattel, P. Scherrer, J. Sempau, E. Acosta, J. Baro, J.M. Hernandez-Varea and F. Salvat, "An algorithm for Monte Carlo simulation of the coupled electron-photon transport", NIM. B, 132, 377, 1997
J. Sempau, E. Acosta, J. Baro, J.M. Hernandez-Varea and F. Salvat, "Validation of the three-dimensional Monte Carlo simulation of the coupled electron-photon transport", IEEE TNS, 51, 9, 2004

γ ray matter interactions

At 122 keV

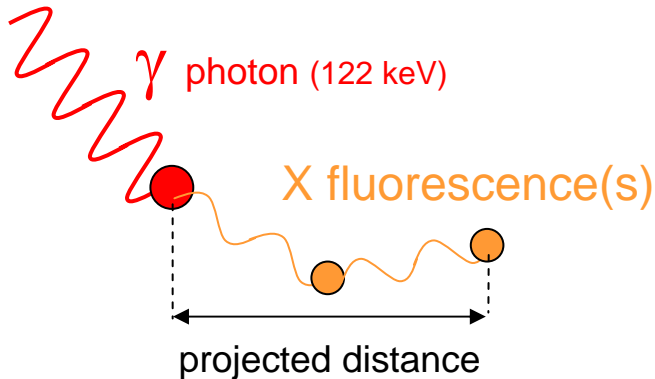
- **Photoelectric** : 82 %
 - Non radiative (Auger electrons)
 - Radiative X : Te 27 - 31 keV ; Cd 23 - 26 keV
Zn 8 - 10 keV
- Compton scattering : 11%
- Rayleigh scattering : 7%



1. Interaction
2. Interaction + induction
3. Comparison with experimentation

Nb secondary photon	Ratio	Mean distance
0 (Auger)	25 %	0 μm
1 fluorescence	45 %	75 μm
2 fluorescences	25 %	111 μm
> 2 fluorescences	5 %	118 μm
Mean distance X photons	75 %	90 μm
Mean distance (all)	100 %	67 μm

Monte Carlo simulation : PENELOPE

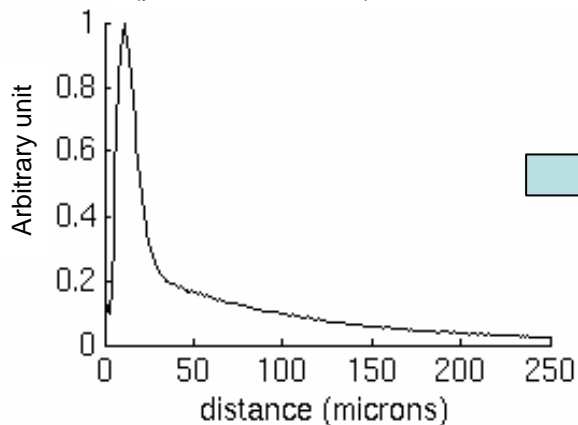


Electron cloud size at its creation

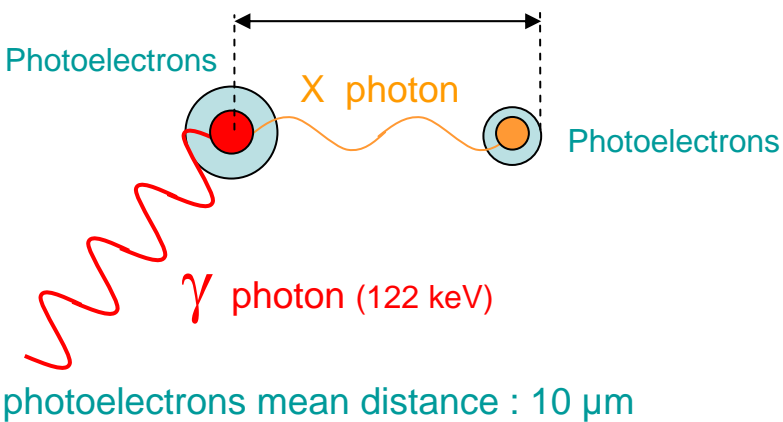
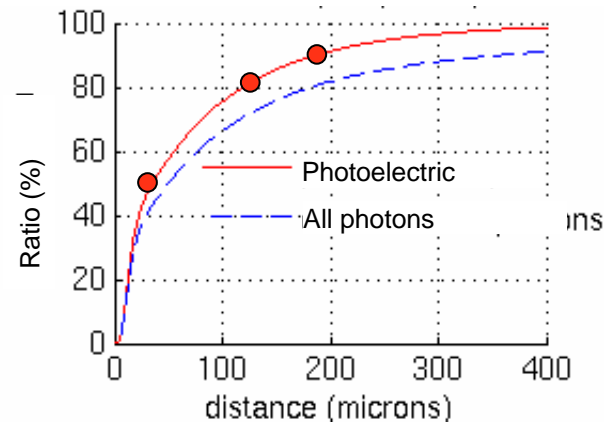
Monte Carlo simulation

1. Interaction
2. Interaction + induction
3. Comparison with experimentation

Distribution of events in function of size (photoelectric effect)



Ratio of events which size is inferior to the distance in abscise



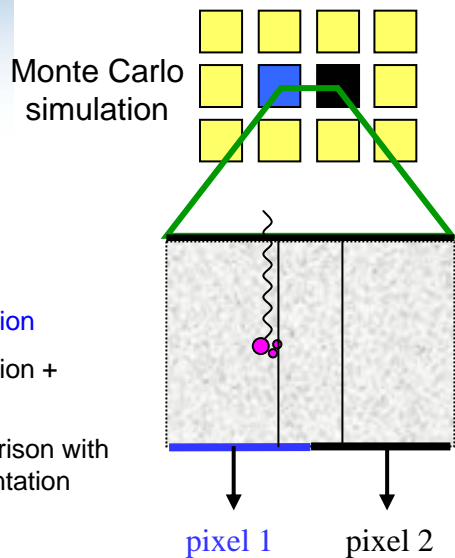
For photoelectric effect

50 % of events : size inferior to **36 μm**

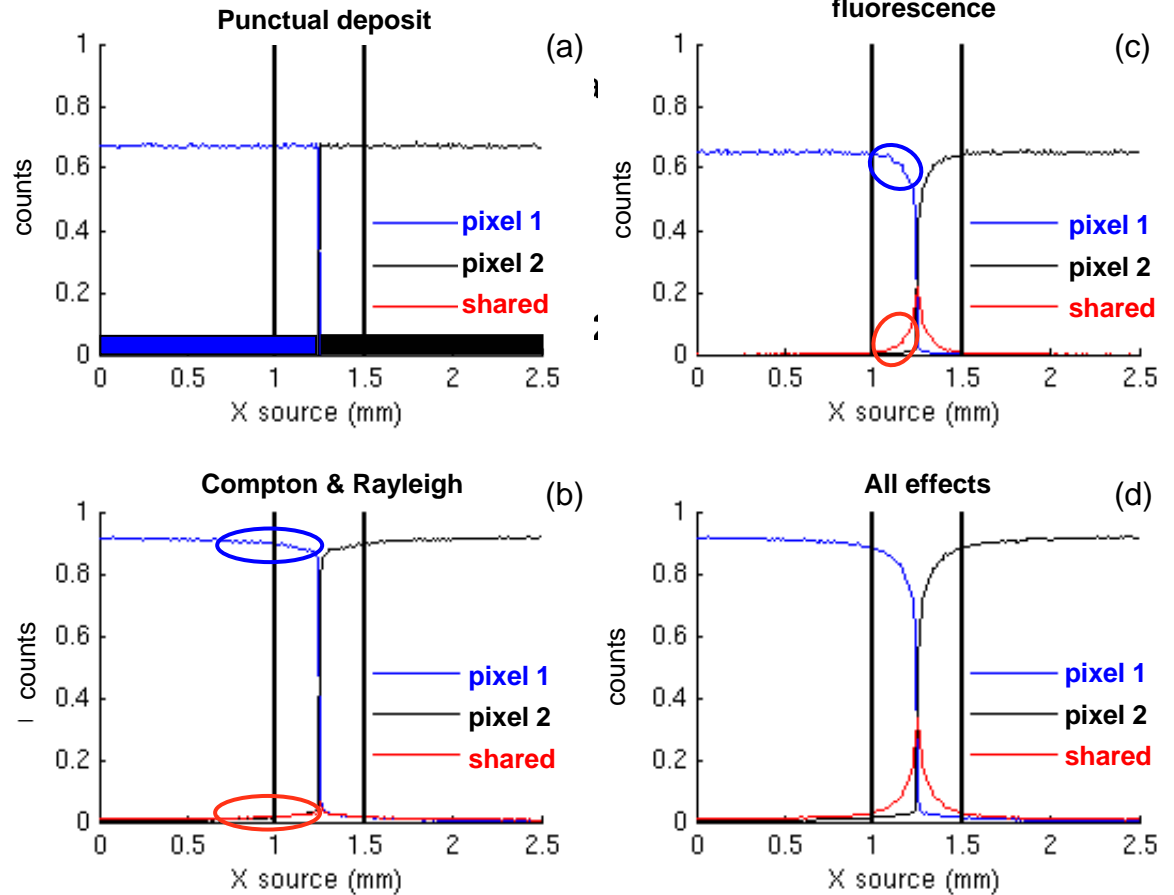
80 % of events : size inferior to **120 μm**

90 % of events : size inferior to **190 μm**

Monte Carlo study: the deposit cloud



Ratio of shared events according to deposited position



E photon = 122 keV
Threshold = 15 keV
Perfect electric field or jointed anode

The distance to which charge sharing occurred is **500 μm** .

Charge sharing is important for **80 μm** (FWHM).

- **for other photon energy :**

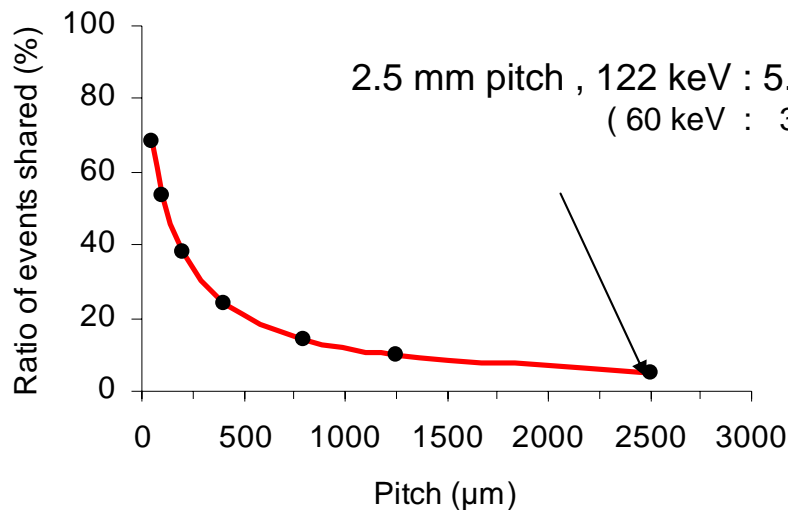
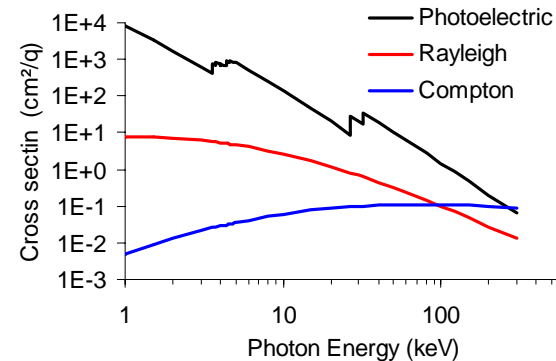
- cross section ratio depends on energy : photoelectric ratio : 140keV 78% ; 122keV 83% ; 60keV 95%
- X fluorescence occurred until 32 keV (Kedge)

- **for other threshold:**

- low effect as long as threshold < Kedge

- **for other pitch (irradiation on the full detector surface) :**

- shared events ratio increases up to 75 % (Auger)
- then reach a plateau until 10 μm (photoelectron)

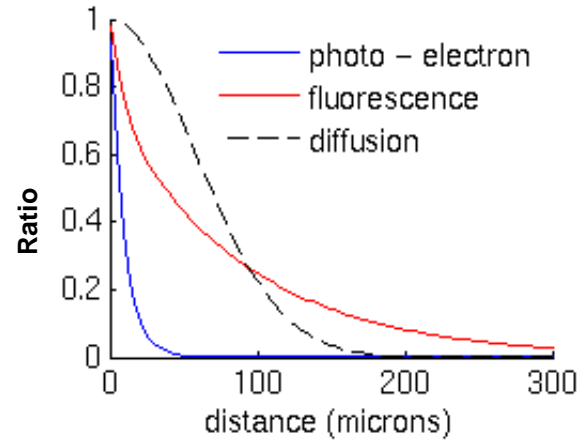
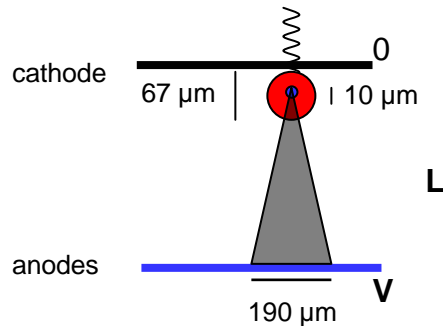


1. Interaction

2. Interaction + induction

3. Comparison with experimentation

Electron cloud diffusion in the detector



Fluorescence : some photons
≠ Diffusion : all electrons clouds

$\sigma = 190 \mu\text{m FWHM}$ (80 $\mu\text{m rms}$)

(planar projection)
$$\sigma_D = \sqrt{\frac{4DL^2}{\mu V}}$$

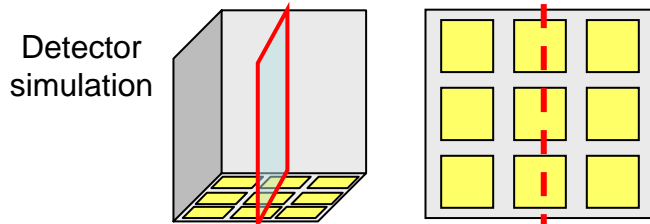
$D_{\text{CdTe}} = 0.0026 \text{ m}^2/\text{s}$
 $\mu = 0.1 \text{ m}^2/\text{V/S}$
 $L = 5 \text{ mm}$
 $V = 400 \text{ V}$

diffusion constant $D = k_B T \mu / e$
 electron mobility
 detector **thickness**
 applied **bias**

Nuclear medicine : $E = 140 \text{ keV}$, CdTe thickness = 5 mm, $V = 300 - 1000 \text{ V} \rightarrow \sigma_D = 120 - 220 \mu\text{m FWHM}$

Simulation of the detector: CIE computation

Computation of the **Induced Charge** on each electrode



Bias 400 V
Electron life time 3 μs
Electron mobility 1000 cm²/V/s

τ	1 - 5 μs	electron lifetime
σ	10 ⁻⁹ Ω ⁻¹ cm ⁻¹	conductivity
ϵ_r	11	permittivity
μ_n	0.1 m ² V ⁻¹ s ⁻¹	electron mobility
G	cm ⁻³ s ⁻¹	electron generation

approximations: conductivity and trapping are homogeneous in the bulk

1. Interaction
2. Interaction + induction
3. Comparison with experimentation

Applied potential
charge transport

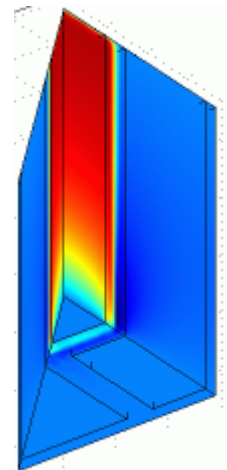
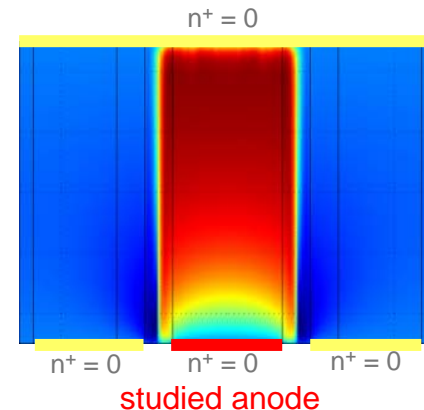
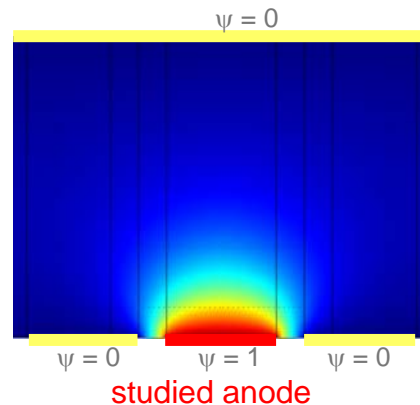
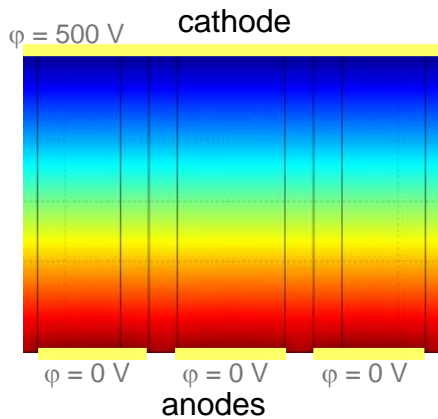
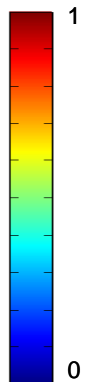
$$\vec{\nabla} \sigma \vec{\nabla} \phi = 0$$

Weighting potential
charge induction

$$\vec{\nabla} \epsilon \vec{\nabla} \psi = 0$$

Charge Induction Efficiency
Ratio measured charge on deposited charge

$$CIE = \frac{Q}{Q_0} = \int_t \left(\iiint_{\Omega} q \mu_n n \vec{\nabla} \phi \vec{\nabla} \psi d\Omega \right) dt$$

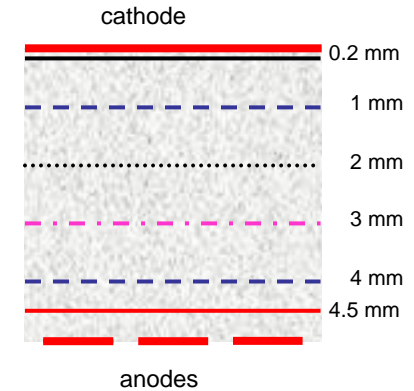
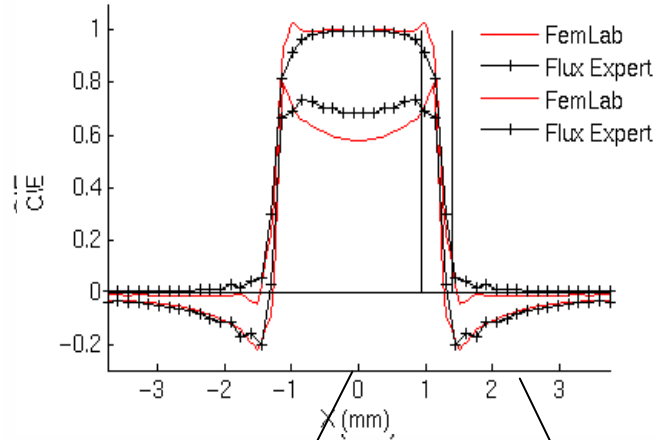


The **CIE** map contains the whole information to model the detector (i.e. signals induced by an interaction in any point in the detector)

The Charge Induction Efficiency

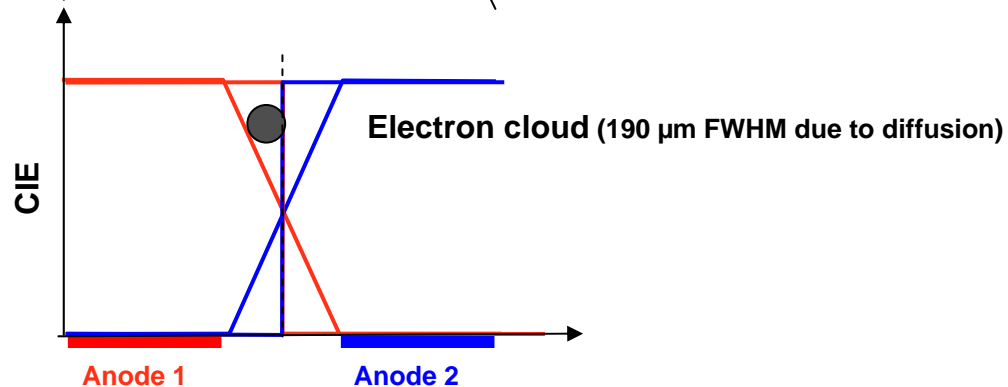
Detector simulation

Comparison between FemLab and Flux Expert computation

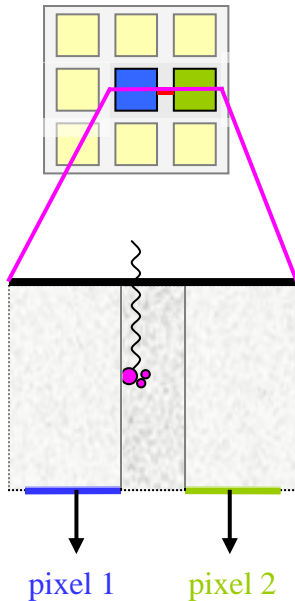


1. Interaction
2. Interaction + induction
3. Comparison with experimentation

CIE decrease from maximum to negative value is not abrupt
Distance => 500 μm due to **diffusion**
Independent on numerical parameters



Monte Carlo
+
Detector



1. Interaction
2. Interaction + induction
3. Comparison with experimentation

- counts on pixel 1
- counts on pixel 2
- counts shared

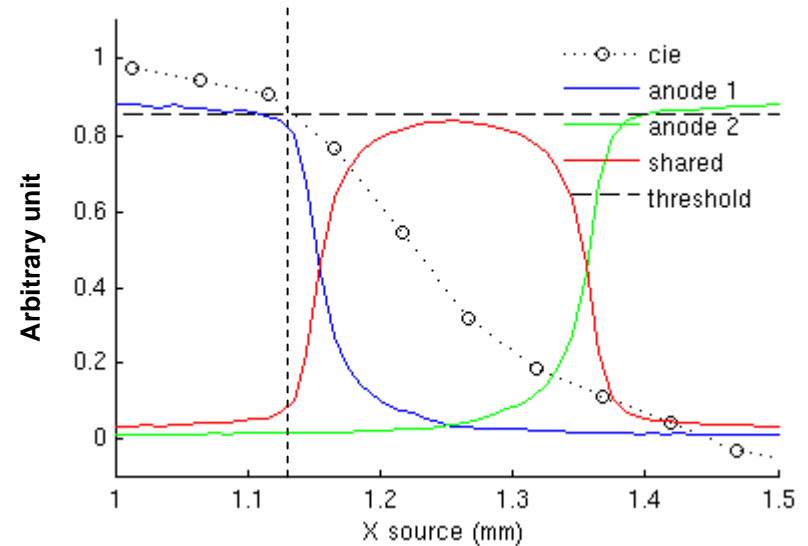
According to Interaction position

Bias 400 V
Electron life time 3 μ s
Electron mobility 1000 cm²/V/s

E photon = 122 keV
Threshold = 15 keV

Monolithic detector
thickness 5 mm
Pixel 2 x 2 mm, 2.5 mm pitch

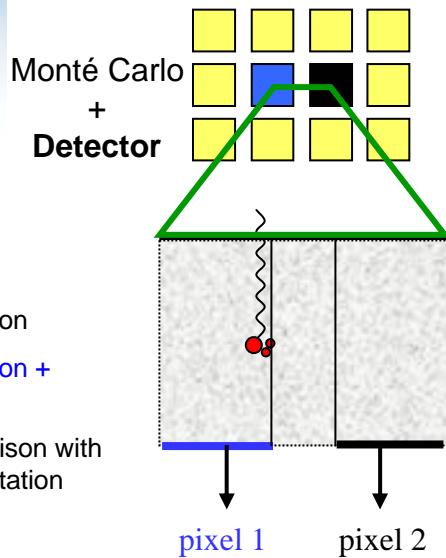
CIE ρ Induced charge : Monte Carlo + detector ρ



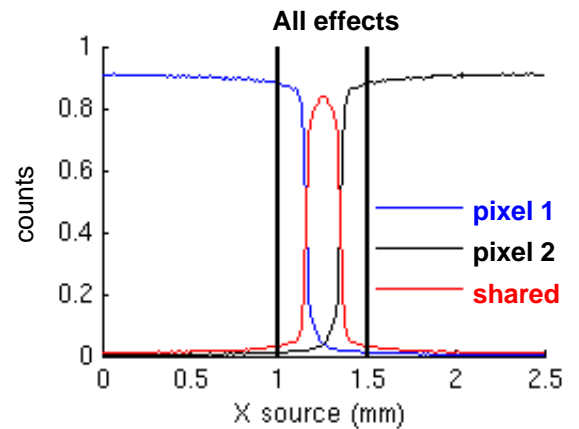
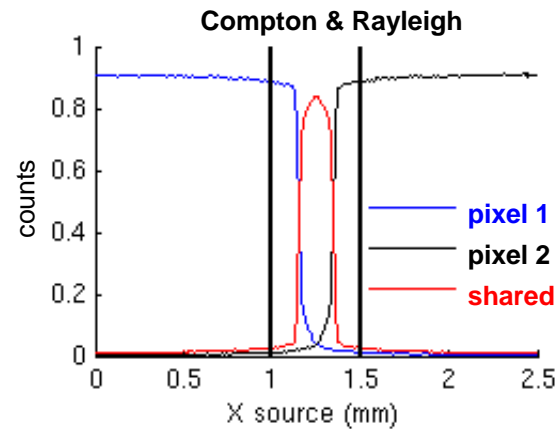
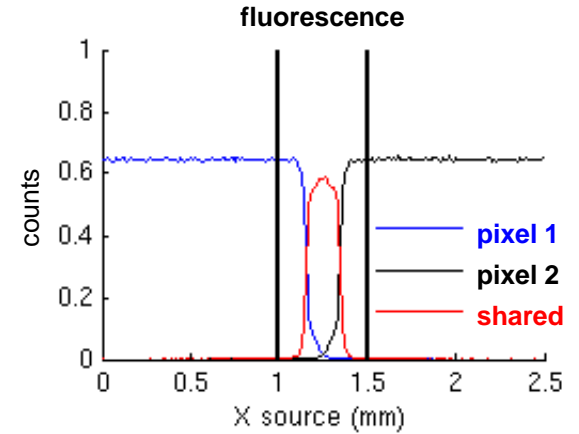
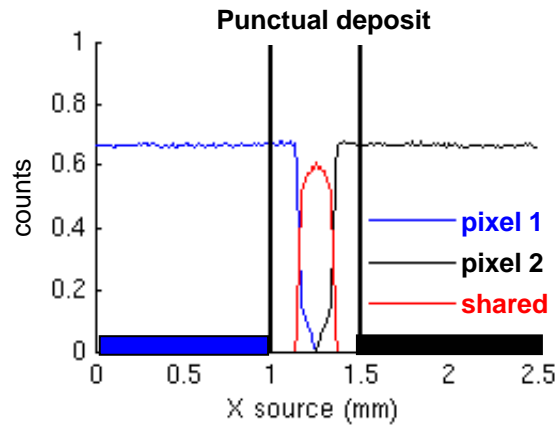
charge sharing : 210 μ m FWHM
recall : diffusion = 190 μ m FWHM

Diffusion enlarge charge sharing area from 80 μ m to 210 μ m FWHM

Monte Carlo and detector study



Ratio of shared events according to deposited position



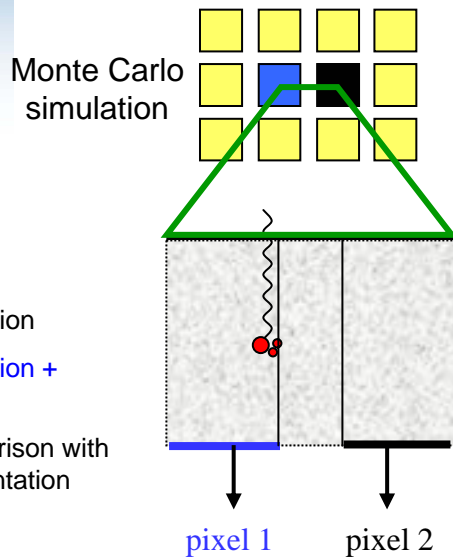
Bias 400 V
Electron life time 3 μ s
Electron mobility 1000 cm²/V/s

E photon = 122 keV
Threshold = 15 keV

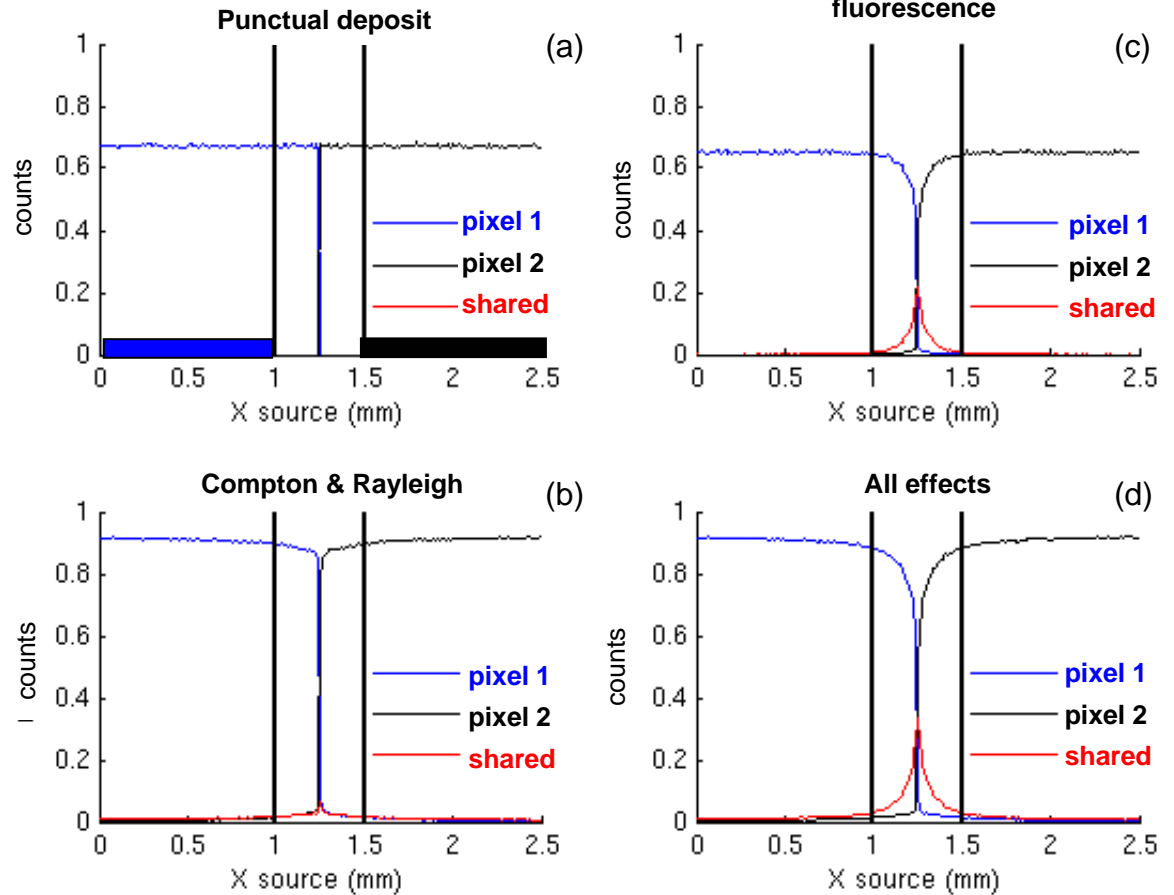
Monolithic detector
thickness 5 mm
Pixel 2 x 2 mm, 2.5 mm pitch

In this situation, the main effect on charge sharing is **electron cloud diffusion**

Monte Carlo study: the deposit cloud



Ratio of shared events according to deposited position



E photon = 122 keV
Threshold = 15 keV

Monolithic detector
thickness 5 mm
Pixel 2 x 2 mm, 2.5 mm pitch

The charge sharing distance occurred in **500 μm** .

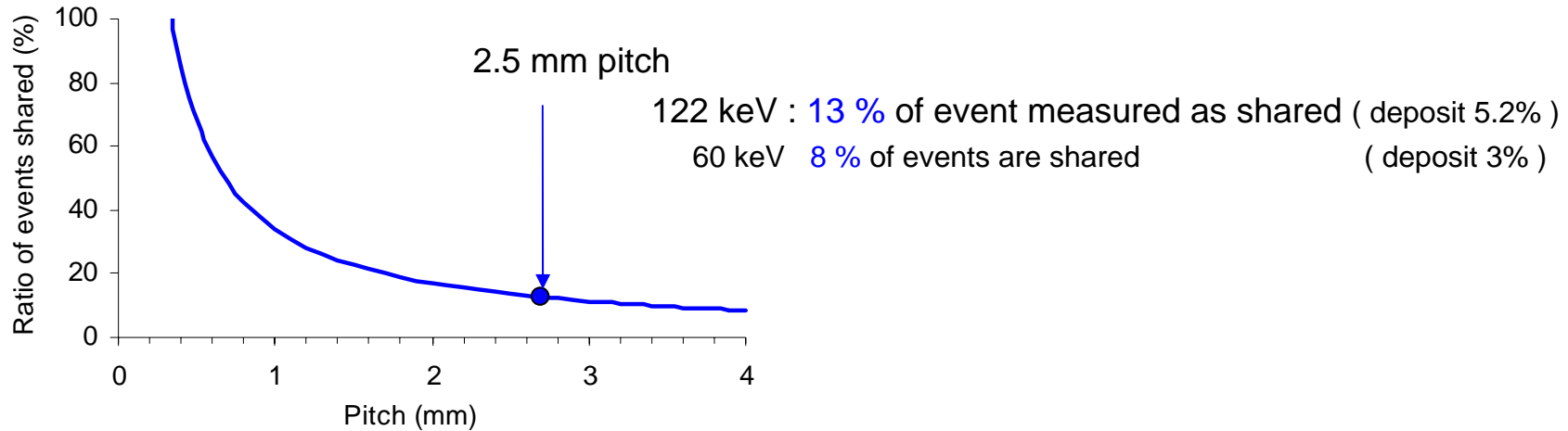
Charge sharing is important for **80 μm (FWHM)**.

- **for other detector geometry :**

- gap : no effect on charge sharing (if it is insulating)
- thickness and bias : little effect on diffusion
- pitch and thickness → pixel effect

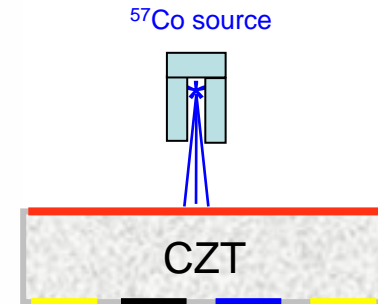
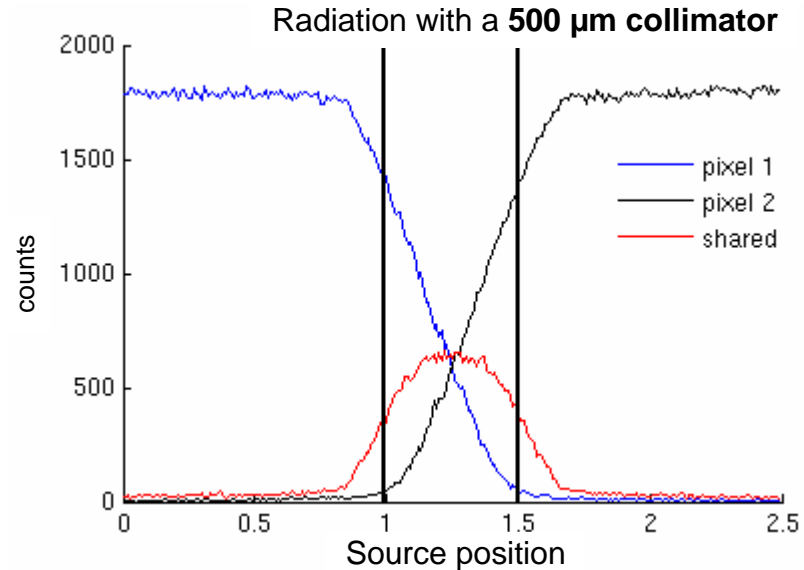
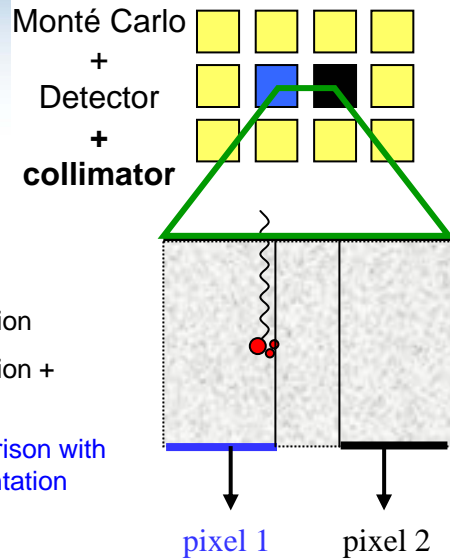
- **for other pitch** (irradiation on the full detector surface) :

- charge sharing increases drastically for pitch < 1 mm



1. Interaction
2. Interaction + induction
3. Comparison with experimentation

Simulation with a 500 μm collimator



Bias 400 V
Electron life time 3 μs
Electron mobility 1000 $\text{cm}^2/\text{V}/\text{s}$

E photon = 122 keV
Threshold = 15 keV

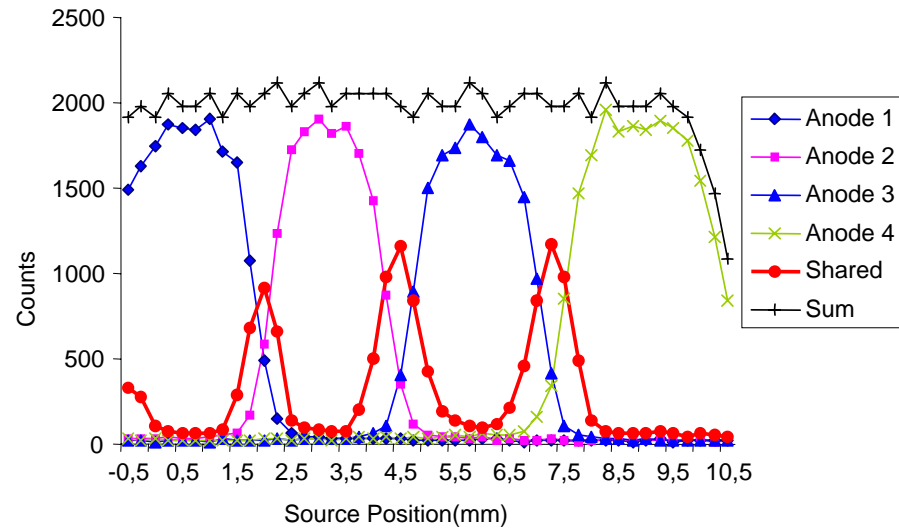
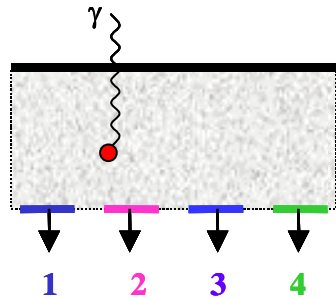
Monolithic detector
thickness 5 mm
Pixel 2 x 2 mm, 2.5 mm pitch

Collimator Pb 500 μm

Charge sharing FWHM : 570 μm to compare to 210 μm with a straight source

Collimator width will hide other effects

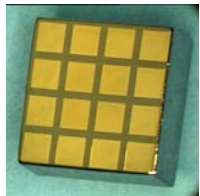
Experimentation with a 500 μm collimator



Events sharing FWHM : 500 – 800 μm

Simulation : charge sharing FWHM = 570 μm

1. Interaction
2. Interaction + induction
3. Comparison with experimentation



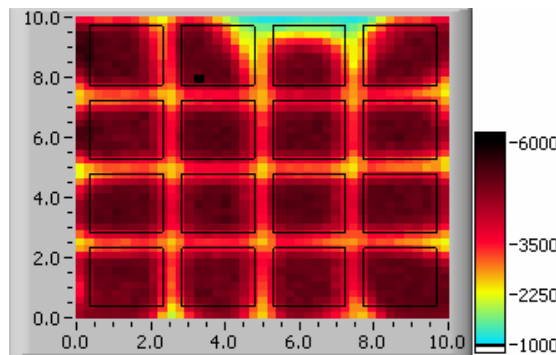
HPBM CZT monolithic detector
thickness 5 mm
Pixel 2 x 2 mm, 2.5 mm pitch

Bias 400 V

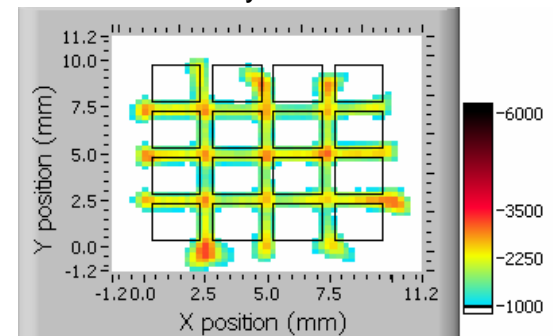
E photon = 122 keV
Threshold = 15 keV

Collimator Pb 500 μm

Events measured by one single anode



Events measured by more than one anode



On the full area 10 % of events are shared

Recall : in simulation 13 % of event measured as shared

Monte Carlo Study only : the deposit cloud

• Gamma ray – matter interaction

Photoelectric effect : 82 % :

Mean distance of fluorescence (75 %) **90 μm**

Mean distance (all) **67 μm**

Photoelectron range **10 μm**

• Fluorescence

For photoelectric effect considering photoelectron range

50 % of events : size inferior to 36 μm

80 % of events : size inferior to 120 μm

90 % of events : size inferior to 190 μm

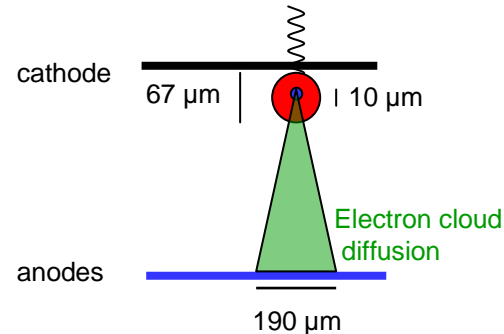
For all events, **charge sharing FWHM 80 μm** (\rightarrow 500 μm)

• Pixilated detector

For a 2.5 mm pitch detector

- At 122 keV : **5.3 %** of events are shared

- At 60 keV : 3 % of events are shared



E photon = 122 keV

Threshold = 15 keV

Monolithic detector

thickness 5 mm

Pixel 2 x 2 mm, 2.5 mm pitch

Bias 400 V

Electron life time 3 μs

mobility 1000 $\text{cm}^2/\text{V/s}$

Monte Carlo + Induction in the Detector

- Diffusion enlarge **charge sharing** to **210 μm** FWHM

• Pixilated detector

For a 2.5 mm pitch detector

- At 122 keV : **13 %** of event as shared (10% experimentally)

- At 60 keV : 8% of events are shared

thank you for your attention

Diffusion, thickness and bias

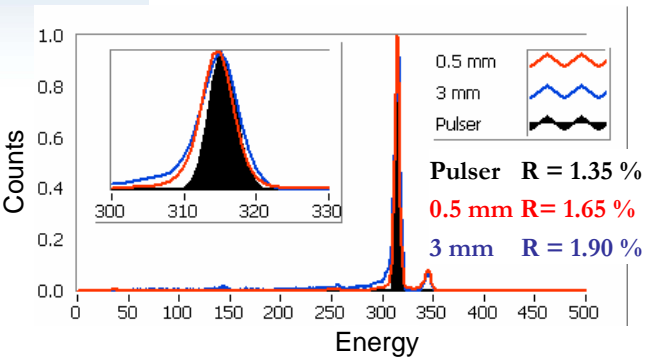
Diffusion is independent of thickness and bias because bias is chosen to collect charge (mean free path \gg thickness)
But bias must not be too high to limit noise

Diffusion $\sigma_D = \sqrt{\frac{4DL^2}{\mu V}}$

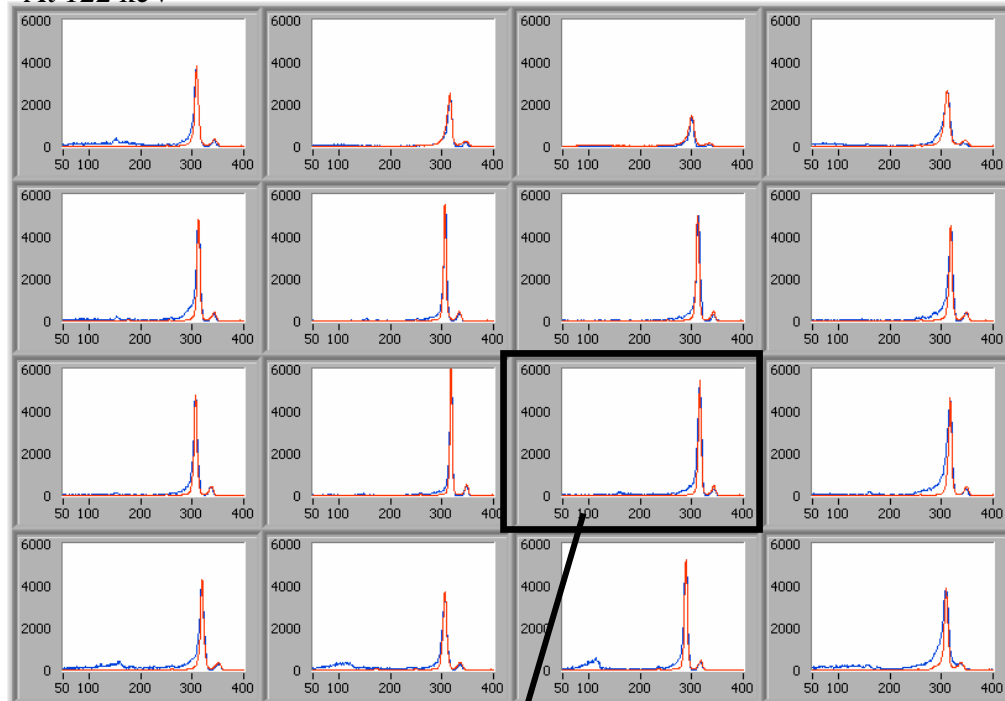
mean free path \gg thickness $\frac{\mu\tau V}{L} \gg L \implies \frac{\mu\tau V}{L} \approx \alpha L \implies V \approx \alpha L^2 / \mu\tau$

Diffusion $\sigma_D^2 = 4D\tau / \alpha$

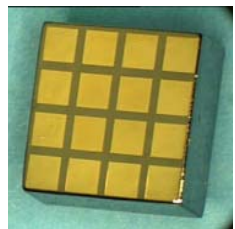
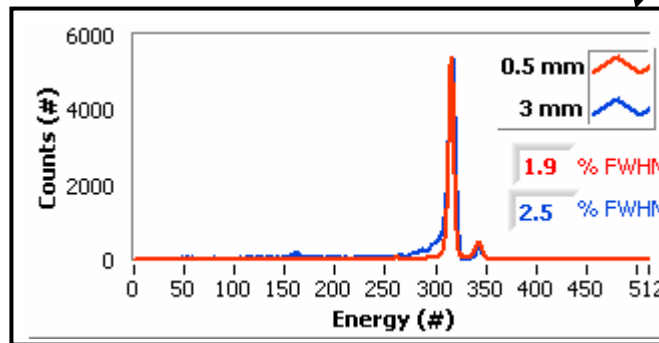
Good pixel



At 122 keV



3 mm collimator $R = 3\% \pm 0.7\%$
0.5 mm collimator $R = 2.46\% \pm 0.64\%$



MVB CZT monolithic detector
thickness 5 mm
Pixel 2 x 2 mm, 2.5 mm pitch

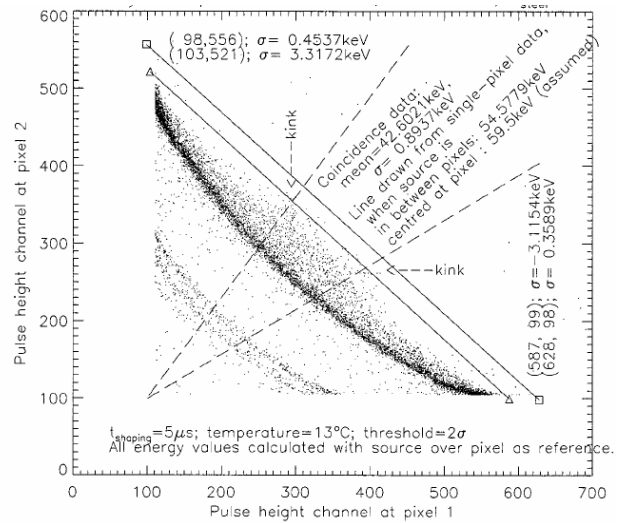
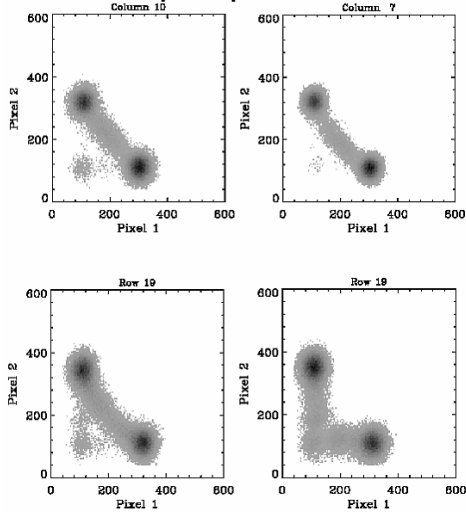
Bias 700 V

E photon = 122 keV
Threshold = 15 keV

Collimator Pb 500 μ m / 3mm

Treatments

Scatter plot pixel 1 versus pixel 2



Distinction between charge sharing and charge loss

